**Deviations of the “Hubble Constant” Value
and the increasing deviations of the
“James Webb Space Telescope Constant” Value
within a “Spherical Gravitational Indentation
Originating from the Milky Way Galaxy”
in a 4-dimensional Space-Time Continuum**

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*The Calculations (Mathematica 13.0) which belong
to this article can be downloaded at the Download Page
<https://quantumlight.science/>*

Abstract

The “Hubble Constant” Value and specially the deviations in the “Hubble Constant” Value are one of the most fundamental parameters in our universe to understand the fine-structure of our 4-dimensional Space-Time continuum. Recent measurements with the “HST” of the “Hubble Constant” and the measured deviations^[Ref. 17] reveal fundamental information of the fine-structure of our 4-dimensional Space-Time continuum. The New Theory about the interaction between “Gravity and Light” offers an easy way to calculate the extra Gravitational “Blueshifts” when a Beam of Light (from a far away Galaxy) enters our “Milky Way Galaxy” and a second “Blueshift” when the Beam of Light enters the Gravitational Field around the Earth. And additional Gravitational Redshift has been created when a Beam of Light (from a far away Galaxy) leaves the Gravitational Field of the far away Galaxy. All these

interactions between Gravity and Light disturbs the accuracy of the, by “HST” measured, “Hubble Constant” Value.

With increasing accuracies the need increases of a “New Theory in Physics” to explain the measured anomalies in the “Hubble Constant” value. Because “General Relativity” is not enough anymore to solve the nowadays problems in physics and specially in astronomy. With increasing accuracies the anomalies in the “Hubble Constant” value only become clearer. To develop a “New Theory in Physics” fundamental corrections have to be made in 2 of the 4 foundations in Physics. Corrections have to be made in Maxwell’s Electrodynamics and Bohr’s Quantum Mechanics. A fundamental problem in the value of the “Hubble Constant” is that we measure with a very precisely instrument the “HST” which is looking a little bit with “crossed eyes”. Because the galaxies are not really there where “HST” measures it. The intensities are not really that value which the “HST” measures and therefore the distances are differently than the “HST measures and also the redshift is different than which the “HST measures. Because the “HST” has been designed for an Euclidean (linear) universe. And the universe is not Euclidean at all. Gravity is everywhere in the universe and for that reason the universe is not Euclidean. “GR” is not enough, it is not big enough to correct the values for the “HST”.

The impact of the gravitational field around our “Milky Way Galaxy” on our “HST” measurements are nothing compared to the real enormously gigantic and intense gravitational fields in our Galaxy. With our very accurate measurements we measure a non existing universe. The real “Non Euclidean” universe is very differently.

[“The James Webb Space Telescope”](#) (sometimes called JWST or Webb) is an orbiting infrared observatory that will

complement and extend the discoveries of the Hubble Space Telescope, with longer wavelength coverage and greatly improved sensitivity. The longer wavelengths enable Webb to look much closer to the beginning of time and to hunt for the unobserved formation of the first galaxies, as well as to look inside dust clouds where stars and planetary systems are forming today”. The “JWST” will reveal the non Euclidean Universe. And will be a fundamental test for equation (113) as a result of a new kind of physics.

Isaac Newton, James Clerk Maxwell, Niels Bohr and Albert Einstein lived in fundamentally different time frames. Newton in the 16th century, Maxwell in the 18th century, Bohr in the 20th century and Einstein was physically living in the 20th century but he was his time far ahead and with his concept of a “**curved space-time continuum**” more connected to the 21st century.

Keywords: General Relativity; Quantum Physics; Dirac Equation; Gravitational-Electromagnetic Interaction; Black Holes; Gravitational-Electromagnetic Confinement; Electromagnetism; Quantum Optics

1. The Fundamental Correction in Maxwell's Theory of Electrodynamics

To find a new “Fundamental Electromagnetic Equation” to describe the Electromagnetic field (including Electromagnetic Interaction) in a different and more complete way than Maxwell did (Einstein called Maxwell the greatest physicist of his century), we have to go back to the time of [Isaac Newton](#) who published in 1687 in the “Philosophiae Naturalis Principia Mathematica” a Universal Fundamental Principle in Physics. “**The Fundamental Principle of Harmony in the Whole Universe**” based on his religious understanding of the “**Creator of the Universe**”. Newton expressed this “**Harmony**” in the foundation of a “**Universal Equilibrium**” and he expressed the “**Universal Equilibrium**” in his **third Law** on which all Physics (till now) has been based.

1.1 Newton's approach to Electrodynamics and Electromagnetic Interaction based on Newtonian Physics.

Newton found the concept of “Universal Equilibrium” which he formulated in his famous third equation Action = - Reaction. In nowadays math the concept of “**Universal Equilibrium**” has been formulated as:

$$\sum_{i=0}^{i=n} \overline{F_i} = 0 \quad (1)$$

Because the Inertia Force is a Reaction Force, the Inertia Force appears in the equation with a minus sign.

$$\sum_{i=0}^{i=n} \overline{\mathbf{F}}_i - m \overline{\mathbf{a}} = 0 \quad (2)$$

Equation (2) is a general presentation of [Newton's famous second law of motion](#). In a fundamental way, Newton's second law of motion describes the required electromagnetic equation for the Gravitational-Electromagnetic Interaction in general terms, including [Maxwell's theory of Electrodynamics](#) published in 1865 in the article: "[A Dynamic Theory of the Electromagnetic Field](#)" and Einstein's theory of [General Relativity](#) published in 1911 the article: "[On the Influence of Gravitation on the Propagation of Light](#)".

Because Maxwell's 4 equations are not part of one whole uniform understanding of the universe like the fundamental equation of Newton's second law of motion represents, Maxwell's theory is missing the fundamental foundation.

Newton's second law of motion has been based on a profound understanding of the universe which is based on the fundamental principle of "**Harmony and Equilibrium**", expressed in equation (2).

To realize the new "Gravitational-Electromagnetic Equation", Newton's second law of motion will be the Universal Concept in Physics on which "**Quantum Light Theory**" will be built. The fundamental Electromagnetic force density equation has been based integral on Newton's second law of motion and has been divided into 5 separate terms (B-1 until B-5), each one describing a part of the electromagnetic and inertia force densities.

$$\sum_{i=0}^{i=5} B_i = 0 \quad (3)$$

The first term B-1 represents the inertia of the mass density of light (Electromagnetic Radiation). The terms B-2 and B-3 represent the electric force densities within the Electromagnetic Radiation (Beam of Light) and the terms B-4 and B-5 represent the magnetic force densities within the Electromagnetic Radiation (Beam of Light).

Fundamental in the “Quantum Light Theory” is the outcome of (3) which always has to be zero according Newton’s fundamental principle of “Universal Equilibrium”.

To apply the concept of “Universal Equilibrium” within an electromagnetic field, the electric forces F_{Electric} , the magnetic forces F_{Magnetic} and the inertia forces will be presented separately in equation (3):

$$\sum_{i=0, j=0}^{i=n, j=m} \left(\overline{F_{\text{Electric}-i}} + \overline{F_{\text{Magnetic}-j}} - m \bar{a} \right) = 0 \quad (4)$$

1.2 The Inertia of Light (Term B-1)

Reducing Equation (2) to one single Force $\bar{F}$, equation (2) will be written in the well-known presentation:

$$\bar{F} = m \bar{a} \quad (5)$$

The right and the left term of Newton’s law of motion in equation (5) has to be divided by the Volume “V” to find an

equation for the force density $\bar{f}$ related to the mass density “ ρ ”.

$$\begin{aligned}\bar{\mathbf{F}} &= m \bar{\mathbf{a}} \\ \left(\frac{\bar{\mathbf{F}}}{V} \right) &= \left(\frac{m}{V} \right) \bar{\mathbf{a}} \\ \bar{\mathbf{f}} &= \rho \bar{\mathbf{a}}\end{aligned}\tag{6}$$

The Inertia Force $\overline{F_{\text{Inertia}}}$ for Electromagnetic Radiation will be derived from Newton’s second law of motion, using the relationship between the momentum vector $\bar{\mathbf{p}}$ for radiation expressed by the Poynting vector $\bar{\mathbf{S}}$:

$$\overline{F_{\text{INERTIA}}} = -m \bar{\mathbf{a}} = -m \frac{\Delta \bar{\mathbf{v}}}{\Delta t} = -\frac{\Delta(m\bar{\mathbf{v}})}{\Delta t} = -\frac{\Delta \bar{\mathbf{p}}}{\Delta t} = -\left(\frac{V}{c^2}\right) \frac{\Delta \bar{\mathbf{S}}}{\Delta t} \tag{7}$$

Dividing the right and the left term in equation (7) by the volume V results in the inertia force density $\overline{f_{\text{Inertia}}}$:

$$\begin{aligned}\overline{F_{\text{INERTIA}}} &= -m \bar{\mathbf{a}} = -m \frac{\Delta \bar{\mathbf{v}}}{\Delta t} = -\frac{\Delta(m\bar{\mathbf{v}})}{\Delta t} = -\frac{\Delta \bar{\mathbf{p}}}{\Delta t} = -\left(\frac{V}{c^2}\right) \frac{\Delta \bar{\mathbf{S}}}{\Delta t} \\ \frac{\overline{F_{\text{INERTIA}}}}{V} &= -\frac{m}{V} \bar{\mathbf{a}} = -\frac{m}{V} \frac{\Delta \bar{\mathbf{v}}}{\Delta t} = -\frac{1}{V} \frac{\Delta \bar{\mathbf{p}}}{\Delta t} = -\left(\frac{1}{c^2}\right) \frac{\Delta \bar{\mathbf{S}}}{\Delta t} \\ \overline{f_{\text{INERTIA}}} &= -\rho \bar{\mathbf{a}} = -\left(\frac{1}{c^2}\right) \frac{\Delta \bar{\mathbf{S}}}{\Delta t} \quad [\text{N/m}^3]\end{aligned}\tag{8}$$

The Poynting vector $\bar{\mathbf{S}}$ represents the total energy transport of the electromagnetic radiation per unit surface per unit time [$\text{J} / \text{m}^2 \text{ s}$]. Which can be written as the cross product of the Electric Field intensity $\bar{\mathbf{E}}$ and the magnetic Field intensity $\bar{\mathbf{H}}$.

$$\begin{aligned}\overline{f_{INERTIA}} &= -\rho a = -\left(\frac{1}{c^2}\right)\frac{\Delta S}{\Delta t} = -\left(\frac{1}{c^2}\right)\frac{\Delta (\bar{E} \times \bar{H})}{\Delta t} [\text{N/ m}^3] \\ \overline{f_{INERTIA}} &= -\left(\frac{1}{c^2}\right)\frac{\partial (\bar{E} \times \bar{H})}{\partial t} [\text{N/ m}^3]\end{aligned}\tag{9}$$

1.3 Coulomb's Law (Colomb Force) for Electromagnetic GEONs (Term B-2 and B-4)

An example of the Coulomb Force is the Electric Force F_{Coulomb} acting on an electric charge Q placed in an electric field E . The equation for the Coulomb Force equals:

$$\overline{F_{\text{Coulomb}}} = \bar{E} Q \quad [\text{N}]\tag{10}$$

Dividing the right and the left term in equation (10) by the volume V results in the Electric force density $\overline{f_{\text{Coulomb}}}$:

$$\begin{aligned}\bar{F}_{\text{COULOMB}} &= \bar{E} Q \quad [\text{N}] \\ \frac{\bar{F}_{\text{COULOMB}}}{V} &= \bar{E} \frac{Q}{V} \quad [\text{N/ m}^3] \\ \bar{f}_{\text{COULOMB}} &= \bar{E} \rho_E \quad [\text{N/ m}^3]\end{aligned}\tag{11}$$

Substituting [Gauss's law in differential form](#) in (11) results in Coulombs Law for Electromagnetic Radiation for the Electric force density $\overline{f_{\text{Coulomb}}}$:

$$\begin{aligned}
\bar{\mathbf{f}}_{\text{COULOMB}} &= \bar{\mathbf{E}} \rho_E \\
\bar{\mathbf{f}}_{\text{COULOMB}} &= \bar{\mathbf{E}} \rho_E = \bar{\mathbf{E}} (\nabla \cdot \bar{\mathbf{D}}) \\
\bar{\mathbf{f}}_{\text{COULOMB}} &= \bar{\mathbf{E}} (\nabla \cdot \bar{\mathbf{D}}) = \varepsilon \bar{\mathbf{E}} (\nabla \cdot \bar{\mathbf{E}}) \left[\text{N/ m}^3 \right]
\end{aligned} \tag{12}$$

In Electromagnetic Field Configurations, there is in general no preference for the electric force densities or the magnetic force densities. In general the equations for the electric field densities are universally exchangeable with the magnetic field densities.

For the magnetic field densities, equation (12) can be written as:

$$\begin{aligned}
\bar{\mathbf{f}}_{\text{Coulomb - Electric}} &= \bar{\mathbf{E}} (\nabla \cdot \bar{\mathbf{D}}) = \varepsilon \bar{\mathbf{E}} (\nabla \cdot \bar{\mathbf{E}}) \left[\text{N/ m}^3 \right] \text{ (Term B-2)} \\
\bar{\mathbf{f}}_{\text{Coulomb - Magnetic}} &= \bar{\mathbf{H}} (\nabla \cdot \bar{\mathbf{B}}) = \mu \bar{\mathbf{H}} (\nabla \cdot \bar{\mathbf{H}}) \left[\text{N/ m}^3 \right] \text{ (Term B-4)}
\end{aligned} \tag{13}$$

1.4 Lorentz's Law (Lorentz Force) for Electromagnetic GEONs (Term B-3 and B-5)

An example of the Lorentz Force is the Magnetic Force $\mathbf{F}_{\text{Lorentz}}$ acting on an electric charge Q moving with a velocity $\mathbf{v}$ within a magnetic field with magnetic field intensity $\mathbf{B}$ (magnetic induction).

