

CNNs, RNNs, and Parameter Sharing

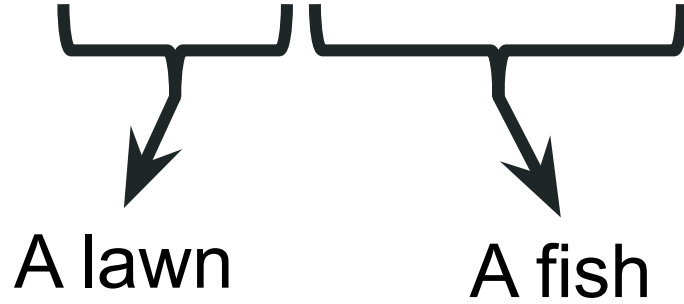
Alona Fyshe (h/t Konrad Kording)



Section 0: Introduction



Alona Fyshe



Last week: Regularization

Last week you learned about regularization

- Improves generalization

- Encourages simpler models: L1, L2, early stopping

- Data augmentation

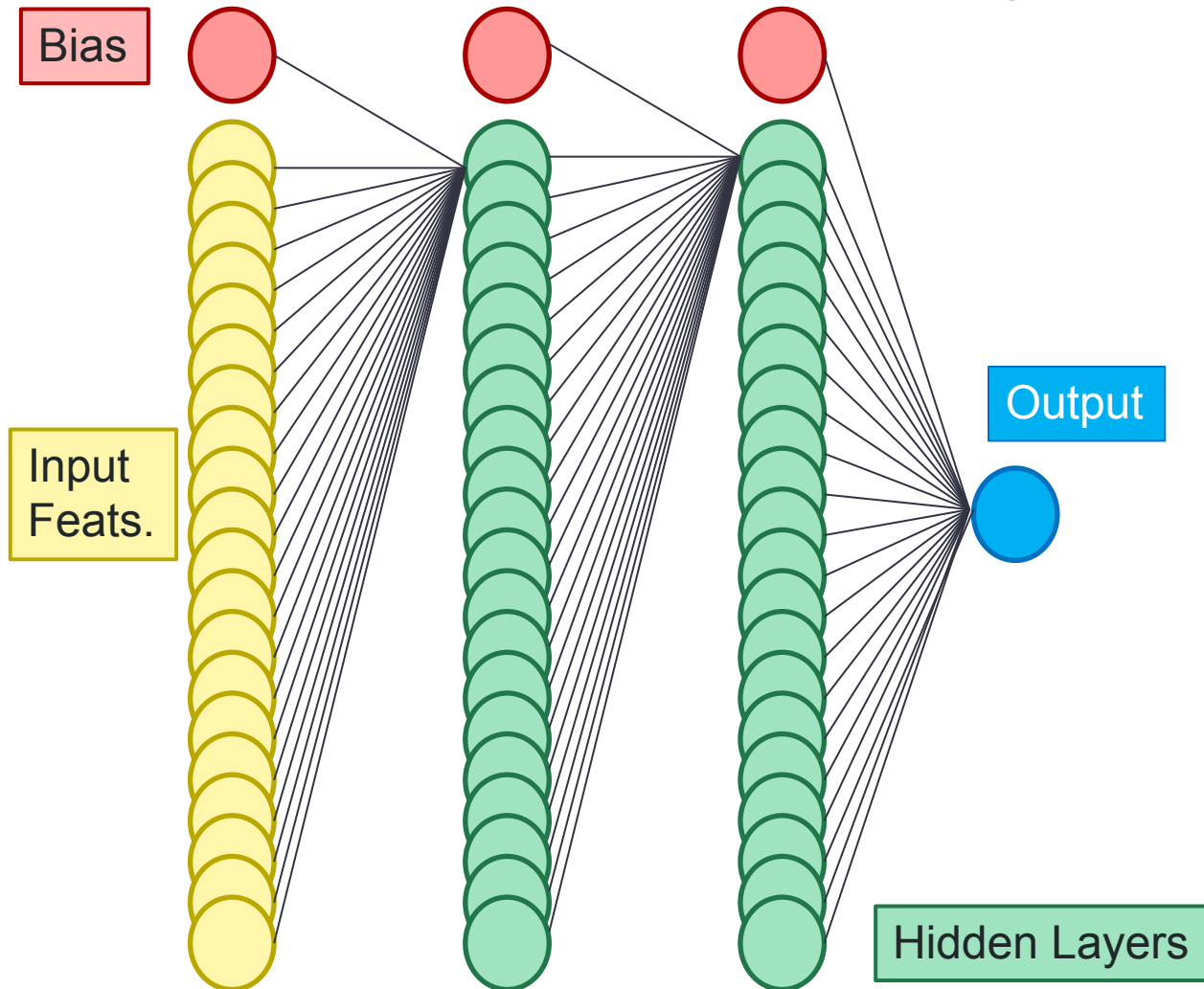
- Dropout

Recall: regularization reduces the **effective** number of parameters in a model

Today: Parameter Sharing: CNNs and RNNs

- Convolutional Neural Networks (CNNs) operate on images
 - Parameter share over space
 - CIFAR 10 images are $32 \times 32 = 1024$ pixels, 1024 input features
 - ImageNet often pre-processed to be $256 \times 256 = \sim 64K$ pixels, $\sim 64k$ input features 🤪
- Recurrent Neural networks (RNNs) operate on sequences of data
 - Often data sequences that occur over time
 - Time series can be long, but more importantly, they can vary in length