Fig. 1. The Lorentz Force equals the cross product of the Magnetic Induction $\vec{B}$ and the velocity $\vec{v}$ of the charge q moving within the magnetic field times the value of the electric charge

The equation for the Lorentz Force equals:

$$\vec{F}_{\text{LORENTZ}} = Q \vec{v} \times \vec{B} \quad [\text{N}] \quad (14)$$

Dividing the right and the left term in equation (14) by the volume V results in the Lorentz force density $\vec{f}_{\text{Lorentz}}$

$$\begin{aligned} \vec{F}_{\text{LORENTZ}} &= Q \vec{v} \times \vec{B} \quad [\text{N}] \\ \frac{\vec{F}_{\text{LORENTZ}}}{V} &= - \vec{B} \times \frac{Q \vec{v}}{V} \quad [\text{N}/\text{m}^3] \\ \vec{f}_{\text{LORENTZ}} &= - \vec{B} \times \frac{Q \vec{v}}{V} = - \vec{B} \times \vec{j} = - \mu \vec{H} \times \vec{j} \quad [\text{N}/\text{m}^3] \end{aligned} \quad (15)$$

In which q is the electric charge, v the velocity of the electric charge, B the magnetic induction and j the electric current density. Substituting Ampère's law in differential form in

(15) results in Lorentz's Law for Electromagnetic Radiation
for the Electric force density $\overline{f}_{\text{Lorentz}}$:

$$\begin{aligned}\overline{f}_{\text{LORENTZ}} &= -\mu \overline{H} \times (\dot{\overline{j}}) \\ \overline{f}_{\text{LORENTZ}} &= -\mu \overline{H} \times (\dot{\overline{j}}) = -\mu \overline{H} \times (\nabla \times \overline{H}) \left[\text{N/ m}^3 \right] \quad (16)\end{aligned}$$

In Electromagnetic Field Configurations, there is in general no preference for the electric force densities or the magnetic force densities. In general the equations for the electric field densities are universally exchangeable with the magnetic field densities. For the electric field densities, equation (16) can be written as:

$$\begin{aligned}\overline{f}_{\text{Coulomb - Electric}} &= -\epsilon \overline{E} \times (\nabla \times \overline{E}) \left[\text{N/ m}^3 \right] \quad (\text{Term B-3}) \\ \overline{f}_{\text{Coulomb - Magnetic}} &= -\mu \overline{H} \times (\nabla \times \overline{H}) \left[\text{N/ m}^3 \right] \quad (\text{Term B-5})\end{aligned} \quad (17)$$

1.5 The Universal Equation for the Electromagnetic field (Term B-1 + Term B-2 + Term B-3 + Term B-4 + Term B-5)

Newton's second law of motion applied within any arbitrary electromagnetic field configuration results in the fundamental equation (23) for any arbitrary electromagnetic field configuration (a beam of light):

$$\begin{aligned}
 &\text{NEWTON: } \mathbf{F}_{\text{TOTAAL}} = m \mathbf{a} \text{ represents: } \mathbf{f}_{\text{TOTAAL}} = \rho \mathbf{a} \\
 &\begin{aligned}
 &\text{B-1} \quad -\rho \mathbf{a} \quad + \quad \mathbf{f}_{\text{TOTAAL}} \quad = 0 \\
 &\text{B-2} \quad -\rho \mathbf{a} \quad + \quad \mathbf{f}_{\text{ELEKTRISCH}} \quad + \quad \mathbf{f}_{\text{MAGNETISCH}} \quad = 0 \quad (18) \\
 &\text{B-3} \quad -\rho \mathbf{a} \quad + \quad \mathbf{F}_{\text{COULOMB}} \quad + \quad \mathbf{F}_{\text{LORENTZ}} \quad + \quad \mathbf{F}_{\text{COULOMB}} \quad + \quad \mathbf{F}_{\text{LORENTZ}} \quad = 0 \\
 &\text{B-4} \quad -\frac{1}{c^2} \frac{\partial (\vec{E} \times \vec{H})}{\partial t} + \epsilon_0 \vec{E}(\nabla \cdot \vec{E}) - \epsilon_0 \vec{E} \times (\nabla \times \vec{E}) + \mu_0 \vec{H}(\nabla \cdot \vec{H}) - \mu_0 \vec{H} \times (\nabla \times \vec{H}) = 0 \\
 &\text{B-5}
 \end{aligned}
 \end{aligned}$$

Term B-4 is the magnetic equivalent of the (electric) Coulomb's law B-2 and Term B-3 is the electric equivalent of the (magnetic) Lorentz's law B-5.

The universal equation for the electromagnetic field (free electromagnetic waves and confined electromagnetic fields) has been presented in (24) and expresses the perfect equilibrium between the inertia forces (B-1), the electric forces (B-2 and B-3) and the magnetic forces (B-4 and B-5) in any arbitrary electromagnetic field configuration.

$$\begin{aligned}
 &\text{B-1} \quad -\frac{1}{c^2} \frac{\partial (\vec{E} \times \vec{H})}{\partial t} + \epsilon_0 \vec{E}(\nabla \cdot \vec{E}) - \epsilon_0 \vec{E} \times (\nabla \times \vec{E}) + \mu_0 \vec{H}(\nabla \cdot \vec{H}) - \mu_0 \vec{H} \times (\nabla \times \vec{H}) = 0 \quad (19) \\
 &\text{B-2} \quad \text{B-3} \quad \text{B-4} \quad \text{B-5}
 \end{aligned}$$

Comparing the 4 Maxwell Equations (26) with the Universal Equation (24) we conclude that the 4 Maxwell equations show only the 4 parts of the Universal Dynamic Equilibrium in 4 separate terms and the 4 Maxwell equations are missing the fundamental term for inertia. For that reason it is impossible to calculate the interaction between light and gravity with the 4 Maxwell equations. To find the interaction terms between light and gravity the inertia term (B-1 in 24) is necessary.

2 The Fundamental Correction in Bohr's Theory of "Quantum Physics"

The physical concept of quantum mechanical probability waves has been created during the famous [1927 5th Solvay Conference](#). During that period there were several circumstances which came just together and made it possible to create a unique idea of "**Material Waves**" (Solutions of Schödinger's wave equation) being complex (partly real and partly imaginary) and describing the probability of the appearance of a physical object (elementary particle) generally indicated as "**Quantum Mechanical Probability Waves**".

2.1 Newton's approach to the Fundamental Concept of Probability based on Newtonian Physics.

Newton's second law can be interpreted as the law of "[Conservation of Energy](#)". For an Electromagnetic Field the law of conservation of Energy has been expressed as:

$$\nabla \cdot \vec{S} + \frac{\partial W}{\partial t} = 0 \quad (23)$$

From the equation for the "Conservation of Electromagnetic Energy" the Relativistic Quantum Mechanical "Dirac" equation will be derived which can be considered to be the relativistic version of the Quantum Mechanical Schrodinger wave equation.

2.2 The fundamental concept of Probability

The idea of complex (probability) waves is directly related to the concept of confined ([standing](#)) waves. Characteristic for any [standing](#) wave is the fact that the velocity and the pressure (electric field and magnetic field) are always shifted

over 90 degrees. The same principle does exist for the [standing \(confined\) electromagnetic waves](#),

For that reason every confined (standing) Electromagnetic wave can be described by a complex sum vector $\bar{\phi}$ of the Electric Field Vector $\bar{E}$ and the Magnetic Field Vector $\bar{B}$ ($\bar{E}$ has 90 degrees phase shift compared to $\bar{B}$).

The vector functions $\bar{\phi}$ and the complex conjugated vector function $\bar{\phi}^*$ will be written as:

$$\bar{\phi} = \frac{1}{\sqrt{2} \mu} \left(\bar{B} + i \frac{\bar{E}}{c} \right) \quad (24)$$

$\bar{B}$ equals the magnetic induction, $\bar{E}$ the electric field intensity ($\bar{E}$ has + 90 degrees phase shift compared to $\bar{B}$) and c the speed of light.

The complex conjugated vector function equals:

$$\bar{\phi}^* = \frac{1}{\sqrt{2} \mu} \left(\bar{B} - i \frac{\bar{E}}{c} \right) \quad (25)$$

The dot product equals the electromagnetic energy density w :

$$\bar{\phi} \cdot \bar{\phi}^* = \frac{1}{2 \mu} \left(\bar{B} + i \frac{\bar{E}}{c} \right) \cdot \left(\bar{B} - i \frac{\bar{E}}{c} \right) = \frac{1}{2} \mu H^2 + \frac{1}{2} \varepsilon E^2 = w \quad (26)$$

Using Einstein's equation $W = m c^2$, the dot product equals the electromagnetic mass density w

$$\bar{\phi} \cdot \bar{\phi}^* \frac{1}{c^2} = \frac{\varepsilon}{2} \left(\bar{\mathbf{B}} + i \frac{\bar{\mathbf{E}}}{c} \right) \cdot \left(\bar{\mathbf{B}} - i \frac{\bar{\mathbf{E}}}{c} \right) = \frac{1}{2} \varepsilon \mu^2 H^2 + \frac{1}{2} \varepsilon^2 E^2 = \rho \text{ [kg/m}^3\text{]} \quad (27)$$

The cross product is proportional to the Poynting vector
([Ref. 3, page 202, equation 15](#)).

$$\bar{\phi} \times \bar{\phi}^* = \frac{1}{2\mu} \left(\bar{\mathbf{B}} + i \frac{\bar{\mathbf{E}}}{c} \right) \times \left(\bar{\mathbf{B}} - i \frac{\bar{\mathbf{E}}}{c} \right) = i \sqrt{\varepsilon \mu} \bar{\mathbf{E}} \times \bar{\mathbf{H}} = i \sqrt{\varepsilon \mu} \bar{\mathbf{S}} \quad (28)$$

Newton's second law of motion has been described in 3 spatial dimensions, resulting in the fundamental equation for the electromagnetic field.

$$\begin{array}{c} \text{3-Dimensional Space Domain} \\ \text{B-1} \quad \text{B-2} \quad \text{B-3} \\ \left(\begin{array}{c} x_3 \\ x_2 \\ x_1 \end{array} \right) \cdot \frac{1}{c^2} \frac{\partial (\bar{\mathbf{E}} \times \bar{\mathbf{H}})}{\partial t} + \varepsilon_0 \bar{\mathbf{E}} (\nabla \cdot \bar{\mathbf{E}}) - \varepsilon_0 \bar{\mathbf{E}} \times (\nabla \times \bar{\mathbf{E}}) + \\ \text{B-4} \quad \text{B-5} \quad \text{B-6} \\ + \mu_0 \bar{\mathbf{H}} (\nabla \cdot \bar{\mathbf{H}}) - \mu_0 \bar{\mathbf{H}} \times (\nabla \times \bar{\mathbf{H}}) + \frac{1}{2} \left(\varepsilon^2 \mu (\bar{\mathbf{E}} \cdot \bar{\mathbf{E}}) + \varepsilon \mu^2 (\bar{\mathbf{H}} \cdot \bar{\mathbf{H}}) \right) \bar{\mathbf{g}} = \bar{0} \end{array} \quad (29)$$

The formal mathematical way to describe the force density results from the 4-dimensional divergence of the 4-dimensional energy momentum tensor, resulting in a 4-dimensional Force vector. Dividing the 4-dimensional Force vector by the Volume results in the 4-dimensional force density vector.

The 4-dimensional Electromagnetic Vector Potential has been defined by:

$$\overset{-4}{\varphi} = \begin{pmatrix} \varphi_4 \\ \varphi_3 \\ \varphi_2 \\ \varphi_1 \end{pmatrix} \xrightarrow{\text{CartesianCoordinateSystem}} \begin{pmatrix} \varphi_t \\ \varphi_z \\ \varphi_y \\ \varphi_x \end{pmatrix} \quad (30)$$

In which the term φ_a represents the 4-dimensional electromagnetic vector potential in the “a” direction while the indice “a” varies from 1 to 4. In a cartesian coordinate system the indices are chosen varying from the x,y,z and t direction. In which the indice “t” represents the time direction which has been considered to be the 4th dimension. The 4-dimensional Electromagnetic “[Maxwell Tensor](#)” has been defined by:

$$F_{ab} = \partial_b \varphi_a - \partial_a \varphi_b \quad (31)$$

Where the indices “a” and “b” vary from 1 to 4.

The 4-dimensional Electromagnetic “[Energy Momentum Tensor](#)” has been defined by:

$$T^{ab} = \frac{I}{\mu_0} \left[F_{ac} F^{cb} + \frac{I}{4} \delta_{ab} F_{cd} F^{cd} \right] \quad (32)$$

The 4-dimensional divergence of the 4-dimensional Energy Momentum Tensor equals the 4-dimensional Force Density

4-vector f^a :

$$f^a = \partial_b T^{ab} \quad (33)$$

Substituting the electromagnetic values for the electric field intensity “E” and the magnetic field intensity “H” in (71) results in the 4-dimensional representation of Newton’s second law of motion:

$$\begin{aligned}
 & \text{Energy-Time Domain} \\
 & \text{B-7} \\
 (f_4) \quad & \nabla \cdot (\bar{E} \times \bar{H}) + \frac{1}{2} \frac{\partial \left(\epsilon_0 (\bar{E} \cdot \bar{E}) + \mu_0 (\bar{H} \cdot \bar{H}) \right)}{\partial t} = 0 \\
 & \text{3-Dimensional Space Domain} \\
 & \text{B-1} \qquad \text{B-2} \qquad \text{B-3} \\
 & \left(\begin{array}{c} f_3 \\ f_2 \\ f_1 \end{array} \right) - \frac{1}{c^2} \frac{\partial (\bar{E} \times \bar{H})}{\partial t} + \epsilon_0 \bar{E} (\nabla \cdot \bar{E}) - \epsilon_0 \bar{E} \times (\nabla \times \bar{E}) + \\
 & \qquad \text{B-4} \qquad \text{B-5} \\
 & \qquad \qquad + \mu_0 \bar{H} (\nabla \cdot \bar{H}) - \mu_0 \bar{H} \times (\nabla \times \bar{H}) = \bar{0}
 \end{aligned} \quad (34)$$

In which f_1 , f_2 , f_3 , represent the force densities in the 3 spatial dimensions and f_4 represent the force density (energy flow) in the time dimension (4th dimension). Equation (42) can be written as:

The 4th term in equation (42) can be written in the terms of the Poynting vector “S” and the energy density “w” representing the electromagnetic law for the conservation of energy (Newton’s second law of motion).

Energy-Time Domain
 Inner Energy
 B-7

$$\left(\begin{matrix} f_4 \end{matrix} \right) \qquad \qquad \qquad \nabla \cdot \bar{S} + \frac{\partial w}{\partial t} = 0 \qquad (35.1)$$

3-Dimensional Space Domain
 B-1 B-2 B-3

(35)

$$\left(\begin{matrix} f_3 \\ f_2 \\ f_1 \end{matrix} \right) \qquad \qquad \qquad - \frac{1}{c^2} \frac{\partial (\bar{E} \times \bar{H})}{\partial t} + \varepsilon_0 \bar{E} (\nabla \cdot \bar{E}) - \varepsilon_0 \bar{E} \times (\nabla \times \bar{E}) +$$

B-4 B-5

$$+ \mu_0 \bar{H} (\nabla \cdot \bar{H}) - \mu_0 \bar{H} \times (\nabla \times \bar{H}) = \bar{0} \qquad (35.2)$$

2.3 The 4-Dimensional Relativistic Quantum Mechanical Dirac Equation

Substituting (27) and (28) in Equation (35.1) results in The 4-Dimensional Equilibrium Equation (36):

$$(x_4) - \frac{i}{\sqrt{\epsilon_0 \mu_0}} \nabla \cdot (\bar{\phi} \times \bar{\phi}) = - \frac{\partial \bar{\phi} \cdot \bar{\phi}^*}{\partial t} \quad (36.1)$$

$$\begin{pmatrix} x_3 \\ x_2 \\ x_1 \end{pmatrix} - \frac{1}{c^2} \frac{\partial (\bar{\mathbf{E}} \times \bar{\mathbf{H}})}{\partial t} + \epsilon_0 \bar{\mathbf{E}} (\nabla \cdot \bar{\mathbf{E}}) - \epsilon_0 \bar{\mathbf{E}} \times (\nabla \times \bar{\mathbf{E}}) + \quad (36)$$

$$+ \mu_0 \bar{\mathbf{H}} (\nabla \cdot \bar{\mathbf{H}}) - \mu_0 \bar{\mathbf{H}} \times (\nabla \times \bar{\mathbf{H}}) = \bar{0} \quad (36.2)$$

To transform the electromagnetic vector wave function $\bar{\phi}$ into a scalar (spinor or one-dimensional matrix representation), the Pauli spin matrices σ and the following matrices ([Ref. 3 page 213, equation 99](#)) are introduced:

$$\bar{\alpha} = \begin{bmatrix} 0 & \sigma \\ \sigma & 0 \end{bmatrix} \quad \text{and} \quad \bar{\beta} = \begin{bmatrix} \delta_{ab} & 0 \\ 0 & -\delta_{ab} \end{bmatrix} \quad (37)$$

Then equation (44) can be written as the 4-Dimensional Hyperspace Equilibrium Dirac Equation:

$$(x_4) \left(\frac{i m c}{h} \bar{\beta} + \bar{\alpha} \cdot \nabla \right) \psi = - \frac{1}{c} \frac{\partial \psi}{\partial t} \quad (38.1)$$

$$\begin{pmatrix} x_3 \\ x_2 \\ x_1 \end{pmatrix} - \frac{1}{c^2} \frac{\partial (\bar{\mathbf{E}} \times \bar{\mathbf{H}})}{\partial t} + \epsilon_0 \bar{\mathbf{E}} (\nabla \cdot \bar{\mathbf{E}}) - \epsilon_0 \bar{\mathbf{E}} \times (\nabla \times \bar{\mathbf{E}}) + \quad (38) \\ + \mu_0 \bar{\mathbf{H}} (\nabla \cdot \bar{\mathbf{H}}) - \mu_0 \bar{\mathbf{H}} \times (\nabla \times \bar{\mathbf{H}}) = 0 \quad (38.2)$$

The fourth term (x_4) equals the [relativistic Dirac equation](#) (38.1) which equals equation (102) page 213 in [Ref.3](#).

Equation (38.1) represents the relativistic quantum mechanical Dirac Equation where ψ represents the quantum mechanical probability wave function. The mathematical evidence for the equivalent for (38.1) has been published in 1995 in the article: [“A Continuous Model of Matter based on AEONs”](#). Equation (1) page 201 to Equation (102) page 213. (Doi: [10.31219/osf.io/ra7ng](https://doi.org/10.31219/osf.io/ra7ng))

The Electromagnetic Law for the conservation of Energy (35.1) and the Relativistic Dirac Equation (38.1) are **identical** but written in a different form.

The law of conservation of Electromagnetic Energy can be written in an electromagnetic form (39.1) or in an identical way in a quantum mechanical form (39.2):

Energy-Time Domain

Inner Energy

B-7

$$\left(f_4 \right) \quad \nabla \cdot (\bar{\phi} \times \bar{\phi}) = - \frac{i}{c} \frac{\partial \bar{\phi} \cdot \bar{\phi}^*}{\partial t} \quad (39.1)$$

$$\left(x_4 \right) \quad \left(\frac{i m c}{h} \bar{\beta} + \bar{\alpha} \cdot \nabla \right) \psi = - \frac{1}{c} \frac{\partial \psi}{\partial t} \quad (39.2)$$

The weakness in the Quantum Mechanical Relativistic [Dirac Equation](#) (39.2) is that the Dirac Equation is a 1-dimensional equation which will never be able to describe the 4-dimensional real physical world. While 39.1 represents a Electromagnetic Vector Equation.

From the equations (27) and (28) follows the 4-Dimensional Vector-Dirac equation (40). This equation is a 4-dimensional vector equation and is coherent with the 4-dimensional physical reality.

$$\left(x_4 \right) \quad \nabla \cdot (\bar{\phi} \times \bar{\phi}) = - \frac{i}{c} \frac{\partial \bar{\phi} \cdot \bar{\phi}^*}{\partial t}$$

$$\left(\begin{matrix} x_3 \\ x_2 \\ x_1 \end{matrix} \right) \quad \frac{i}{c} \frac{\partial (\bar{\phi} \times \bar{\phi}^*)}{\partial t} - \left(\bar{\phi} \times (\nabla \times \bar{\phi}^*) + \bar{\phi}^* \times (\nabla \times \bar{\phi}) \right) + \left(\bar{\phi} (\nabla \cdot \bar{\phi}^*) + \bar{\phi}^* (\nabla \cdot \bar{\phi}) \right) = 0 \quad (40)$$

In which the Quantum Mechanical Complex Probability Vector Function $\bar{\phi}$ and the complex conjugated vector function $\bar{\phi}^*$ equals:

$$\begin{aligned}\bar{\phi} &= \bar{B} + \frac{i}{c} \bar{E} = \mu \bar{H} + \frac{i}{c} \bar{E} \\ \bar{\phi}^* &= \bar{B} - \frac{i}{c} \bar{E} = \mu \bar{H} - \frac{i}{c} \bar{E}\end{aligned}\quad (41)$$

The 4-Dimensional [Dirac equation](#) represents the “Newtonian Perfect Equilibrium” in the 4-Dimensional Space-Time Continuum en has been represented by 4 separate equations. The first one represents the well-known relativistic quantum mechanical Dirac Equation in the Time-Energy domain x_4 . The 3 quantum mechanical equations in the space-momentum domain represents the “Newtonian Perfect Equilibrium” for the force densities in the domains (x_1, x_2, x_3)

$$\begin{aligned}(x_4) \quad \nabla \cdot (\bar{\phi} \times \bar{\phi}) &= -\frac{i}{c} \frac{\partial \bar{\phi} \cdot \bar{\phi}^*}{\partial t} \\ \left(\begin{matrix} x_3 \\ x_2 \\ x_1 \end{matrix} \right) \frac{i}{c} \frac{\partial (\bar{\phi} \times \bar{\phi}^*)}{\partial t} &- \left(\bar{\phi} \times (\nabla \times \bar{\phi}^*) + \bar{\phi}^* \times (\nabla \times \bar{\phi}) \right) + \left(\bar{\phi} (\nabla \cdot \bar{\phi}^*) + \bar{\phi}^* (\nabla \cdot \bar{\phi}) \right) = 0\end{aligned}\quad (42)$$

Newton
Lorentz
Coulomb
Newtonian Perfect Equilibrium

$$\frac{1}{c^2} \bar{\phi} \cdot \bar{\phi}^* = \rho \text{ [kg/m}^3\text{]}$$

These results lead to the conclusion that the results of the experiments, published in 2021 “[Operational Resource Theory of Imaginarity](#)” in “[Physical Review Letters](#)” present strong evidence for the existence at sub-atomic level of the **electromagnetic GEONs** and the correctness of Wheeler’s theory (Equation (50) and (51)).

To define the Fundamental Equation for the Interaction between Gravity and Light, an extra term (B-6) has been introduced in equation (29). The term B-6 represents the force density of the gravitational field acting on the electromagnetic mass density.

$$F_{\text{GRAVITY}} = m \bar{g} \text{ [N]}$$

Dividing both terms by the Volume V:

$$\frac{F_{\text{GRAVITY}}}{V} = \frac{m}{V} \bar{g} \text{ [N/ m}^3\text{]} \quad (43)$$

Results in the force density:

$$f_{\text{GRAVITY}} = \rho \bar{g} \text{ [N/ m}^3\text{]}$$

The specific mass “ ρ ” of a beam of light follows from Einstein’s equation:

$$W = m c^2$$

Dividing both terms by the Volume V results in:

$$\frac{W}{V} = \frac{m}{V} c^2 \quad (44)$$

which represents the energy density “w” and the specific mass “ ρ ” of the electromagnetic radiation:

$$w = \rho c^2$$

which results for an expression of the specific mass ρ :

$$\rho = \frac{1}{c^2} w = \varepsilon \mu w$$

The energy density “w” follows from the electric and the magnetic field intensities:

$$w = \frac{1}{2} \epsilon E^2 + \frac{1}{2} \mu H^2$$

$$w = \frac{1}{2} (\epsilon E^2 + \mu H^2) = \frac{1}{2} (\epsilon (\vec{E} \cdot \vec{E}) + \mu (\vec{H} \cdot \vec{H})) \quad (45)$$

Substituting equation (45) in equation (29) results in the gravitational force density f_{GRAVITY} acting on an arbitrary electromagnetic field configuration (a beam of light) with mass density ρ .

$$f_{\text{GRAVITY}} = \rho \vec{g}$$

$$f_{\text{GRAVITY}} = \rho \vec{g} = \epsilon \mu w \vec{g} = \frac{1}{2} (\epsilon^2 \mu (\vec{E} \cdot \vec{E}) + \epsilon \mu^2 (\vec{H} \cdot \vec{H})) \vec{g} \quad (46)$$

Substituting equation (46) in equation (29) results in the fundamental equation describing the Electromagnetic-Gravitational interaction for any arbitrary electromagnetic field configuration (a beam of light):

$$\begin{aligned} \text{NEWTON: } \vec{F}_{\text{TOTAAL}} &= m \vec{a} \text{ [N]} \\ \text{NEWTON: Expressed in force densities: } \vec{f}_{\text{TOTAAL}} &= \rho \vec{a} \text{ [N/m}^3\text{]} \end{aligned}$$

$$\begin{aligned} -\rho \vec{a} &+ \vec{f}_{\text{TOTAAL}} = \vec{0} \\ -\rho \vec{a} &+ \vec{f}_{\text{ELEKTRISCH}} + \vec{f}_{\text{MAGNETISCH}} + \vec{f}_{\text{GRAVITY}} = \vec{0} \\ \vec{f}_{\text{INERTIA}} + \vec{f}_{\text{COULOMB}} + \vec{f}_{\text{LORENTZ}} + \vec{f}_{\text{COULOMB}} + \vec{f}_{\text{LORENTZ}} + \vec{f}_{\text{GRAVITY}} &= \vec{0} \\ -\frac{1}{c^2} \frac{\partial (\vec{E} \times \vec{H})}{\partial t} + \epsilon_0 \vec{E} (\nabla \cdot \vec{E}) - \epsilon_0 \vec{E} \times (\nabla \times \vec{E}) + \mu_0 \vec{H} (\nabla \cdot \vec{H}) - \mu_0 \vec{H} \times (\nabla \times \vec{H}) + \frac{1}{2} (\epsilon^2 \mu (\vec{E} \cdot \vec{E}) + \epsilon \mu^2 (\vec{H} \cdot \vec{H})) \vec{g} &= \vec{0} \end{aligned} \quad (47)$$

B-1
B-2
B-3
B-4
B-5
B-6

Term B-1 represents the inertia term of the electromagnetic radiation. Term B-4 is the magnetic representation of the (electric) Coulomb's Force B-2 and Term B-3 is the electric representation of the (magnetic) Lorentz Force B-5. Term B-6 represents the Electromagnetic-Gravitational interaction of a gravitational field with field acceleration $\vec{g}$ acting on an

arbitrary electromagnetic field configuration (a beam of light) with specific mass ρ .