An MLP can have many many params



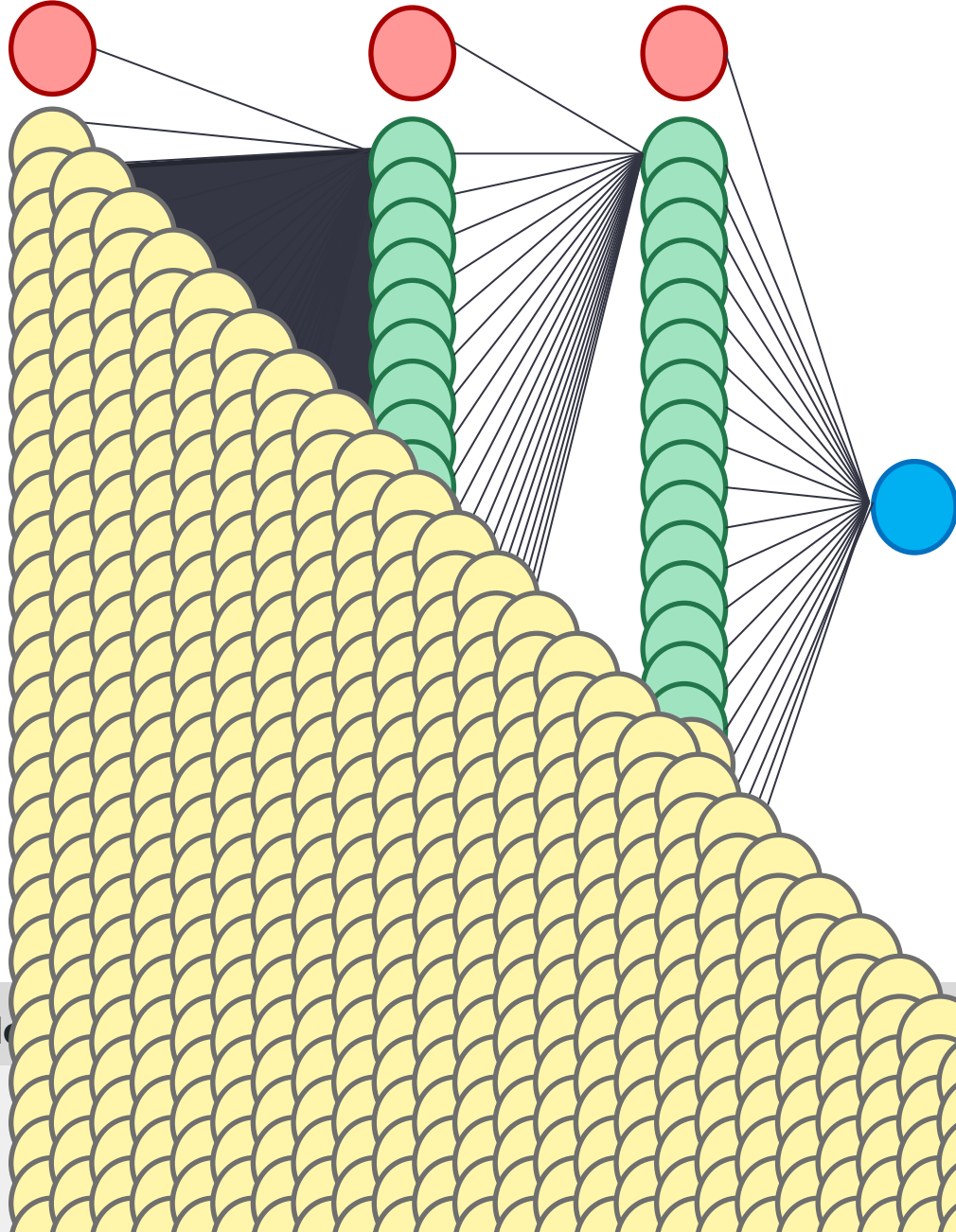
Data: 20 input features, single binary label

- 1 input layer with 20 nodes,
- 2 fully connected layers, 20 nodes each
- 1 final prediction node

How many weights is that?

$(20+1)*20+(20+1)*20+(20+1)*1=861$ params

An MLP can have many many params



1 input layer with 256*256 nodes,
2 fully connected layers, 20 nodes each
1 final prediction node

How many weights is that?

$(256*256+1)*20+(20+1)*20+(20+1)*1 = \sim 1.3\text{M params}$

And that's with only two fairly small hidden layers!
Modern CNNs have many more layers! 50-100 or more!

Translation invariance in images

- At the same time that the number of parameters grows very quickly, we are missing an opportunity



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Outline

- Neuroscience motivation for CNNs
- Definitions and intuitions
- Parts of a CNN
 - Convolutional layers
 - Pooling layers
 - Putting it together

Regularization

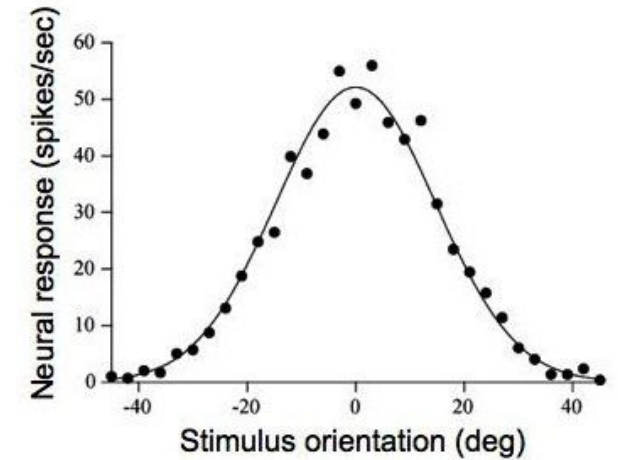
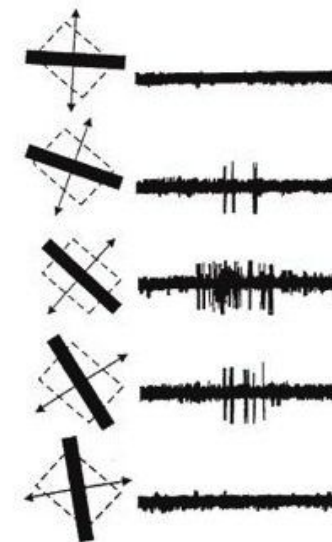
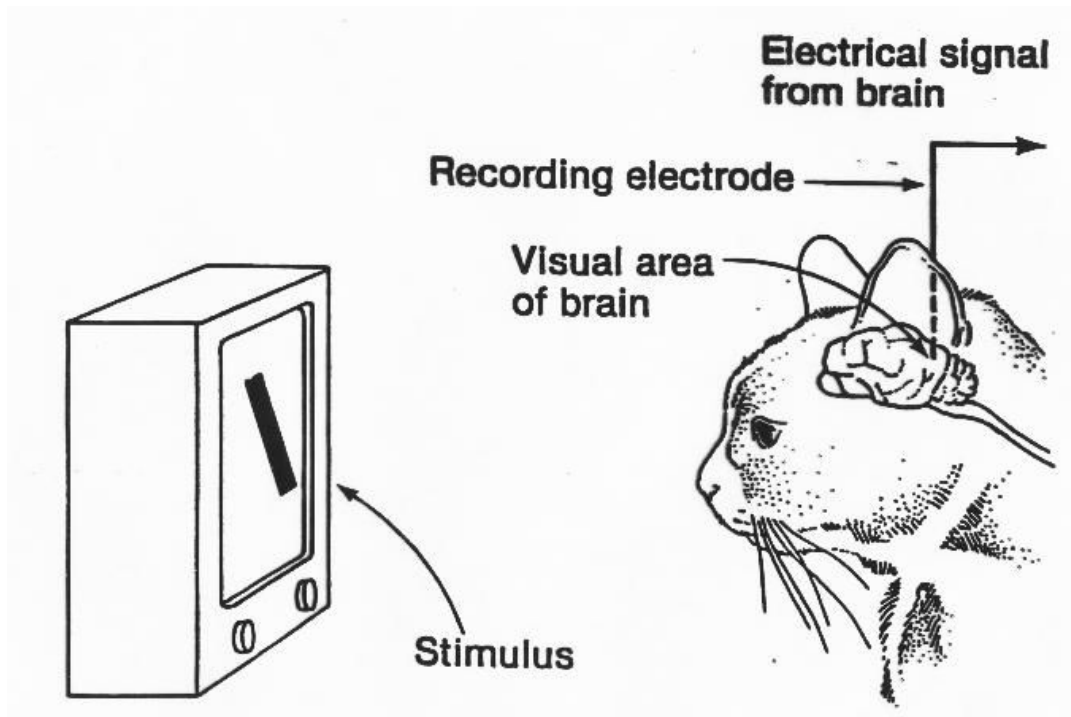
E 1.1. Regularization reduces # effective params