The universal equation for the electromagnetic field (free electromagnetic waves and confined electromagnetic fields) within a gravitational field with gravity field intensity $\bar{g}$ has been presented in (48) and expresses the perfect equilibrium between the inertia forces (B-1), the electric forces (B-2 and B-3), the magnetic forces (B-4 and B-5) and the gravitational force (B-6) in any arbitrary electromagnetic field configuration.

$$\begin{aligned}
 & - \underbrace{\frac{1}{c^2} \frac{\partial(\bar{\mathbf{E}} \times \bar{\mathbf{H}})}{\partial t}}_{\text{B-1}} + \underbrace{\epsilon_0 \bar{\mathbf{E}} (\nabla \cdot \bar{\mathbf{E}})}_{\text{B-2}} - \underbrace{\epsilon_0 \bar{\mathbf{E}} \times (\nabla \times \bar{\mathbf{E}})}_{\text{B-3}} + \underbrace{\mu_0 \bar{\mathbf{H}} (\nabla \cdot \bar{\mathbf{H}})}_{\text{B-4}} - \\
 & - \underbrace{\mu_0 \bar{\mathbf{H}} \times (\nabla \times \bar{\mathbf{H}})}_{\text{B-5}} + \underbrace{\frac{1}{2} \left(\epsilon^2 \mu (\bar{\mathbf{E}} \cdot \bar{\mathbf{E}}) + \epsilon \mu^2 (\bar{\mathbf{H}} \cdot \bar{\mathbf{H}}) \right)}_{\text{B-6}} \bar{\mathbf{g}} = \bar{\mathbf{0}}
 \end{aligned} \tag{48}$$

2.4 The Gravitational-Electromagnetic Confinement of GEONs.

The physicist “John Archibald Wheeler”, and well-known friend of Albert Einstein, published his theory about **Gravitational Electromagnetic Entities** (GEONs) in 1955 in *Physical Review Journals*: “GEONs” (Ref. 1). John Archibald Wheeler was the first one in physics who understood that:

$$\begin{aligned} \textit{Light} &\triangleq \textit{Electromagnetic Radiation} \triangleq \textit{Energy} \triangleq \\ &\triangleq \textit{Mass} \left(E = m c^2 \right) \triangleq \textit{Gravity} \triangleq \textit{Gravitational Field} \end{aligned}$$

Wheeler’s conclusion was that every beam of light creates simultaneously a gravitational field, besides the original electromagnetic field, proportional to the electromagnetic energy of the beam of light.

Like a Black Hole can capture a beam of light, it is possible that a beam of light confines itself due to its own gravitational field forming a **Gravitational Electromagnetic Entity** (GEON). The final results of Wheeler’s research were not what he expected. He found only GEONs by toroidal “Gravitational-Electromagnetic Confinement” with the dimensions of a star constellation and a stable lifetime of a few milliseconds.

“Quantum Light Theory” presents a new “Gravitational-Electromagnetic Equation” (Ref. [7], [8] and [9]) describing Electromagnetic Field Configurations which are simultaneously the Mathematical Solutions for the Quantum Mechanical “Schrodinger Wave Equation” and more exactly the Mathematical Solutions for the “Relativistic Quantum Mechanical Dirac Equation”. The Mathematical Solutions for

the “Gravitational-Electromagnetic Equation” carry Mass, Electric Charge and Magnetic Spin at discrete values.

When a beam of light is approaching a strong gravitational field in the direction of the gravitational field, generated by a Black Hole, the confinement has been called a Longitudinal Black Hole. The direction of propagation of the beam of light is in the same direction (or in the opposite direction) of the gravitational field. According the first term in (33), the beam of light will be accelerated or decelerated. However, the speed of light is a universal constant and for that reason the speed of light cannot increase or decrease. Instead the intensity of the electromagnetic radiation will increase when the beam of light approaches (propagates in the opposite direction as the direction of the gravitational field) the Black Hole. And the intensity of the electromagnetic radiation will decrease when the beam of light leaves (propagates in the same direction as the direction of the gravitational field) the Black Hole.

The Gravitational-Electromagnetic Confinement for the elementary structure beyond the “[superstring](#)” / “[Black Hole](#)” is presented in equation (49).

3-Dimensional Space Domain

$$\begin{pmatrix} x_3 \\ x_2 \\ x_1 \end{pmatrix} - \frac{1}{c^2} \frac{\partial (\vec{E} \times \vec{H})}{\partial t} + \epsilon_0 \vec{E} (\nabla \cdot \vec{E}) - \epsilon_0 \vec{E} \times (\nabla \times \vec{E}) + \mu_0 \vec{H} (\nabla \cdot \vec{H}) - \mu_0 \vec{H} \times (\nabla \times \vec{H}) + \frac{1}{2} \left(\epsilon^2 \mu (\vec{E} \cdot \vec{E}) + \epsilon \mu^2 (\vec{H} \cdot \vec{H}) \right) \vec{g} = \vec{0} \quad (49)$$

In which $\bar{g}$ represents the gravitational acceleration acting on the electromagnetic mass density of the confined electromagnetic radiation.

A possible solution for equation (49) describing an **Gravitational Electromagnetic Confinement (GEON)** within a radial gravitational field with acceleration $\bar{g}$ has been represented in (50).

$$\begin{pmatrix} e_r \\ e_\theta \\ e_\phi \end{pmatrix} = \begin{pmatrix} 0 \\ f(r) \sin(\omega t) \\ -f(r) \cos(\omega t) \end{pmatrix} \quad \begin{pmatrix} m_r \\ m_\theta \\ m_\phi \end{pmatrix} = \begin{pmatrix} 0 \\ f(r) \cos(\omega t) \\ f(r) \sin(\omega t) \end{pmatrix} \quad \bar{g} = \begin{pmatrix} \frac{G_1}{4 \pi r^2} \\ 0 \\ 0 \end{pmatrix} \quad (50)$$

$$w_{em} = \left(\frac{\mu_0}{2} (\bar{m} \cdot \bar{m}) + \frac{\epsilon_0}{2} (\bar{e} \cdot \bar{e}) \right) = \epsilon_0 f(r)^2$$

In which the radial function $f(r)$ equals:

$$f[r] = K e^{-\frac{-\frac{G_1 \epsilon_0 \mu_0}{r} + 8 \pi \log[r]}{8 \pi}} \quad (51)$$

The solution has been calculated according [Newton's Shell Theorem](#).

2.5 GEONs” with an electromagnetic mass: $e_{mm} = 1.6726 \times 10^{-27}$ [kg] and the radius = 3×10^{-58} [m]

For an electromagnetic mass of the confinement: $e_{mm} = 1.6726 \times 10^{-27}$ [kg] (mass of proton), the radius of the confinement equals approximately 3×10^{-58} [m]. This is far beyond the order of [Planck’s Length](#),

The [Plot graph](#) of the Electric Field Intensity $f(r)$ of the confinement has been presented as a function of the radius in figure (2) and figure (3):

Figure 2 PlotGraph of the Electric Field Intensity $f(r)$ [V/ m] for the region $10^{-59} < r < 10^{-55}$ [m] in which the gravitational field acceleration has been chosen accordingly an electromagnetic mass of $1.6\ 726 \times 10^{-27}$ [kg] located at the center of the confinement, according [Newton’s Shell Theorem](#).

$$\text{Plot} \left[e^{-\frac{G1 \varepsilon_0 \mu_0}{r} + 8 \pi \log[r]}, \{r, 10^{-59}, 10^{-57}\} \right]$$

Figure 3 PlotGraph of the Electric Field Intensity $f(r)$ [V/m] for the region $10^{-59} < r < 10^{-57}$ [m] in which the gravitational field acceleration has been chosen accordingly an electromagnetic mass of 1.6726×10^{-27} [kg] located at the center of the confinement, according [Newton's Shell Theorem](#).

The fundamental question is: How it is possible to create confinements from “visible light” (with a wave length between 3.9×10^{-7} [m] until 7×10^{-7} [m]) within dimensions smaller than Planck's Length?

This is only possible when the wave length of the confined radiation is smaller than de dimensions of the confinement. This requires extreme high frequencies. The transformation in frequency from visible light into the extreme high frequency of the confinement is possible because of the Lorentz/ Doppler transformation during the collapse of the radiation when the confinement has been formed (implosion of visible light).

2.6 The Electric Charge and the Magnetic Spin for Electromagnetic GEONs

The following functions for Electromagnetic GEONs with the quantum variables $\{m_1, n_1, p_1, q_1\}$ have been chosen:

$$\begin{aligned}
 f[r] &= K e^{-\frac{G l \varepsilon_0 \mu_0 + 8 \pi \log[r]}{r}} \\
 g_1(\theta, \varphi, t) &= \sin(t \omega) (\sin(\pi \theta m_1) \sin(n_1 2 \pi \varphi) + 1) \\
 h(\theta, \varphi) &= \sin(\pi \theta p_1) \sin(q_1 2 \pi \varphi) + 1 \\
 g_2(\theta, \varphi, t) &= \frac{\sec(t \omega) \sqrt{\cos(2 t \omega) g_1(\theta, \varphi, t)^2 - g_1(\theta, \varphi, t)^2 + 2 h(\theta, \varphi)}}{\sqrt{2}} \\
 f_1[r, \theta, \varphi, t] &= e^{-\frac{G l \varepsilon_0 \mu_0 + 8 \pi \log[r]}{r}} K g_1[\theta, \varphi, t] \\
 f_2[r, \theta, \varphi, t] &= \frac{e^{-\frac{G l \varepsilon_0 \mu_0 + 8 \pi \log[r]}{r}} K \sqrt{-g_1[\theta, \varphi, t]^2 + \cos[2 t \omega] g_1[\theta, \varphi, t]^2 + 2 h[\theta, \varphi]}}{\sqrt{2}}
 \end{aligned} \tag{52}$$

2.7 GEON with quantum numbers: (Electric- and Magnetic Dipoles, Electric- and Magnetic Spin) { $m_1=0, n_1=0, p_1=0, q_1=0$ }

The divergence of the electric field intensity (electric charge density) equals:

$$\begin{aligned} \nabla \cdot \begin{pmatrix} e_r \\ e_\theta \\ e_\varphi \end{pmatrix} &= \frac{\sqrt{2} K1 \cot(\theta) \sin^2(t \omega) \sqrt{1 - \sin^4(t \omega)} e^{\frac{G_1 \varepsilon_0 \mu_0}{8 \pi r}}}{r^2 \sqrt{2 - 2 \sin^4(t \omega)}} \\ \nabla \cdot \begin{pmatrix} e_r \\ e_\theta \\ e_\varphi \end{pmatrix} &= \frac{\frac{1}{2} K1 \cot(\theta) e^{\frac{G_1 \varepsilon_0 \mu_0}{8 \pi r}}}{r^2} \quad (\text{averaged over 1 period of time}) \end{aligned} \quad (53)$$

The divergence of the magnetic field intensity (magnetic monopole) equals:

$$\begin{aligned} \nabla \cdot \begin{pmatrix} m_r \\ m_\theta \\ m_\varphi \end{pmatrix} &= \frac{K1 \sqrt{\varepsilon_0} \cot(\theta) \sqrt{2 - 2 \sin^4(t \omega)} e^{\frac{G_1 \varepsilon_0 \mu_0}{8 \pi r}}}{\sqrt{2} \sqrt{\mu_0} r^2} \\ \nabla \cdot \begin{pmatrix} m_r \\ m_\theta \\ m_\varphi \end{pmatrix} &= \frac{K1 \sqrt{\varepsilon_0} \cot(\theta) \sqrt{\frac{3}{4}} e^{\frac{G_1 \varepsilon_0 \mu_0}{8 \pi r}}}{\sqrt{\mu_0} r^2} \quad (\text{averaged over 1 period of time}) \end{aligned} \quad (54)$$

In which K1 is an arbitrary variable. Because of the $\text{Cot}(\theta)$ function, the electric divergence as well as the magnetic divergence changes from sign when the angle θ varies between 0° until 360° forming electric dipoles (+ versus -) and magnetic dipoles (N versus S).

2.8 GEON with quantum numbers: (Electric- and Magnetic Dipoles, Electric- and Magnetic Spin) {m₁=1, n₁=0, p₁=0, q₁=0}

3.26.2 Type 2 of "Sub Max Planck Length Gravitational-Electromagnetic Confinements" (Electric- and Magnetic Dipoles, Electric- and Magnetic Spin) {m₁=1, n₁=0, p₁=0, q₁=0}

The divergence of the electric field intensity (electric charge density) equals:

$$\nabla \cdot \begin{pmatrix} e_r \\ e_\theta \\ e_\varphi \end{pmatrix} = \frac{\sqrt{2} K1 \cot(\theta) \sin^2(t\omega) \sqrt{1 - \sin^4(t\omega)} e^{\frac{G_1 \varepsilon_0 \mu_0}{8 \pi r}}}{r^2 \sqrt{2 - 2 \sin^4(t\omega)}} \quad (55)$$

$$\nabla \cdot \begin{pmatrix} e_r \\ e_\theta \\ e_\varphi \end{pmatrix} = \frac{\frac{1}{2} K1 \cot(\theta) e^{\frac{G_1 \varepsilon_0 \mu_0}{8 \pi r}}}{r^2} \quad (\text{averaged over 1 period of time})$$

The divergence of the magnetic field intensity (magnetic monopole) equals:

$$\nabla \cdot \begin{pmatrix} m_r \\ m_\theta \\ m_\varphi \end{pmatrix} = \frac{K1 \sqrt{\varepsilon_0} \cot(\theta) \sqrt{2 - 2 \sin^4(t\omega)} e^{\frac{G_1 \varepsilon_0 \mu_0}{8 \pi r}}}{\sqrt{2} \sqrt{\mu_0} r^2} \quad (56)$$

$$\nabla \cdot \begin{pmatrix} m_r \\ m_\theta \\ m_\varphi \end{pmatrix} = \frac{K1 \sqrt{\frac{3}{4}} \sqrt{\varepsilon_0} \cot(\theta) e^{\frac{G_1 \varepsilon_0 \mu_0}{8 \pi r}}}{\sqrt{\mu_0} r^2} \quad (\text{averaged over 1 period of time})$$

In which $K1$ is an arbitrary variable. Because of the $\cot(\theta)$ function, the electric divergence as well as the magnetic divergence changes from sign when the angle θ varies between 0^0 until 360^0 forming electric dipoles (+ versus -) and magnetic dipoles (N versus S).

2.9 GEON with quantum numbers: (Electric- and Magnetic Dipoles, Electric- and Magnetic Spin) $\{m_1=0, n_1=0, p_1=1, q_1=0\}$

The divergence of the electric field intensity (electric charge density) equals:

$$\nabla \cdot \begin{pmatrix} e_r \\ e_\theta \\ e_\varphi \end{pmatrix} = \frac{e \frac{G_1 \varepsilon_0 \mu_0}{8 \pi r} K1 \cot[\theta] \sin[t\omega]^2}{r^2} \quad (57)$$

$$\nabla \cdot \begin{pmatrix} e_r \\ e_\theta \\ e_\varphi \end{pmatrix} = \frac{e \frac{G_1 \varepsilon_0 \mu_0}{8 \pi r} K1 \cot[\theta]}{2 r^2} \text{ (averaged over 1 period of time)}$$

In which $K1$ is an arbitrary variable with a Positive (positive charge) or a Negative (negative charge) value.

Figure 4 Equation (54). Averaged over 1 period of time. Electric Charge Density Plot in a range from 10^{-37} [m] until 10^{-35} [m].

The divergence of the magnetic field intensity (magnetic monopole) equals:

$$\nabla \cdot \begin{pmatrix} m_r \\ m_\theta \\ m_\varphi \end{pmatrix} = \frac{e \frac{G_1 \varepsilon_0 \mu_0}{8 \pi r} K1 \sqrt{\varepsilon_0} \cot[\theta] \sqrt{1 - \sin^2[\theta]}}{r^2 \sqrt{\mu_0}} \quad (58)$$

$$\nabla \cdot \begin{pmatrix} m_r \\ m_\theta \\ m_\varphi \end{pmatrix} = \frac{e \frac{G_1 \varepsilon_0 \mu_0}{8 \pi r} K1 \sqrt{\varepsilon_0} \cot[\theta]}{2 r^2 \sqrt{\mu_0}} \quad (\text{averaged over 1 period of time})$$

In which K1 is an arbitrary variable. Because of the $\cot(\theta)$ function, the electric divergence as well as the magnetic divergence changes from sign when the angle θ varies between 0^0 until 360^0 forming electric dipoles (+ versus -) and magnetic dipoles (N versus S).

2.10 Plank's Law in relation to Newtonian Physics.

To describe the “proportionality between Energy and Frequency (Plank's Law) for confined Electromagnetic Waves, an example has been chosen of an electromagnetic wave (light) confined between two 100 % reflecting mirrors.

Figure 5 Confined Electromagnetic Radiation between two 100 % reflecting mirrors

Figure 2 represents confined electromagnetic radiation with amplitude E_0 and frequency ω .

A general property of confined electromagnetic waves is the proportionality between energy and frequency. As an example we choose the confinement of light between two perfect reflecting mirrors with surface A . When we press both mirrors together of a distance Δx , the work ΔW has been delivered:

$$\Delta W = p A \Delta x \quad (59)$$

In which “ A ” equals the surface of the mirrors and “ p ” equals the [radiation pressure](#):

$$p = w = \frac{1}{2} \epsilon E^2 + \frac{1}{2} \mu H^2 \text{ [N / m}^2\text{]} \quad (60)$$

The Electromagnetic “Work ΔW ” which has been delivered equals:

$$\Delta W = w A \Delta x \quad (61)$$

When over a time “ Δt ” both mirrors move towards each other with a velocity “ v ”, then the distance “ Δx ” passed over a time interval Δt equals:

$$\Delta x = v \Delta t \quad [\text{m}] \quad (62)$$

Substituting (62) in (61) results in:

$$\begin{aligned} \Delta W &= w A \Delta x \\ \Delta W &= w A v \Delta t \\ v &= \frac{\Delta W}{w A \Delta t} \end{aligned} \quad (63)$$

Due to the [Doppler-Shift](#), the frequency of the confined radiation will increase when the mirrors move towards each other and will decrease when both mirrors move apart from each other. When both mirrors move towards each other, the observed frequency shift Δf will be:

$$\Delta f = f_1 - f_0 = f_0 \sqrt{\frac{1 + \frac{v}{c}}{1 - \frac{v}{c}}} - f_0 = f_0 \left(\sqrt{\frac{1 + \frac{v}{c}}{1 - \frac{v}{c}}} - 1 \right) \quad (64)$$

Applying Taylor series, the observed frequency shift equals:

$$\begin{aligned} \Delta f = f_0 \left(\sqrt{\frac{1 + \frac{v}{c}}{1 - \frac{v}{c}}} - 1 \right) &= f_0 \left(1 + \frac{v}{c} + \frac{1}{2} \left(\frac{v}{c} \right)^2 + \frac{1}{2} \left(\frac{v}{c} \right)^3 + \frac{3}{8} \left(\frac{v}{c} \right)^4 + \right) + \\ &+ f_0 \left(\frac{3}{8} \left(\frac{v}{c} \right)^5 + \frac{5}{16} \left(\frac{v}{c} \right)^6 + \frac{5}{16} \left(\frac{v}{c} \right)^7 + \frac{35}{128} \left(\frac{v}{c} \right)^8 + \frac{35}{128} \left(\frac{v}{c} \right)^9 + \frac{63}{256} \left(\frac{v}{c} \right)^{10} + \dots \right) \end{aligned} \quad (65)$$

From

$$\begin{aligned} \Delta f &= f_0 \left(1 + \frac{v}{c} + \frac{1}{2} \left(\frac{v}{c} \right)^2 + \frac{1}{2} \left(\frac{v}{c} \right)^3 + \frac{3}{8} \left(\frac{v}{c} \right)^4 - 1 \right) \\ \Delta f &= f_0 \left(\frac{v}{c} + \frac{1}{2} \left(\frac{v}{c} \right)^2 + \frac{1}{2} \left(\frac{v}{c} \right)^3 + \frac{3}{8} \left(\frac{v}{c} \right)^4 \right) \end{aligned}$$

At low velocities ($v \ll c$)

$$v \approx c \frac{\Delta f}{f_0} \approx \frac{\Delta W}{w A \Delta t} \quad (66)$$

$$\Delta f \approx \left(\frac{f_0}{w A c \Delta t} \right) \Delta W = \left(\frac{f_0}{W} \right) \Delta W$$

$$\Delta W = h_{EM} \Delta f$$

In which “W” equals the total energy involved in the transformation of Mechanical Energy into the Electromagnetic Energy. The term h_{EM} represents an Electromagnetic equivalent for Planck’s constant.

$$\Delta W = h_{EM} \Delta f$$

$$h_{EM} = \frac{f_0}{W} \quad (67)$$

3 The Fundamental Continuing of Einstein's Theory of "General Relativity".

Einstein's two fundamental contributions to Modern Physics are General Relativity and the theory describing "Gravitational Redshift" based on General Relativity.

Einstein assumes a deformation of the space-time continuum because of a gravitational field. But in general a deformation of any medium will be caused by the change of the energy density within the medium. Like the speed of sound will increase/ decrease when we change the air pressure. However, the speed of sound (which became higher or lower) will still be the same in any direction. The change of the speed of sound will be omni-directional.

A gravitational field contains a gravitational energy-density. For that reason the change in the speed of light will be omni-directional within a gravitational field (with a omni-directional gravitational energy density). Einstein however assumes a one-directional change in the speed of light, (only in the direction of the gravitational field). When the change of the speed of light was omni-directional, a beam of light would never be deflected by a gravitational field which is in contradiction with what we measure. Only the absolute value of the speed of light would change omni-directional.

The theory of Newton however results in the theory of a 2-directional inertia of photons. The inertia of photons equals zero only in the direction of propagation. Perpendicular to the direction of propagation the mass density of photons is according Einstein's $E = m c^2$).

The inertia of photons [Ref. 7] in the direction of propagation will not change within a gravitational field. Gravity can only interact with mass (inertia). Because the

mass of the photons in the direction of propagation equals zero, there will be no interaction with the gravitational field and the photon in the direction of propagation. The speed of light in the direction of propagation will remain unaltered. But according to Newton, the photon will have inertia (mass) in the directions perpendicular to the direction of propagation and for that reason the photon will interact with the gravitational field and the photon will be deflected, only in the direction of the gravitational field.

And that leads to the consequence that photons will be deflected within a gravitational field when the direction of the gravitational field is perpendicular to the direction of propagation of the photons.

To find fundamental mathematical evidence for this concept, we have to make use of Quantum Light Theory. Quantum Light Theory (QLT) is the development in Quantum Field Theory (QFT). In Quantum Field Theory, the fundamental interaction fields are replacing the concept of elementary particles in Classical Quantum Mechanics. In Quantum Light Theory the fundamental interaction fields are being replaced by One Single Field. The Electromagnetic Field, generally well known as Light. To realize this theoretical concept, the fundamental theory has to go back in time 300 years, the time of Isaac Newton to follow a different path in development.

Nowadays experiments question more and more the fundamental concepts in Quantum Field Theory and Classical Quantum Mechanics. The publication “[Operational Resource Theory of Imaginarity](#)” in “[Physical Review Letters](#)” in 2021 (Ref. [2]) presenting the first experimental evidence for the measurability of “Quantum Mechanical Imaginarity” directly leads to the fundamental question in this experiment: How is it possible to measure the imaginary part of “Quantum

Physical Probability Waves”? This publication provides an unambiguously answer to this fundamental question in Physics, based on the fundamental “Gravitational Electromagnetic Interaction” force densities. The “Quantum Light Theory” presents a new “Gravitational-Electromagnetic Equation” describing Electromagnetic Field Configurations which are simultaneously the Mathematical Solutions for the Quantum Mechanical “Schrodinger Wave Equation” and more exactly the Mathematical Solutions for the “Relativistic Quantum Mechanical Dirac Equation”. The Mathematical Solutions for the “Gravitational-Electromagnetic Equation” carry Mass, Electric Charge and Magnetic Spin at discrete values.

3.1 Newton’s approach to General Relativity based on Newtonian Physics.

To define the Fundamental Equation for the Interaction between Gravity and Light, an extra term (B-6) has been introduced in equation (24). The term B-6 represents the force density of the gravitational field acting on the electromagnetic mass density.

$$F_{\text{GRAVITY}} = m \bar{g} \text{ [N]}$$

Dividing both terms by the Volume V:

$$\frac{F_{\text{GRAVITY}}}{V} = \frac{m}{V} \bar{g} \text{ [N/ m}^3\text{]} \quad (68)$$

Results in the force density:

$$f_{\text{GRAVITY}} = \rho \bar{g} \text{ [N/ m}^3\text{]}$$

The specific mass “ ρ ” of a beam of light follows from Einstein’s equation:

$$W = m c^2$$

Dividing both terms by the Volume V results in:

$$\frac{W}{V} = \frac{m}{V} c^2$$

which represents the energy density "w" and the specific mass " ρ " of the electromagnetic radiation: (69)

$$w = \rho c^2$$

which results for an expression of the specific mass ρ :

$$\rho = \frac{1}{c^2} w = \varepsilon \mu w$$

The energy density "w" follows from the electric and the magnetic field intensities:

$$w = \frac{1}{2} \varepsilon E^2 + \frac{1}{2} \mu H^2$$

$$w = \frac{1}{2} (\varepsilon E^2 + \mu H^2) = \frac{1}{2} (\varepsilon (\vec{E} \cdot \vec{E}) + \mu (\vec{H} \cdot \vec{H})) \quad (70)$$

Substituting equation (69) and (70) in equation (68) results in the gravitational force density f_{GRAVITY} acting on an arbitrary electromagnetic field configuration (a beam of light) with mass density ρ .

$$f_{\text{GRAVITY}} = \rho \vec{g}$$

$$f_{\text{GRAVITY}} = \rho \vec{g} = \varepsilon \mu w \vec{g} = \frac{1}{2} (\varepsilon^2 \mu (\vec{E} \cdot \vec{E}) + \varepsilon \mu^2 (\vec{H} \cdot \vec{H})) \vec{g} \quad (71)$$

Substituting equation (71) in equation (47) results in the fundamental equation describing the Electromagnetic-Gravitational interaction for any arbitrary electromagnetic field configuration (a beam of light):

$$\begin{aligned}
& \text{NEWTON: } \vec{F}_{\text{TOTAAL}} = m \vec{a} \text{ [N]} \\
& \text{NEWTON: Expressed in force densities: } \vec{f}_{\text{TOTAAL}} = \rho \vec{a} \text{ [N/m}^3\text{]} \\
& \begin{aligned}
& -\rho \vec{a} \quad + \quad \vec{f}_{\text{TOTAAL}} \quad = \vec{0} \quad (72) \\
& -\rho \vec{a} \quad + \quad \vec{f}_{\text{ELEKTRISCH}} \quad + \quad \vec{f}_{\text{MAGNETISCH}} \quad + \quad \vec{f}_{\text{GRAVITY}} \quad = \vec{0} \\
& \vec{f}_{\text{INERTIA}} \quad + \quad \vec{f}_{\text{COULOMB}} \quad + \quad \vec{f}_{\text{LORENTZ}} \quad + \quad \vec{f}_{\text{COULOMB}} \quad + \quad \vec{f}_{\text{LORENTZ}} \quad + \quad \vec{f}_{\text{GRAVITY}} \quad = \vec{0} \\
& -\frac{1}{c^2} \frac{\partial(\vec{E} \times \vec{H})}{\partial t} + \epsilon_0 \vec{E}(\nabla \cdot \vec{E}) - \epsilon_0 \vec{E} \times (\nabla \times \vec{E}) + \mu_0 \vec{H}(\nabla \cdot \vec{H}) - \mu_0 \vec{H} \times (\nabla \times \vec{H}) + \frac{1}{2} \left(\epsilon^2 \mu (\vec{E} \cdot \vec{E}) + \epsilon \mu^2 (\vec{H} \cdot \vec{H}) \right) \vec{g} = \vec{0}
\end{aligned} \\
& \begin{array}{cccccc}
\text{B-1} & & \text{B-2} & & \text{B-3} & & \text{B-4} & & \text{B-5} & & \text{B-6}
\end{array}
\end{aligned}$$

Term B-1 represents the inertia term of the electromagnetic radiation. Term B-4 is the magnetic representation of the (electric) Coulomb's Force B-2 and Term B-3 is the electric representation of the (magnetic) Lorentz Force B-5. Term B-6 represents the Electromagnetic-Gravitational interaction of a gravitational field with field acceleration $\vec{g}$ acting on an arbitrary electromagnetic field configuration (a beam of light) with specific mass ρ .