Section 1: Representations & Visual processing in the brain

Visual Processing in the Brain

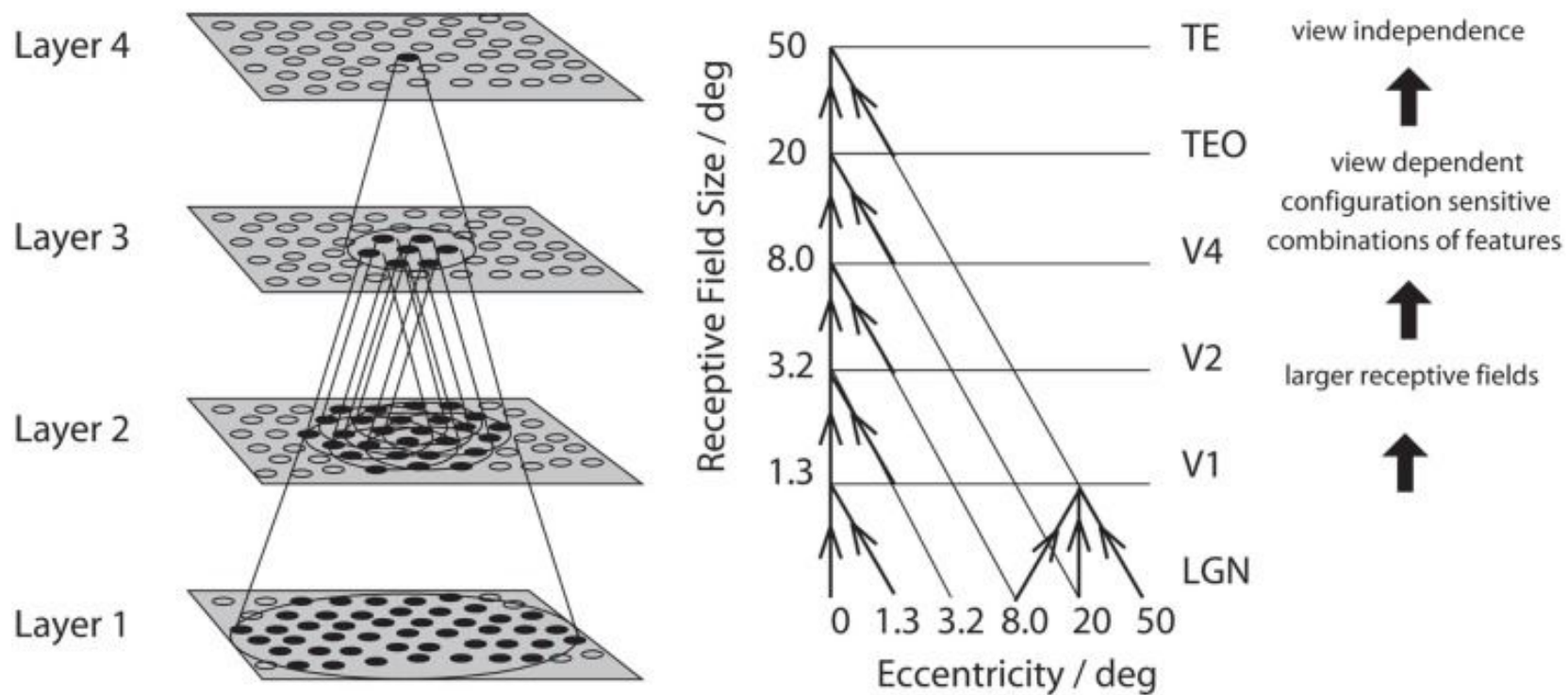
- The brain is an efficient machine
- How does it “solve” vision?

Hubel and Wiesel



Hubel & Wiesel, 1968

A hierarchy of processing



Rolls 2012

Invariances



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Translation Invariance



Rotation/Viewpoint Invariance



Size Invariance



Illumination Invariance



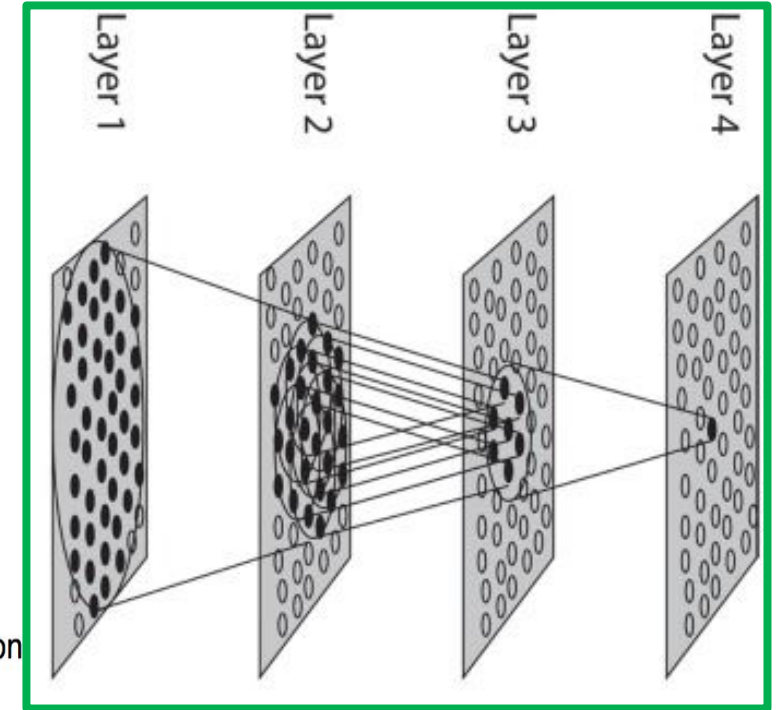
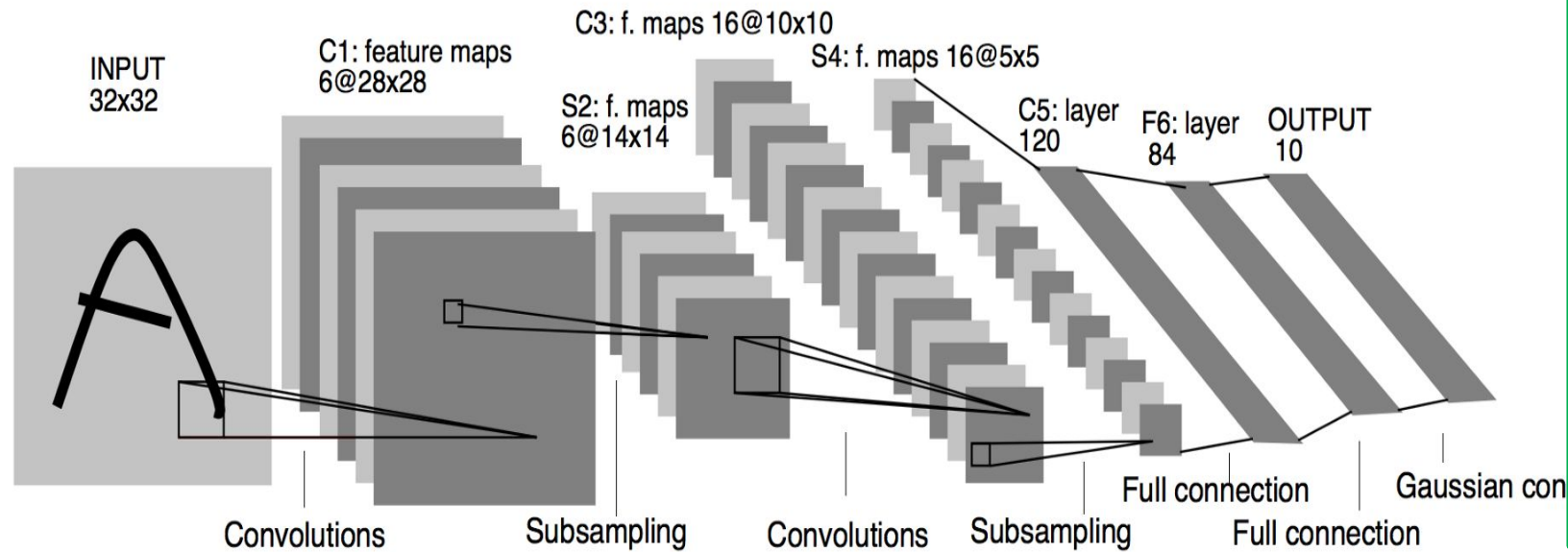
Matt Krause
mattkrause