The universal equation for the electromagnetic field (free electromagnetic waves and confined electromagnetic fields) within a gravitational field with gravity field intensity $\vec{g}$ has been presented in (72) and expresses the perfect equilibrium between the inertia forces (B-1), the electric forces (B-2 and B-3), the magnetic forces (B-4 and B-5) and the gravitational force (B-6) in any arbitrary electromagnetic field configuration.

$$\begin{aligned}
& -\frac{1}{c^2} \frac{\partial(\vec{E} \times \vec{H})}{\partial t} + \epsilon_0 \vec{E}(\nabla \cdot \vec{E}) - \epsilon_0 \vec{E} \times (\nabla \times \vec{E}) + \mu_0 \vec{H}(\nabla \cdot \vec{H}) - \\
& \quad \text{B-1} \quad \quad \quad \text{B-2} \quad \quad \quad \text{B-3} \quad \quad \quad \text{B-4} \\
& -\mu_0 \vec{H} \times (\nabla \times \vec{H}) + \frac{1}{2} \left(\epsilon^2 \mu (\vec{E} \cdot \vec{E}) + \epsilon \mu^2 (\vec{H} \cdot \vec{H}) \right) \vec{g} = \vec{0} \\
& \quad \quad \quad \text{B-5} \quad \quad \quad \text{B-6}
\end{aligned} \tag{73}$$

The “event horizon” is the boundary defining the region of space around a black hole from which nothing (not even light) can escape. The “event horizon” has been created by the equilibrium between the gravitational forces and the forces of electromagnetic interaction and the radiation pressure. At the boundary of a Black Hole does exist the perfect equilibrium. There are two types of Black Holes.

The first type represents an equilibrium in which the Black Hole has been represented by a hollow sphere. Only within the extreme thin shell of the hollow sphere does exist a perfect equilibrium. Inside the hollow sphere any kind of light (electromagnetic radiation) has been pressed with an extreme high radiation pressure towards to the “Shell of Perfect Equilibrium” (Event Horizon) because the radiation pressure inside the hollow sphere is always larger than the confining gravitational force. Outside the hollow sphere, any kind of light (electromagnetic radiation) has been attracted towards the “Shell of Perfect Equilibrium” (Event Horizon) because outside the hollow sphere the confining gravitational force is always larger than the radiation pressure. This type has been called “Transversal Black Holes”. Because like a planet moves within an orbit around a star, any beam of light (electromagnetic radiation) propagates within the Shell of Perfect Equilibrium” (Event Horizon) in an orbit around the Black Hole.

The second type represents an Equilibrium everywhere around the black Hole. At a special distance from the centre of the Black Hole, the radiation density increases suddenly very sharp. This has been called the Boundary (Event Horizon) around the Black Hole. This type has been called “Longitudinal Black Holes”. Because the light (electromagnetic radiation) moves towards the Black Holes or away from the Black Hole in the same direction as the

direction of the Gravitational Field generated by the Black Hole.

We consider a beam of light passing a strong gravitational field, generated by a Black Hole. According the first term in (1) the beam of light will follow a circular orbit around the Black Hole. The required Equilibrium will exist at the radius where the centrifugal electromagnetic inertia forces will be equal and opposite directed to the centripetal oriented gravitational forces on the electromagnetic mass. Figure 12 represents the orbit (colored red) of a LASER beam around a uniform intense gravitational field (Black Hole) .

In general, Newtons second law of motion has been presented as:

$$F = m a \quad (74)$$

In which “a” represents the acceleration which equals the difference of the velocity Δv divided by the time interval Δt .

$$a = \frac{\Delta v}{\Delta t} \quad (75)$$

The momentum p of a mechanical mass equals:

$$p = m v \quad (76)$$

Then Newton’s second law of motion can be presented as:

$$F_{\text{INERTIA}} = m a = m \frac{\Delta v}{\Delta t} = \frac{\Delta (m v)}{\Delta t} = \frac{\Delta (p)}{\Delta t} \quad (77)$$

Like a mechanical mass expresses the property of inertia, also a beam of light expressed the property of inertia. When the sun shines on the earth, the radiation of the sun presses on the earth with thousands of Newton.

Like a mechanical mass, also a beam of light has momentum. The momentum of a beam of light has been expressed by the Poynting vector S and equals the mechanical momentum vector p multiplied by the square of the speed of light c divided by the Volume.

$$F_{\text{INERTIA}} = m a = m \frac{\Delta v}{\Delta t} = \frac{\Delta (m v)}{\Delta t} = \frac{\Delta (p)}{\Delta t} = \frac{V \Delta (S)}{c^2 \Delta t} \quad (78)$$

(mechanical mass) (beam of light)

The inertia force density “ f ” equals the inertia force “ F ” divided by the Volume “ V ”.

$$f_{\text{INERTIA}} = \left(\frac{m}{V} \right) a = \rho \frac{\Delta v}{\Delta t} = \frac{1}{c^2} \frac{\Delta (S)}{\Delta t} \quad (79)$$

(mechanical mass) (beam of light)

The well-known equation of Einstein equals:

$$W = m c^2$$

$$w = \frac{W}{V} = \frac{m}{V} c^2 = \rho c^2 \quad (80)$$

In which “ w ” represents the electromagnetic energy density and equals:

$$w = \frac{1}{2} \epsilon E^2 + \frac{1}{2} \mu H^2 \quad (81)$$

For electromagnetic radiation the electromagnetic impedance Z_0 equals:

$$\begin{aligned}
Z_0 &= \frac{E}{H} = \sqrt{\frac{\mu}{\epsilon}} \\
H &= E \sqrt{\frac{\epsilon}{\mu}} \\
w &= \frac{1}{2} \epsilon E^2 + \frac{1}{2} \mu H^2 = \frac{1}{2} \epsilon E^2 + \frac{1}{2} \epsilon E^2 = \epsilon E^2
\end{aligned} \tag{82}$$

Substituting equation (66) in (64) results in:

$$\begin{aligned}
w &= \rho c^2 = \epsilon E^2 \\
\rho &= \frac{\epsilon}{c^2} E^2
\end{aligned} \tag{83}$$

Because the beam of light has been confined in the radial direction, it demonstrates in the radial direction the property of inertia (electromagnetic mass) and interacts with a gravitational field according Newton's second law of motion. The whole Universe is in a perfect Equilibrium. Also at the "Event Horizon" of a Black Hole does exist a perfect equilibrium between the confining gravitational force of the Black Hole and the radial directed inertia force density of the confined electromagnetic radiation (Laser Beam confined by a Black Hole at the "Event Horizon"). To determine the "Event Horizon" of the Black Hole (Radius of the circular orbit of the Laser Beam), we have to find the perfect equilibrium between the inertia force densities of the electromagnetic energy densities of the Laser Beam and the confining gravitational force acting on the electromagnetic energy densities of the Laser Beam.

$$\begin{aligned}
f_{\text{GRAVITY}} &= f_{\text{INERTIA}} \\
\rho g &= \frac{1}{c^2} \frac{\Delta (S)}{\Delta t}
\end{aligned} \tag{84}$$

Fig. 6 A LASER beam around a Black Hole captured in a circular orbit around the Black Hole in a Transversal Modus by the Gravitational interaction of the Black Hole with the mass (inertia) of the Laser Beam Light.

From Figure (5) follows the relationship between de changing in the Poynting vector ΔS and the time interval Δt :

$$\begin{aligned} \tan(\alpha) &= \frac{c \Delta t}{R} = \frac{\Delta S}{S} \\ \frac{\Delta S}{\Delta t} &= \frac{c S}{R} \\ \rho g &= \frac{1}{c^2} \frac{\Delta (S)}{\Delta t} = \frac{1}{c^2} \frac{c S}{R} = \frac{1}{c} \frac{S}{R} \end{aligned} \quad (85)$$

The Poynting vector $\bar{S}$ represents the total energy transport of the electromagnetic radiation per unit surface per unit time [J / m² s]. Which can be written as the cross product of the Electric Field intensity $\bar{E}$ and the magnetic Field intensity $\bar{H}$.

$$\begin{aligned}\bar{S} &= \bar{E} \times \bar{H} \\ S &= E H \sin(90^\circ) = E H \\ S &= E^2 \sqrt{\frac{\epsilon}{\mu}}\end{aligned}\tag{86}$$

Substituting equation (10) and (13) in (12) results in an equation for the Event Horizon at radius “R” of a Transversal Black Hole.

$$\begin{aligned}\rho \text{ g} &= \frac{1}{c} \frac{S}{R} \\ R &= \frac{S}{\rho \text{ c g}} \\ R &= \frac{E^2 \sqrt{\frac{\epsilon}{\mu}}}{\rho \text{ c g}} = \frac{E^2 \sqrt{\frac{\epsilon}{\mu}}}{\frac{\epsilon}{c} E^2 \text{ g}} \\ R &= \frac{c^2}{\text{g}} \approx \frac{9 \cdot 10^{16}}{\text{g}} \quad [\text{m}]\end{aligned}\tag{87}$$

Equation (84) represents the perfect equilibrium between the inertia force densities of the electromagnetic mass $\frac{1}{c^2} \frac{\Delta \bar{S}}{\Delta t}$ and

the centripetal oriented gravitational force density $\frac{w}{c^2} \bar{g}$ acting

on the electromagnetic mass. The perfect equilibrium direction where the inertia forces due to the circular orbit of the beam of light are in a perfect balance with the attractive gravitational

forces, exists at one defined radius “R” of the beam of light (LASER beam), independent of the intensity of the beam of light and independent of the frequency of the beam of light. Only the acceleration “g” of the gravitational field determines the radius of equilibrium “R”

$$R \approx \frac{9 \cdot 10^{16}}{g} \quad (88)$$

In which “R” is the radius of the beam of light and “g” the acceleration of the gravitational field of the “Black Hole”.

The x-y plane is oriented perpendicular on the z-direction. The speed of light towards the positive z-direction equals the speed of light (the constant "c = 300.000 km/s"). But the speed of light in the x-y plane has to be exactly zero [9,14,15]. Else the diameter of the laser beam would become larger and larger during the propagation along the positive z-direction. This is only possible because the Electromagnetic confining forces B-2, B-3, B-4 and B-5 in Equation (28) compensate exactly the outward oriented radiation pressure towards the x-direction and the y-direction.

The Electric Radiation Pressure has been compensated completely by the Coulomb Force Densities within the Laser Beam. At the same time the inertia force density within the beam of light has been fully compensation by the gravitational force density (generated by the black hole) comparable with a satellite propagating around the earth.

The Newtonian approach results in a Radius “R” (72) around a Black Hole comparable with the results in General Relativity. It is not necessary to develop a new theory in

which space and time are part of a curved space-time continuum.

3.2 Newton's approach to "Gravitational Redshift" based on Newtonian Physics.

To describe gravitational Redshift we have to start with Planck's Law describing the proportionality between Energy and Frequency.

Figure 7 Electromagnetic radiation confined between two 100 % reflecting mirrors

Figure 7 represents confined electromagnetic radiation with amplitude E_0 and frequency ω .