Early history of CNNs



LeNet (1998) -- Architecture

- Developed by Yann LeCun @ Bell labs



LeNet (1998) -- Results

- Successfully trained a 60K parameter neural network without GPU acceleration!
- Automatically reading zip codes on mail
- 0.8% error on MNIST; near state-of-the-art at the time.

LeNet: <http://yann.lecun.com/exdb/publis/pdf/lecun-01a.pdf>

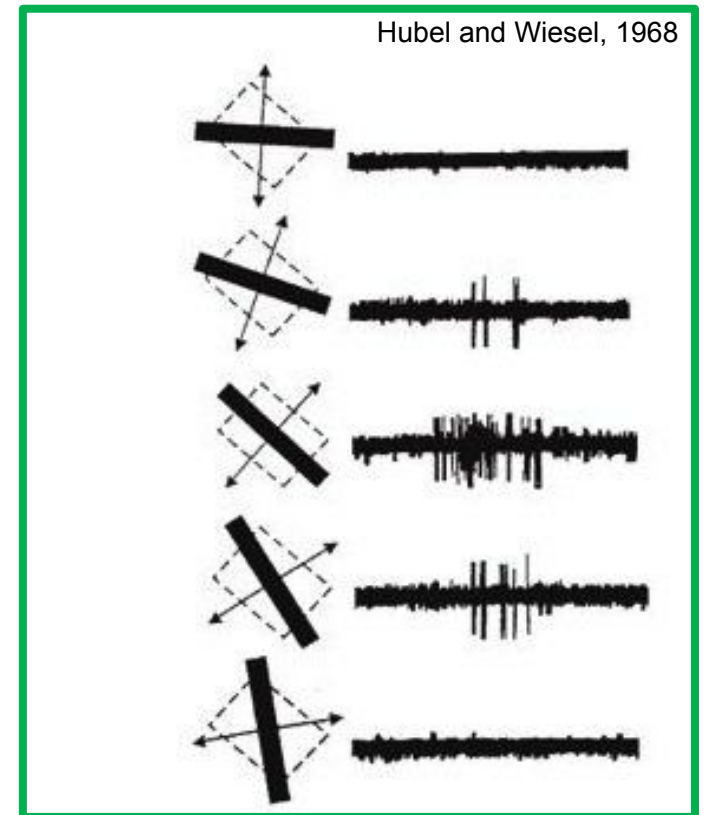


CNNs: Convolution

- Typical Learned Filters



Krizhevsky et al., 2012



Hubel and Wiesel, 1968

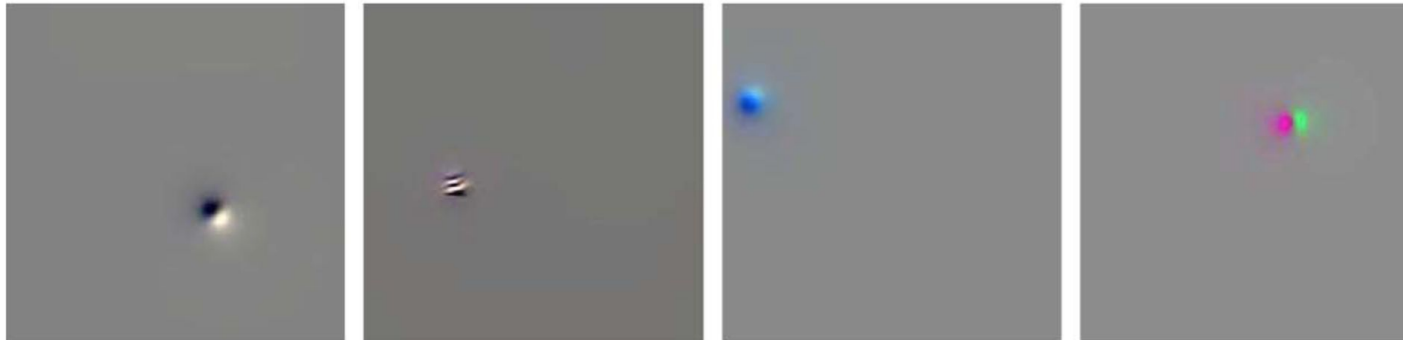
CNN3



CNN2



CNN1

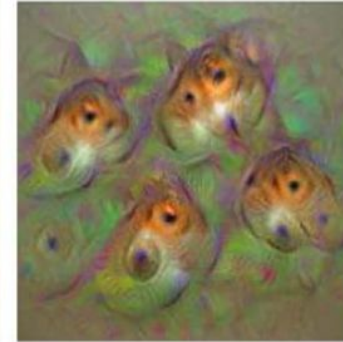


Horikawa & Kamitani (2017)

CNN8



CNN7



CNN6



Horikawa & Kamitani (2017)

DL is a story of representation learning

Hence ICLR

What is a representation?

A symbol or construct that approximates the entities and/or relations in the real world

Your brain has representations of the real world because it cannot actually *contain* the real world

DL is a story of representation learning

Your brain's representations allow it to approximate the real world in very useful ways.

E.g. you understand that some objects are more similar than others, you understand that objects can work together, objects can be parts of other objects, etc...

What do we want a good representation to do for us?

Regularization

Discuss with your pod...

E 1.1 What makes a representation good?

Consider: Object vs digit classification - how would the representations differ?

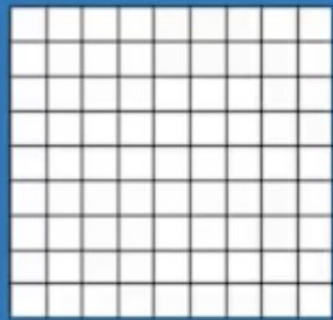
Section 2:

What is a CNN? Convolution?

What is a CNN?

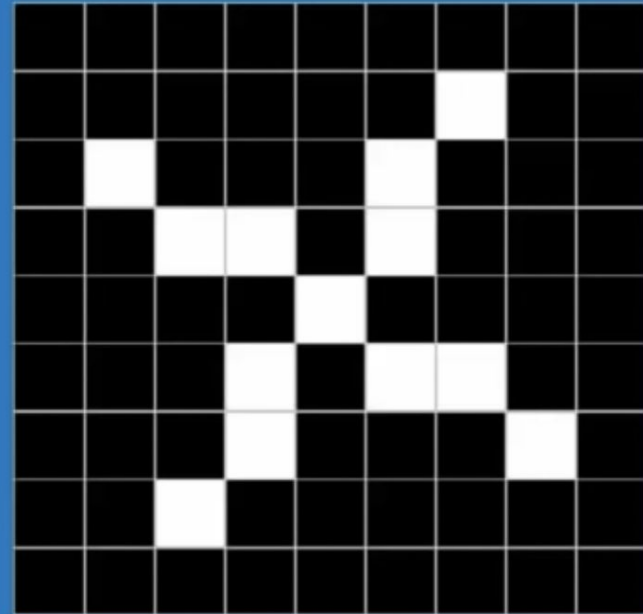
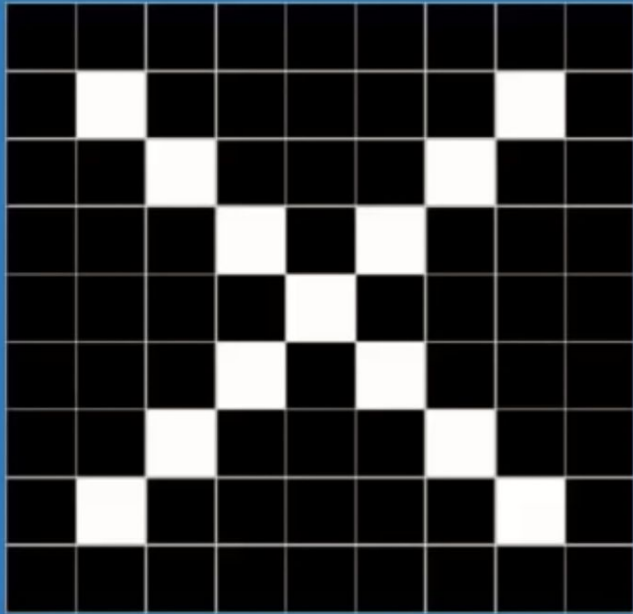
All the (blue) slides adapted from Brandon Rohrer with permission

A two-dimensional
array of pixels



X or **O**

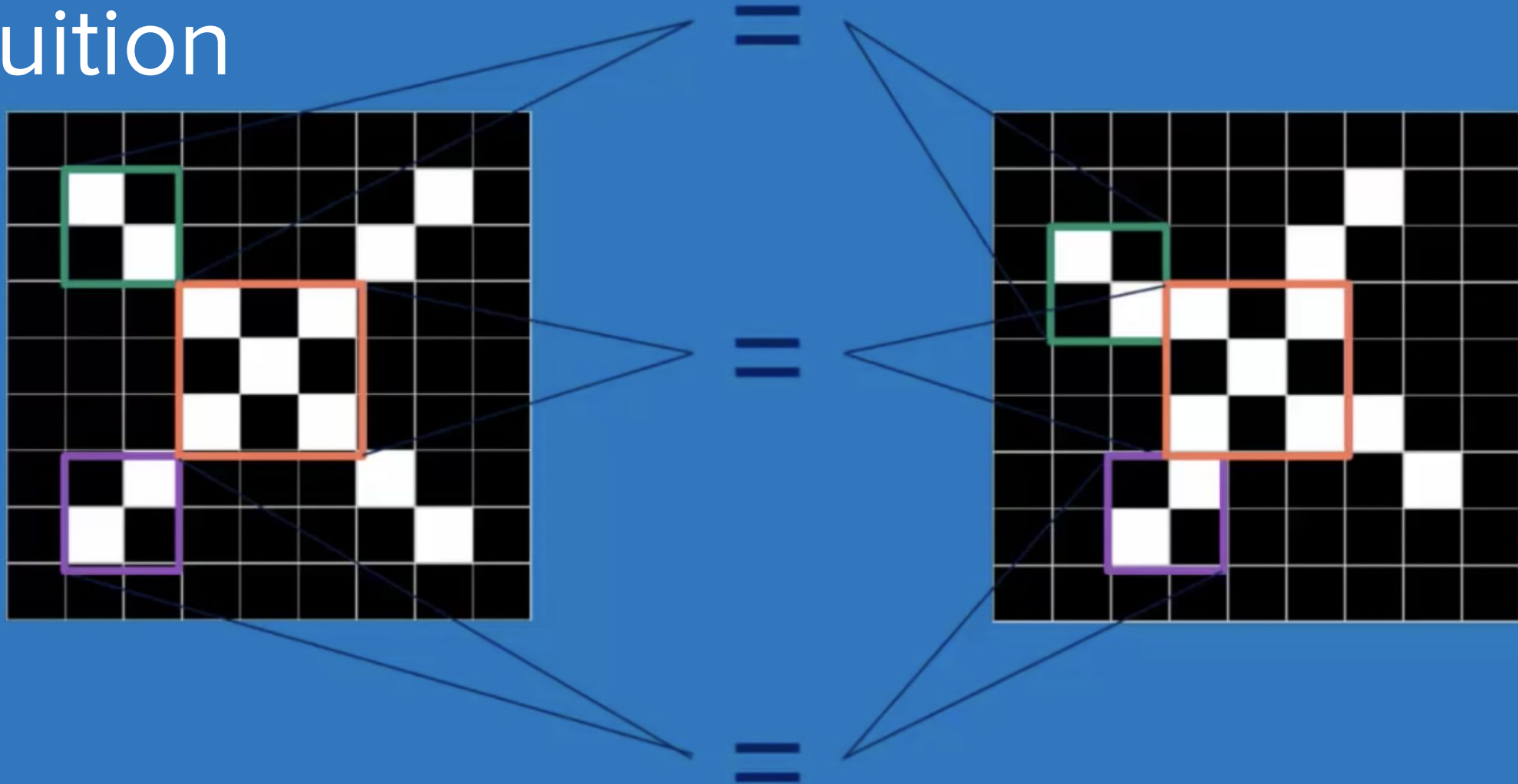
Nontrivial



Naive comparison

-1	-1	-1	-1	-1	-1	-1	-1	-1
-1	X	-1	-1	-1	-1	X	X	-1
-1	X	X	-1	-1	X	X	-1	-1
-1	-1	X	1	-1	1	-1	-1	-1
-1	-1	-1	-1	1	-1	-1	-1	-1
-1	-1	-1	1	-1	1	X	-1	-1
-1	-1	X	X	-1	-1	X	X	-1
-1	X	X	-1	-1	-1	-1	X	-1
-1	-1	-1	-1	-1	-1	-1	-1	-1