A general property of confined electromagnetic waves is the proportionality between energy and frequency. As an example we choose the confinement of light between two perfect reflecting mirrors with surface A. When we press both mirrors together of a distance Δx , the work ΔW has been delivered:

$$\Delta W = p A \Delta x \quad (90)$$

In which "A" equals the surface of the mirrors and "p" equals the [radiation pressure](#):

$$p = w = \frac{1}{2} \epsilon E^2 + \frac{1}{2} \mu H^2 \text{ [N / m}^2\text{]} \quad (91)$$

The Electromagnetic “Work ΔW ” which has been delivered equals:

$$\Delta W = w A \Delta x \quad (92)$$

When over a time “ Δt ” both mirrors move towards each other with a velocity “ v ”, then the distance “ Δx ” passed over a time interval Δt equals:

$$\Delta x = v \Delta t \quad [\text{m}] \quad (93)$$

Substituting (92) in (93) results in:

$$\begin{aligned} \Delta W &= w A \Delta x \\ \Delta W &= w A v \Delta t \end{aligned} \quad (94)$$

$$v = \frac{\Delta W}{w A \Delta t}$$

Due to the [Doppler-Shift](#), the frequency of the confined radiation will increase when the mirrors move towards each other and will decrease when both mirrors move apart from each other. When both mirrors move towards each other, the observed frequency shift Δf will be:

$$\Delta f = f_1 - f_0 = f_0 \sqrt{\frac{1 + \frac{v}{c}}{1 - \frac{v}{c}}} - f_0 = f_0 \left(\sqrt{\frac{1 + \frac{v}{c}}{1 - \frac{v}{c}}} - 1 \right) \quad (95)$$

Applying Taylor series, the observed frequency shift equals:

$$\Delta f = f_0 \left(\sqrt{\frac{1 + \frac{v}{c}}{1 - \frac{v}{c}}} - 1 \right) = f_0 \left(-1 + 1 + \frac{v}{c} + \frac{1}{2} \left(\frac{v}{c} \right)^2 + \frac{1}{2} \left(\frac{v}{c} \right)^3 + \frac{3}{8} \left(\frac{v}{c} \right)^4 + \dots \right) \quad (96)$$

$$+ f_0 \left(\frac{3}{8} \left(\frac{v}{c} \right)^5 + \frac{5}{16} \left(\frac{v}{c} \right)^6 + \frac{5}{16} \left(\frac{v}{c} \right)^7 + \frac{35}{128} \left(\frac{v}{c} \right)^8 + \frac{35}{128} \left(\frac{v}{c} \right)^9 + \frac{63}{256} \left(\frac{v}{c} \right)^{10} + \dots \right)$$

From

$$\Delta f = f_0 \left(1 + \frac{v}{c} + \frac{1}{2} \left(\frac{v}{c} \right)^2 + \frac{1}{2} \left(\frac{v}{c} \right)^3 + \frac{3}{8} \left(\frac{v}{c} \right)^4 - 1 \right)$$

$$\Delta f = f_0 \left(\frac{v}{c} + \frac{1}{2} \left(\frac{v}{c} \right)^2 + \frac{1}{2} \left(\frac{v}{c} \right)^3 + \frac{3}{8} \left(\frac{v}{c} \right)^4 \right)$$

At low velocities ($v \ll c$)

$$v \approx c \frac{\Delta f}{f_0} \approx \frac{\Delta W}{w A \Delta t} \quad (97)$$

$$\Delta f \approx \left(\frac{f_0}{w A c \Delta t} \right) \Delta W = \left(\frac{f_0}{W} \right) \Delta W$$

$$\Delta W = h_{EM} \Delta f$$

In which “W” equals the total energy involved in the transformation of Mechanical Energy into the Electromagnetic Energy. The term h_{EM} represents an Electromagnetic equivalent for Planck’s constant.

$$\Delta W = h_{EM} \Delta f$$

$$h_{EM} = \frac{f_0}{W} \quad (98)$$

The “Newtonian Equilibrium Equation for Electromagnetic Waves interacting with a Gravitational Field with acceleration $\bar{g}$ ”

has been presented in Chapter1: “The Fundamental Discussion between Newton and Maxwell”:
in Equation (47):

$$\begin{aligned}
 & \text{3-Dimensional Space Domain} \\
 & \begin{matrix} \text{B-1} & \text{B-2} & \text{B-3} \\ \text{B-4} & \text{B-5} & \text{B-6} \end{matrix} \\
 & \begin{pmatrix} x_3 \\ x_2 \\ x_1 \end{pmatrix} + \frac{1}{c^2} \frac{\partial (\vec{E} \times \vec{H})}{\partial t} + \epsilon_0 \vec{E} (\nabla \cdot \vec{E}) - \epsilon_0 \vec{E} \times (\nabla \times \vec{E}) + \\
 & + \mu_0 \vec{H} (\nabla \cdot \vec{H}) - \mu_0 \vec{H} \times (\nabla \times \vec{H}) + \frac{1}{2} (\epsilon^2 \mu (\vec{E} \cdot \vec{E}) + \epsilon \mu^2 (\vec{H} \cdot \vec{H})) \vec{g} = \vec{0} \quad (99)
 \end{aligned}$$

A fundamental Solution for Equation (99) within a gravitational constant gravitational field $\vec{g}$ in the z-direction, equals for the electric field:

$$\vec{E} = \begin{pmatrix} e_x \\ e_y \\ e_z \end{pmatrix} = \begin{pmatrix} e^{-\frac{1}{2} g z \mu_0 \epsilon_0} h \left[t - z \sqrt{\epsilon \mu} \right] \\ 0 \\ 0 \end{pmatrix} = \begin{pmatrix} e^{-\frac{1}{2} g z \mu_0 \epsilon_0} h \left[t - \frac{k_z}{\omega} z \right] \\ 0 \\ 0 \end{pmatrix} \quad (100)$$

And for the Magnetic Field:

$$\vec{H} = \begin{pmatrix} H_x \\ H_y \\ H_z \end{pmatrix} = \begin{pmatrix} 0 \\ \frac{1}{\sqrt{\epsilon_0 \mu_0}} e^{-\frac{1}{2} g z \mu_0 \epsilon_0} h \left[t - z \sqrt{\epsilon_0 \mu_0} \right] \\ 0 \end{pmatrix} = \begin{pmatrix} 0 \\ \frac{1}{\sqrt{\epsilon_0 \mu_0}} e^{-\frac{1}{2} g z \mu_0 \epsilon_0} h \left[t - \frac{k_z}{\omega} z \right] \\ 0 \end{pmatrix} \quad (101)$$

According Planck’s law for electromagnetic waves, the Newtonian presentation for the Gravitational Frequency Shift (Red-Shift) equals:

$$\vec{E} = \begin{pmatrix} e_x \\ e_y \\ e_z \end{pmatrix} = \begin{pmatrix} e^{-\frac{1}{2} g z \mu_0 \epsilon_0} h \left[t - \frac{k_z e^{-g z \mu_0 \epsilon_0}}{\omega e^{-g z \mu_0 \epsilon_0}} z \right] \\ 0 \\ 0 \end{pmatrix} \quad (102)$$

And for the Magnetic Field:

$$\vec{H} = \begin{pmatrix} H_x \\ H_y \\ H_z \end{pmatrix} = \begin{pmatrix} 0 \\ \frac{1}{\sqrt{\epsilon_0 \mu_0}} e^{-\frac{1}{2} g z \mu_0 \epsilon_0} h \left[t - \frac{k_z e^{-g z \mu_0 \epsilon_0}}{\omega e^{-g z \mu_0 \epsilon_0}} z \right] \\ 0 \end{pmatrix} \quad (103)$$

Equations (102) and (103) represent a “Constant Speed of Light” “c” In which the “Newtonian Gravitational Red-Shift” equals:

$$\omega_{\text{Newtonian Gravitational Redshift}} = \omega_0 e^{-g z \mu_0 \epsilon_0} \quad (104)$$

In which ω_0 equals the original frequency of the beam of light parallel to the constant gravitational field in the z-direction and the exponential term demonstrates the Gravitational Redshift when the beam of light moves away from the Gravity Source (Solar System or Black Hole) and represents the Blue-Shift when the beam of light moves towards the Gravity Source. Including the “Relativistic Longitudinal Doppler Effect” results in:

$$\omega_{\text{Newtonian Longitudinal Gravitational Redshift}} = \omega_0 e^{-g z \mu_0 \epsilon_0} \sqrt{\frac{1 + \frac{v}{c}}{1 - \frac{v}{c}}} \quad (105)$$

Equation (104) represents the “Longitudinal Gravitational Redshift” for a Constant Gravitational Field. The “Newton Electromagnetic Equilibrium Equation” (99) represents possible solutions for all “Time- and Space Depending Gravitational Fields” and Equation (99) is the fundamental equation to be “tested” relative to Einstein’s theory of General Relativity. New measurements of “Longitudinal Gravitational Frequency Shift (Red-Shift)” from World Wide Observatories could falsify or confirm this new theory.

3.3 Deviations in the “Hubble Constant” Value

Due to the [Doppler-Shift](#), the observed frequency of the radiation will increase when two objects move towards each other and will decrease when both objects move apart from each other. When both objects move apart from each other, the observed frequency shift Δf will be:

$$\Delta f = f_1 - f_0 = -f_0 \left(\sqrt{\frac{1 + \frac{v}{c}}{1 - \frac{v}{c}}} \right) \quad (106)$$

Applying Taylor series, the observed frequency shift equals:

$$\begin{aligned} \Delta f = f_0 \left(\sqrt{\frac{1 + \frac{v}{c}}{1 - \frac{v}{c}}} - 1 \right) &= f_0 \left(-1 + 1 + \frac{v}{c} + \frac{1}{2} \left(\frac{v}{c} \right)^2 + \frac{1}{2} \left(\frac{v}{c} \right)^3 + \frac{3}{8} \left(\frac{v}{c} \right)^4 + \right) + \\ &+ f_0 \left(\frac{3}{8} \left(\frac{v}{c} \right)^5 + \frac{5}{16} \left(\frac{v}{c} \right)^6 + \frac{5}{16} \left(\frac{v}{c} \right)^7 + \frac{35}{128} \left(\frac{v}{c} \right)^8 + \frac{35}{128} \left(\frac{v}{c} \right)^9 + \frac{63}{256} \left(\frac{v}{c} \right)^{10} + \dots \right) \end{aligned} \quad (107)$$

Which approximates:

$$\begin{aligned}\Delta f_{Doppler} &= -f_0 \left(1 + \frac{v}{c} + \frac{1}{2} \left(\frac{v}{c} \right)^2 + \frac{1}{2} \left(\frac{v}{c} \right)^3 + \frac{3}{8} \left(\frac{v}{c} \right)^4 - 1 \right) \\ \Delta f_{Doppler} &= f_0 \left(\frac{v}{c} + \frac{1}{2} \left(\frac{v}{c} \right)^2 + \frac{1}{2} \left(\frac{v}{c} \right)^3 + \frac{3}{8} \left(\frac{v}{c} \right)^4 \right)\end{aligned}\tag{108}$$

At low velocities ($v \ll c$)

$$\Delta f_{Doppler} = f_0 \left(\frac{v}{c} + \frac{1}{2} \left(\frac{v}{c} \right)^2 + \frac{1}{2} \left(\frac{v}{c} \right)^3 \right)$$

Taylor series for the Gravitational Red-Shift results in:

$$\begin{aligned}\Delta f_{NGR} &= \omega_0 \left(-g_z \mu_0 \varepsilon_0 \right) + \\ &+ \frac{1}{2} \left(-g_z \mu_0 \varepsilon_0 \right)^2 + \frac{1}{6} \left(-g_z \mu_0 \varepsilon_0 \right)^3 + \dots\end{aligned}\tag{109}$$

It follows from (109) that the observed Gravitational Frequency Shift is proportional to the distance “z” between both objects. Under the assumption that the Doppler shift has been caused by a “relative velocity” between both objects, we observe an expanding universe with a “Constant Relative Velocity ($H_0 = 67.4 \pm 0.5 \text{ km s}^{-1} \text{ Mpc}^{-1}$)” in which the “Relative Velocity” between both objects is proportional with the distance between both objects. Under the assumption that the average gravitational field is constant over the distance “z” or gravitational fluctuations counterbalance each other, the conclusion can be drawn that the “Hubble Constant Value” has been measured under the condition of an expanding universe or under the condition of a relative constant gravitational field. Both conditions will result in the same observations (Ref. [11] and [12]).

$$\begin{aligned}
\Delta f_{NGR} &= \omega_0 e^{-g z \mu_0 \epsilon_0} = f_0 \left(-g \frac{z}{c^2} \right) + \\
&\quad + \frac{1}{2} \left(-g \frac{z}{c^2} \right)^2 + \frac{1}{6} \left(-g \frac{z}{c^2} \right)^3 \dots\dots\dots \\
\Delta f_{Doppler} &= -f_0 \left(\frac{v}{c} + \frac{1}{2} \left(\frac{v}{c} \right)^2 + \frac{1}{2} \left(\frac{v}{c} \right)^3 \right) \quad (110) \\
\Delta H_0 &= \frac{1}{v} \left(\frac{zg}{c} \right) \left(\Delta f_{Doppler} \right) - \Delta f_{NGR} \approx \frac{1}{2c^3} z g v - \frac{1}{2c^4} g^2 z^2 \\
\Delta H_0 &= \frac{1}{2c^3} z g \left(v - g \frac{z}{c} \right) \approx 2 \cdot 10^{-26} \left(v - g \frac{z}{c} \right) (z g)
\end{aligned}$$

It follows from (110) that with a measurement accuracy of 10 %, for the “Hubble Constant H_0 ” the first deviation term ΔH_0 in the “Hubble Constant” will appear at distances of about 10^{25} [m] (about 1000 Mpc). This is under the assumption of the absence of strongly disturbing gravitational fields generated by objects like a “Black Hole”. In the presence of disturbing objects, higher deviations in the “Hubble Constant” will be measured, which appears in recent measurements by the (HST). In recent measurements for the “Hubble Constant” by the HST, fundamental deviations (Ref. [14] and [15]) in the Hubble Constant has been measured. Being recently observed by the HST, no other theory explains this effect .