Intuition



Potential local features

1	-1	-1
-1	1	-1
-1	-1	1

1	-1	1
-1	1	-1
1	-1	1

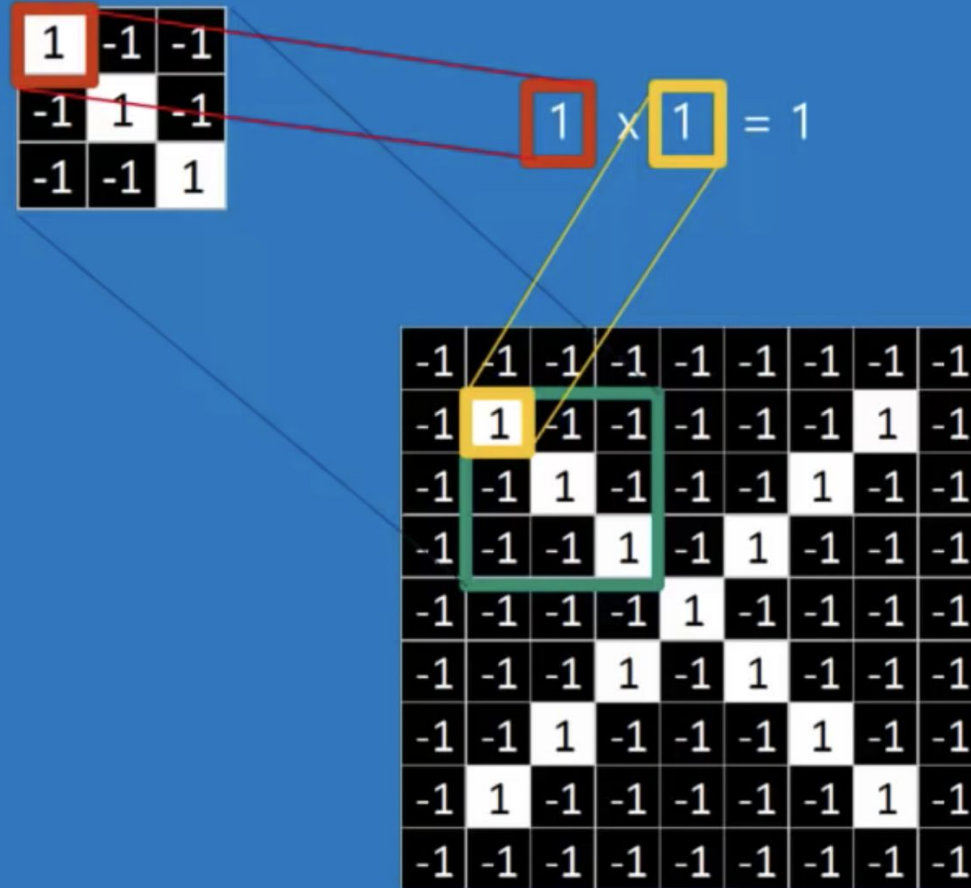
-1	-1	1
-1	1	-1
1	-1	-1

Setting

1	-1	-1
-1	1	-1
-1	-1	1

-1	-1	-1	-1	-1	-1	-1	-1	-1
-1	1	-1	-1	-1	-1	-1	1	-1
-1	-1	1	-1	-1	-1	1	-1	-1
-1	-1	-1	1	-1	1	-1	-1	-1
-1	-1	-1	-1	1	-1	-1	-1	-1
-1	-1	-1	1	-1	1	-1	-1	-1
-1	-1	1	-1	-1	-1	1	-1	-1
-1	1	-1	-1	-1	-1	-1	1	-1
-1	-1	-1	-1	-1	-1	-1	-1	-1

Local filtering



And at different locations

1	-1	-1
-1	1	-1
-1	-1	1

1	1	-1
1	1	1
-1	1	1

-1	-1	-1	-1	-1	-1	-1	-1	-1
-1	1	-1	-1	-1	-1	-1	1	-1
-1	-1	1	-1	-1	-1	1	-1	-1
-1	-1	-1	1	-1	1	-1	-1	-1
-1	-1	-1	-1	1	-1	-1	-1	-1
-1	-1	-1	1	-1	1	-1	-1	-1
-1	-1	1	-1	-1	-1	1	-1	-1
-1	1	-1	-1	-1	-1	-1	1	-1
-1	-1	-1	-1	-1	-1	-1	-1	-1

Convolution

-1	-1	-1	-1	-1	-1	-1	-1	-1
-1	1	-1	-1	-1	-1	-1	1	-1
-1	-1	1	-1	-1	-1	1	-1	-1
-1	-1	-1	1	-1	1	-1	-1	-1
-1	-1	-1	-1	1	-1	-1	-1	-1
-1	-1	-1	1	-1	1	-1	-1	-1
-1	-1	1	-1	-1	-1	1	-1	-1
-1	1	-1	-1	-1	-1	-1	1	-1
-1	-1	-1	-1	-1	-1	-1	-1	-1



1	-1	-1
-1	1	-1
-1	-1	1

=

0.77	-0.11	0.11	0.33	0.55	-0.11	0.33
-0.11	1.00	-0.11	0.33	-0.11	0.11	-0.11
0.11	-0.11	1.00	-0.33	0.11	-0.11	0.55
0.33	0.33	-0.33	0.55	-0.33	0.33	0.33
0.55	-0.11	0.11	-0.33	1.00	-0.11	0.11
-0.11	0.11	-0.11	0.33	-0.11	1.00	-0.11
0.33	-0.11	0.55	0.33	0.11	-0.11	0.77

This is 2D convolution

- Convolution can also be 1D and 3D
- Convolutions can be used in other application areas
 - Whenever there's predictable correlation over time/space
 - Language, protein or DNA sequences

A convolution exercise

$$\begin{bmatrix} 0 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 \\ 1 & 1 & 1 & 1 \\ 0 & -2 & 0 & -2 \end{bmatrix}$$

Here's our "image"

$$\begin{bmatrix} -\frac{1}{2} & 1 & -\frac{1}{2} \\ -\frac{1}{2} & 1 & -\frac{1}{2} \\ -\frac{1}{2} & 1 & -\frac{1}{2} \end{bmatrix}$$

Here's our "filter"

$$\begin{bmatrix} 0 & 1 & 0 \\ 0 & 1 & 0 \\ 1 & 1 & 1 \end{bmatrix}$$

1

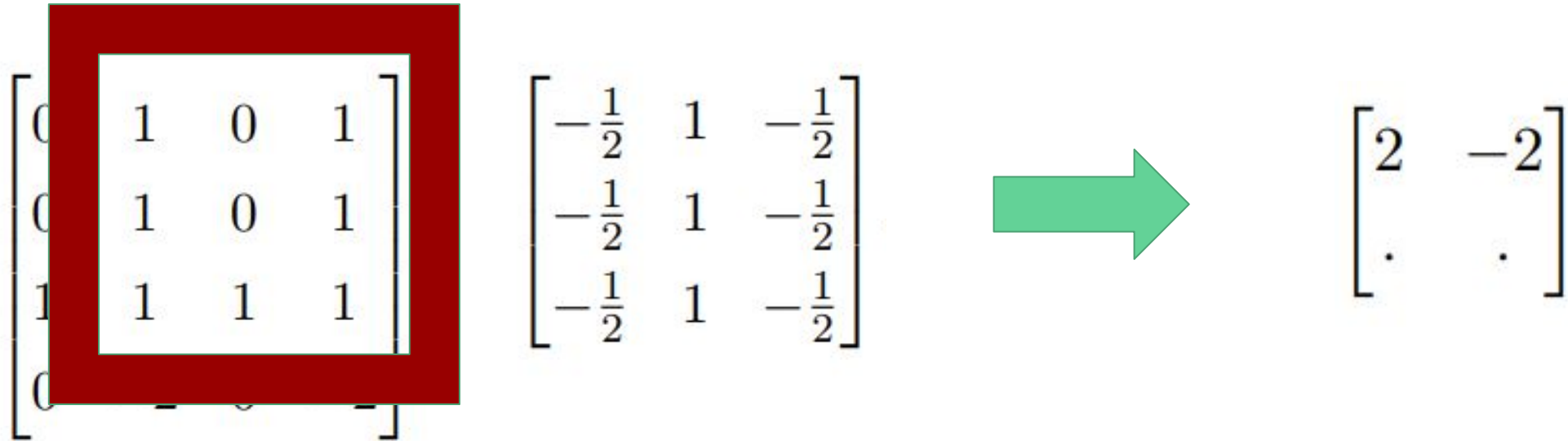
$$\begin{bmatrix} -\frac{1}{2} & 1 & -\frac{1}{2} \\ -\frac{1}{2} & 1 & -\frac{1}{2} \\ -\frac{1}{2} & 1 & -\frac{1}{2} \end{bmatrix}$$



$$\begin{bmatrix} 2 & . \\ . & . \end{bmatrix}$$

$$\begin{aligned} &\left(0 \times \frac{-1}{2}\right) + (1 \times 1) + \left(0 \times \frac{-1}{2}\right) \\ &\left(0 \times \frac{-1}{2}\right) + (1 \times 1) + \left(0 \times \frac{-1}{2}\right) \\ &\left(1 \times \frac{-1}{2}\right) + (1 \times 1) + \left(1 \times \frac{-1}{2}\right) = 2 \end{aligned}$$

A convolution exercise


$$\begin{bmatrix} 0 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 \\ 1 & 1 & 1 & 1 \\ 0 & 1 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 1 \\ 1 & 0 & 1 \\ 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} -\frac{1}{2} & 1 & -\frac{1}{2} \\ -\frac{1}{2} & 1 & -\frac{1}{2} \\ -\frac{1}{2} & 1 & -\frac{1}{2} \end{bmatrix} \rightarrow \begin{bmatrix} 2 & -2 \\ . & . \end{bmatrix}$$

A convolution exercise

$$\begin{bmatrix} 0 & 1 & 0 \\ 1 & 1 & 1 \\ 0 & -2 & 0 \end{bmatrix} \begin{bmatrix} -\frac{1}{2} & 1 & -\frac{1}{2} \\ -\frac{1}{2} & 1 & -\frac{1}{2} \\ -\frac{1}{2} & 1 & -\frac{1}{2} \end{bmatrix} \rightarrow \begin{bmatrix} 2 & -2 \\ -1 & . \end{bmatrix}$$

A convolution exercise

$$\begin{bmatrix} 0 & 1 & 0 & 1 \\ 0 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 0 & -2 & 0 & -2 \end{bmatrix} \begin{bmatrix} -\frac{1}{2} & 1 & -\frac{1}{2} \\ -\frac{1}{2} & 1 & -\frac{1}{2} \\ -\frac{1}{2} & 1 & -\frac{1}{2} \end{bmatrix} \rightarrow \begin{bmatrix} 2 & -2 \\ -1 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 0 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 \\ 1 & 1 & 1 & 1 \\ 0 & -2 & 0 & -2 \end{bmatrix} \quad \begin{bmatrix} -\frac{1}{2} & 1 & -\frac{1}{2} \\ -\frac{1}{2} & 1 & -\frac{1}{2} \\ -\frac{1}{2} & 1 & -\frac{1}{2} \end{bmatrix}$$

**E 2.1-2.2 Do a convolution by hand
and implement as function**

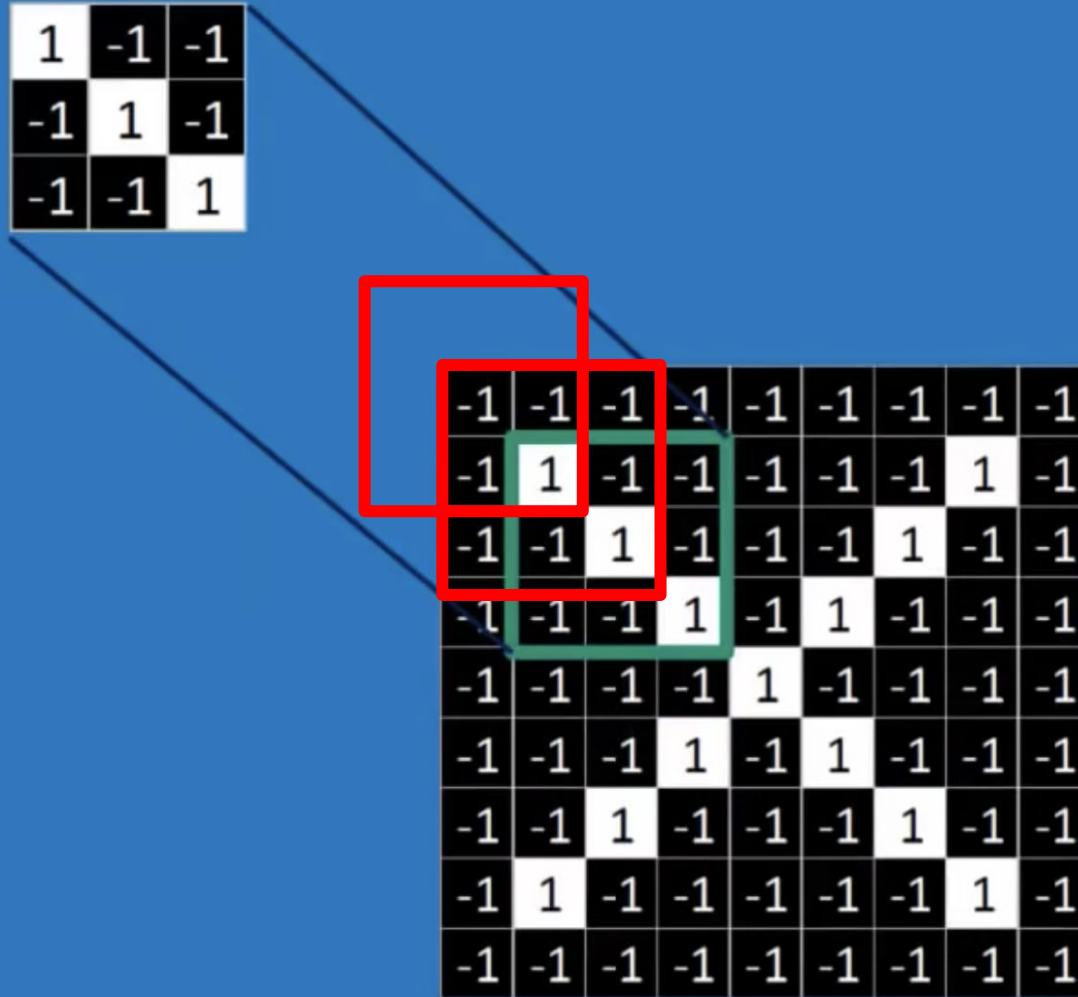
Details about convolution

What about the edges of an image?