Fig. 8 Plot of measured H_0 (Colour Blue) and calculated $H_{0(NRS)}$ (Colour Orange) within an averaged universal gravitational field $g = 10^{-10} \text{ [m/s}^2\text{]}$, causing an additional Gravitational “Redshift” as function of the Distance “z” between Object and Observer.

Fig. 9 Plot of measured H_0 (Colour Blue) and calculated $H_{0(NRS)}$ (Colour Orange) within a gravitational field of the “Milky Way Galaxy” (1.5×10^{12} Solar Masses), causing an additional Gravitational “Blueshift” as function of the Distance “z” between Object and the Earth.

3.4 The Universe

A fundamental problem in the value of the “Hubble Constant” is that we measure with a very precisely instrument the “HST”, which is looking a little bit with “crossed eyes” towards our Universe. Because the galaxies are not really there where “HST” measures it. The intensities are not really that value which the “HST” measures and therefore the distances are differently than the “HST measures and also the redshift is different than which the “HST measures. Because the “HST” has been designed for an “Euclidean (linear) Universe”. And the Universe is not Euclidean at all. Gravity is everywhere in the universe and for that reason the Universe in not Euclidean. And “GR” is not enough and it is not big enough to correct the values for the “HST” for a “Non Euclidean Universe”.

The impact of the gravitational field around our “Milky Way Galaxy” on our “HST” measurements are nothing compared to the real enormously gigantic and intense gravitational fields in our Galaxy. With our vey accurate measurements we measure a not existing universe. The real “Non Euclidean Universe” is very differently.

The “Whirlpool Galaxy” lies 31 million light-years from Earth and has an estimated diameter of 76,000 light-years. Overall the galaxy is about 43% the size of the Milky Way. Its mass is estimated to be 160 billion solar masses. The gravitational force intensities are so massive in and around the “Whirlpool Galaxy” that reasonable measurements are only possible when we involve the interaction between Gravity and Light.

3.5 Measurements with the “HST”.

For measurements with the “Hubble Space Telescope” correction are needed for the impact of gravity on the observations.

For simplicity 3 distinguishments have been made for the different kinds of gravitational fields. The first one is a function with a linear increment to the source of the gravitational field (The center of the of the Milky Way Galaxy to the Edge of the Milky Way Galaxy) in which the gravitational acceleration “g”. and the corresponding solution for equation (99) have been presents in equation (111) . The second gravitational field is proportional to $1 / r^2$ (The gravitational field around the edge of the Milky Way Galaxy) in which “r” equals the distance. The third type of Gravitational Field is a constant Gravitational Field over Long Distances far away from sources of gravity like Black Holes.

3.6 The Introduction of Gravitational Redshift.

When on Earth a ball has been thrown up, the Kinetic Energy (EM field) has been converted into a Potential Energy. When a Beam of Light (e.g. Laser Beam) shines up, something comparable happens. The EM Field Intensity becomes exponentially lower (the higher the beam shines upwards) but the speed does not change. The speed of light remains always constant. For a Laser Beam shining downwards on earth, the opposite happens. The intensity becomes (exponentially) higher and the observed frequency higher (Blue Shift). For that reason a lower “Hubble Constant” Value H_0 will be measured because the real Read Shift has been Higher than being measured by the “HST” because of the Gravitational Field of the Milky Way Galaxy.

But far away, when the Red-Shift has been measured by the “HST” of e.g. the “GN-z11”), the opposite happens. The Light being emitted e.g. by “GN-z11” has to leave the Gravitational field of the “GN-z11) and an additional Red-Shift has been introduced by its own gravitational field.

$$(\omega_{\text{Newtonian Longitudinal Gravitational Redshift}} = \omega_{\text{NLGR}})$$

Gravitational Field Type 1

$$g = G_1 z$$

$$\omega_{NLGR} = \omega_0 e^{-\frac{1}{4} G_1 z^2 \epsilon_0 \mu_0} \sqrt{\frac{1 + \frac{v}{c}}{1 - \frac{v}{c}}}$$

Gravitational Field Type 2

$$g = \frac{G_1}{z^2} \quad (111)$$

$$\omega_{NLGR} = \omega_0 e^{-\frac{G_1 \epsilon_0 \mu_0}{2 z}} \sqrt{\frac{1 + \frac{v}{c}}{1 - \frac{v}{c}}}$$

Gravitational Field Type 3

$$g = G_1$$

$$\omega_{NLGR} = \omega_0 e^{-\frac{1}{2} g z \epsilon_0 \mu_0} \sqrt{\frac{1 + \frac{v}{c}}{1 - \frac{v}{c}}}$$

For a gravitational field proportional to z^n , Equation (111) can be presented as:

Gravitational Field Type z^n

$$g = G_1 z^n$$

$$\omega_{NLGR} = \omega_0 e^{\frac{-G_1 z^{1+n} \epsilon_0 \mu_0}{2(1+n)}} \sqrt{\frac{1 + \frac{v}{c}}{1 - \frac{v}{c}}} \quad (112)$$

In general Equation (111) can be represented as:

Gravitational Field as a function "h(z)" along the z-axis between "object" and observer

$$g = G_1 g[z]$$

$$\omega_{NLGR} = \omega_0 e^{-\frac{1}{2} \epsilon_0 \mu_0 G_1 \int_0^z g(h) dh} \sqrt{\frac{1 + \frac{v}{c}}{1 - \frac{v}{c}}} \quad (113)$$

frequency being observed original frequency Gravitational Redshift Doppler Redshift

3.7 The Introduction of Gravitational Intensity Shift.

According equation (67), which describes Planck's law for electromagnetic configurations, the Gravitational Intensity Shift is proportional to the Gravitational Redshift.

Gravitational Field as a function "h(z)" along the z-axis between "object" and observer

$$g = G_1 g[z] \quad (114)$$

$$I_{\text{NLGR}} = I_0 e^{-\frac{1}{2} \epsilon_0 \mu_0 G_1 \int_0^z g(h) dh} \sqrt{\frac{1 + \frac{v}{c}}{1 - \frac{v}{c}}}$$

intensity being observed original intensity Gravitational Redshift Doppler Redshift

The observed intensity of the emitting object is due to the Gravitational Redshift lower/ higher than the original intensity. This implies that objects have a smaller/larger distance than being observed.

5. Conclusions

It is possible to design **GEONs** with sizes of sub atomic level ($< 10^{-10}$ [m]) and an infinite lifetime which are in perfect equilibrium with themselves and their surrounding. (Equation (51), Figure (4)).

Solutions for **GEONs** (Gravitational Electromagnetic Confinement) always have to be solutions of the relativistic quantum mechanical Dirac Equation (Equation 47.1)

Measuring the **imaginary part** of the solutions for the relativistic quantum mechanical Dirac Equation is *identical* with measuring the **imaginary part** of the quantum mechanical probability waves (de Broglie waves). When the Electromagnetic confined waves for the **GEONs** have been written in a quantum mechanical complex way:

$$\bar{\phi} = \frac{1}{\sqrt{2} \mu} \left(\bar{B} + i \frac{\bar{E}}{c} \right)$$

In which “B” equals the magnetic field component of the electromagnetic GEON field configuration and “E” equals the electric field component of the electromagnetic GEON field configuration). Then is well understandable how the imaginary part of the GEON waves have been measured. Instead of the **magnetic part (B)**, the electric **part (E)** of the **GEONs** has been measured.

For this reason the results of the experiments, published in 2021 “[Operational Resource Theory of Imaginarity](#)” in “[Physical Review Letters](#)”(Ref. [2]) present strong evidence for the existence at sub-atomic level of the **electromagnetic GEONs** and the correctness of Wheeler’s theory.

The Newtonian approach results in a Radius “R” (88) around a Black Hole comparable with the results in General Relativity. Equation (105) represents the “Longitudinal Gravitational Redshift” for a Constant Gravitational Field including the doppler effect. Accurate observations by the “Hubble Space Telescope” of variations in the “Hubble Constant Value” nearby strong gravitational fields will falsify or confirm the new theory.

The new theory predicts deviations (Ref. [14] – [18]) ΔH_0 (Equation 110) in the “Hubble Constant” H_0 proportional with the relative distance “z” between object and observer and relative velocity “v” between both objects and strong inhomogeneous gravitational fields (Black Holes). Until now, this is the only theory which explains the deviations in the “Hubble Constant”, measured by the “Hubble Space Telescope” at distances larger than about 1000 Mpc.

5.1 Data Availability

All the Data and all the Calculations to provide evidence to “Quantum Light Theory” have been published in the ‘Open Source Framework(OSF)’ : <https://osf.io/gbn4p/>

DOI: [10.31219/osf.io/gbn4p](https://doi.org/10.31219/osf.io/gbn4p)
(<https://doi.org/10.31219/osf.io/gbn4p>)

(Calculations in Mathematica 11.0)’ , Page 1 – 33).

References

- [1] Geons; Wheeler; John Archibald; Phys. Rev. 97, 511, Issue 2, pages 511-526, Published 15 January 1955; Publisher: American Physical Society; DOI: 10.1103/PhysRev.97.511.
- [2] Operational Resource Theory of Imaginarity; Kang-Da Wu, Tulja Varun Kondra, Swapan Rana, Carlo Maria Scandolo, Guo-Yong Xiang, Chuan-Feng Li, Guang-Can Guo, and Alexander Streltsov; Phys. Rev. Lett. 126, 090401 – Published 1 March 2021.
- [4] Z. K. Mineev, S. O. Mundhada, S. Shankar, P. Reinhold, R. Gutiérrez-Jáuregui, R.J. Schoelkopf, N. Mirrahimi, H.J. Carmichael and M. H. Devoret; To catch and reverse a quantum jump mid-flight; Nature; 03 June 2019 equilibrium beyond Einstein 4-Dimensional, Kaluza-Klein 5-Dimensional and Superstring 10- and 11 Dimensional Curved Hyperspaces. <https://www.nature.com/articles/s41586-019-1287-z>
- [5] A. S. Stodolna, A. Rouzée, F. Lépine, S. Cohen, F. Robicheaux, A. Gijsbertsen, J. H. Jungmann, C. Bordas, and M. J. J. Vrakking. Hydrogen Atoms under Magnification: Direct Observation of the Nodal Structure of Stark States. [Phys. Rev. Lett. 110, 213001](https://doi.org/10.1126/science.1257650) – Published 20 May 2013
- [6] IBM Blog Research; A new effect in electromagnetism discovered – 150 years later; <https://phys.org/news/2017-10-effect-electromagnetism-years.html>
- [7] Abuter, R.; Amorim, A.; Anugu, N.; Bauböck, M.; Benisty, M.; Berger, J. P.; Blind, N.; Bonnet, H.; Brandner, W.; Buron, A.; Collin, C. (2018-07-01). "Detection of the gravitational redshift in the orbit of the star S2 near the Galactic centre massive black hole". Astronomy & Astrophysics. DOI: <https://doi.org/10.1051/0004-6361/201833718>

- [8] “Gurzadyan, V.G., Stepanian, A. Hubble tension vs two flows. Eur. Phys. J. Plus 136, 235 (2021).
<https://doi.org/10.1140/epjp/s13360-021-01229-x>
- [9] “[Hayley J. Macpherson et al](#)”, 2018, The Astrophysical Journal Letters, Volume 865, Number 1
- [10] “M.L.Mc Clure, C.C.Dyerb, Anisotropy in the Hubble constant as observed in the HST extragalactic distance scale key project results,
<https://doi.org/10.1016/j.newast.2007.03.005>
- [11] Antonio Enea Romano, Hubble trouble or Hubble bubble?, International Journal of Modern Physics D VOL. 27, NO. 09, <https://doi.org/10.1142/S021827181850102X>
- [12] Kaya, Ali, Hubble’s law and faster than light expansion speeds, American Journal of Physics 79, 1151 (2011);
<https://doi.org/10.1119/1.3625871>
- [13] Eleonora Di Valentino et al, In the Realm of the Hubble tension – a Review of Solutions, Classical and Quantum Gravity, DOI: [10.1088/1361-6382/ac086d](https://doi.org/10.1088/1361-6382/ac086d)
- [14] S.L. Parnovsky, Bias of the Hubble constant value caused by errors in galactic distance indicators, Ukr. J. Phys, <https://arxiv.org/abs/2109.09645v2>
- [15] Stephen M. Feeney, Hiranya V. Peiris, Samaya M. Nissanke, and Daniel J. Mortlock, [Prospects for Measuring the Hubble Constant with Neutron-Star–Black-Hole Mergers](#) Phys. Rev. Lett. 126, 171102 – Published 28 April 2021.
- [16] T. de Jaeger, B. E. Stahl, W. Zheng, A. V Filippenko, A. G. Riess, L. Galbany, A measurement of the Hubble constant from Type II supernovae, Monthly Notices of the Royal Astronomical Society, Volume 496, Issue 3, August 2020, <https://doi.org/10.1093/mnras/staa1801>
- [17] Wendy L. Freedman, [Measurements of the Hubble Constant: Tensions in Perspective](#), Department of Astronomy & Astrophysics & Kavli Institute for Cosmological Physics, University of Chicago, arxiv.org/pdf/2106.15656.pdf.

- [18] Licia Verde, Tommaso Treu and Adam G. Riess, Tensions between the early and late Universe, *Nat Astron* 3, 891–895 (2019), <https://doi.org/10.1038/s41550-019-0902-0>
- [19] Ignacio Trujillo et al, A distance of 13 Mpc resolves the claimed anomalies of the galaxy lacking dark matter, DOI: <https://doi.org/10.1093/mnras/stz771>
- [20] Nandita Khetan et al, A new measurement of the Hubble constant using Type Ia supernovae calibrated with surface brightness fluctuations, *Astronomy and Astrophysics*, Volume 647, March 2021, <https://doi.org/10.1051/0004-6361/202039196>