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Padding



Padding

-1	-1	-1	-1	-1	-1	-1	-1	-1
-1	1	-1	-1	-1	-1	-1	1	-1
-1	-1	1	-1	-1	-1	1	-1	-1
-1	-1	-1	1	-1	1	-1	-1	-1
-1	-1	-1	-1	1	-1	-1	-1	-1
-1	-1	-1	1	-1	1	-1	-1	-1
-1	-1	1	-1	-1	-1	1	-1	-1
-1	1	-1	-1	-1	-1	-1	1	-1
-1	-1	-1	-1	-1	-1	-1	-1	-1

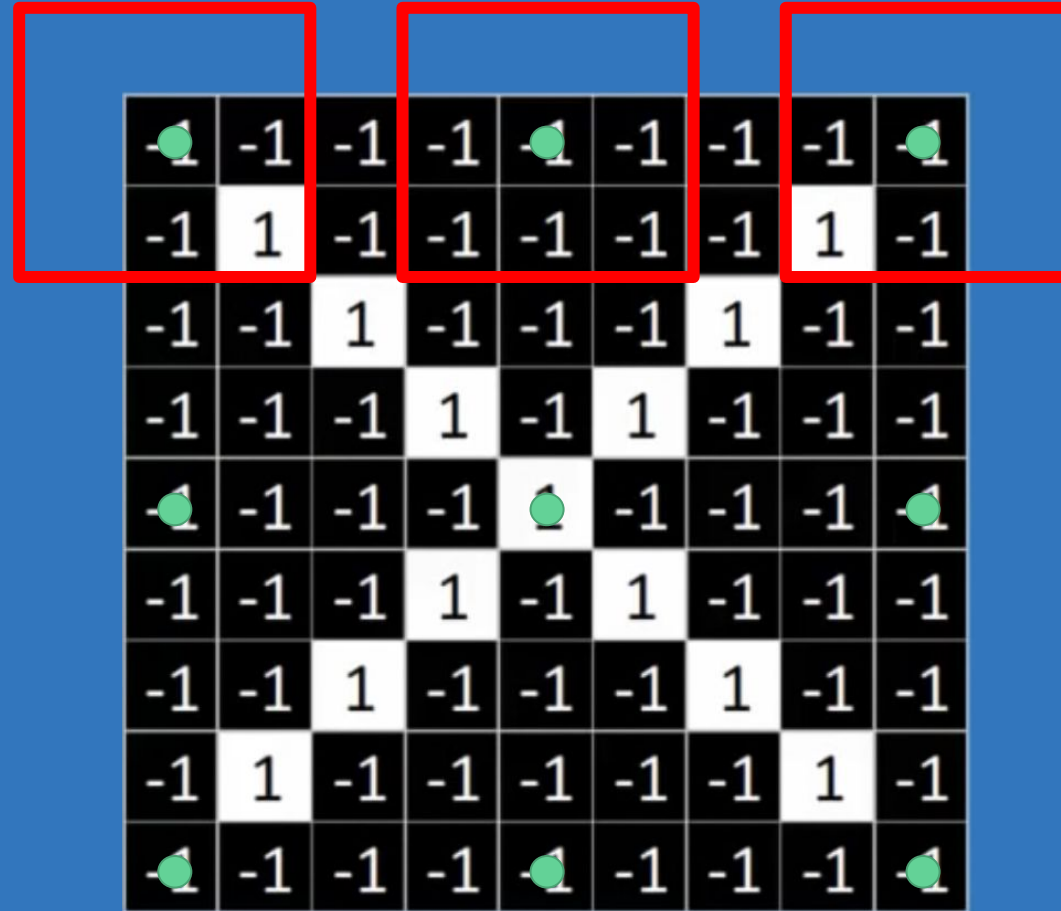
Stride 2



Stride 3



Stride 4



Motivation: conv for edge detection

-1	-1	-1
2	2	2
-1	-1	-1

Horizontal lines

-1	2	-1
-1	2	-1
-1	2	-1

Vertical lines

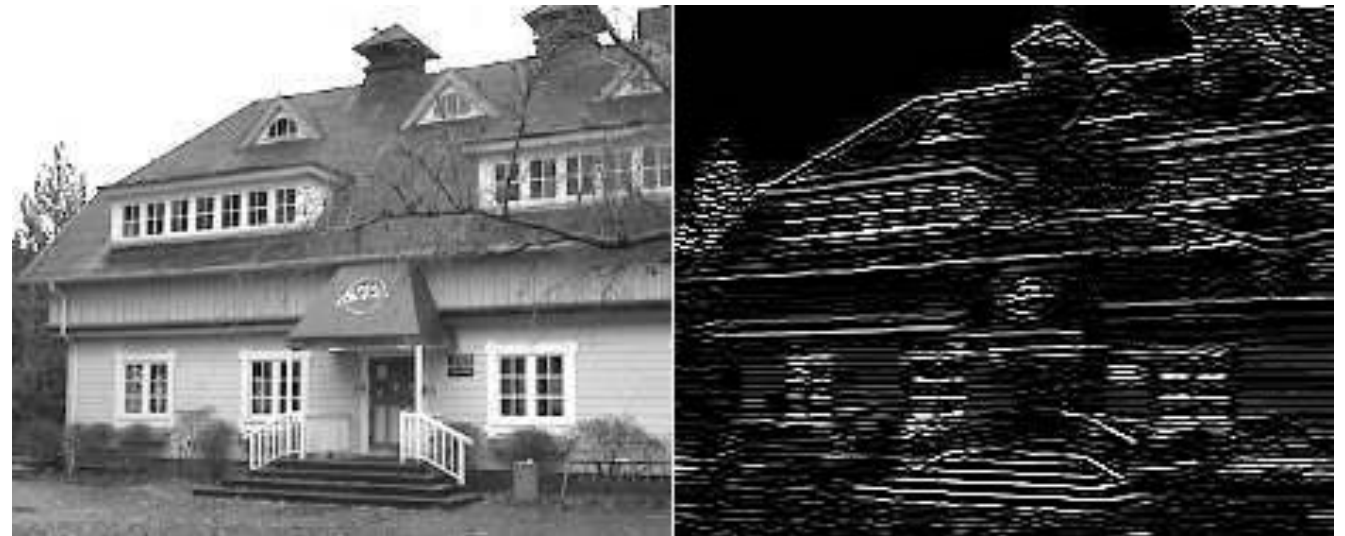
-1	-1	2
-1	2	-1
2	-1	-1

45 degree lines

2	-1	-1
-1	2	-1
-1	-1	2

135 degree lines

Horizontal lines:



Feature detection - edges

Filters give us global translation invariance

Run a filter across an image

How could that be useful for image recognition?

E 2.3-2.4 Convolve a local filter with an image
In what way could this be useful?

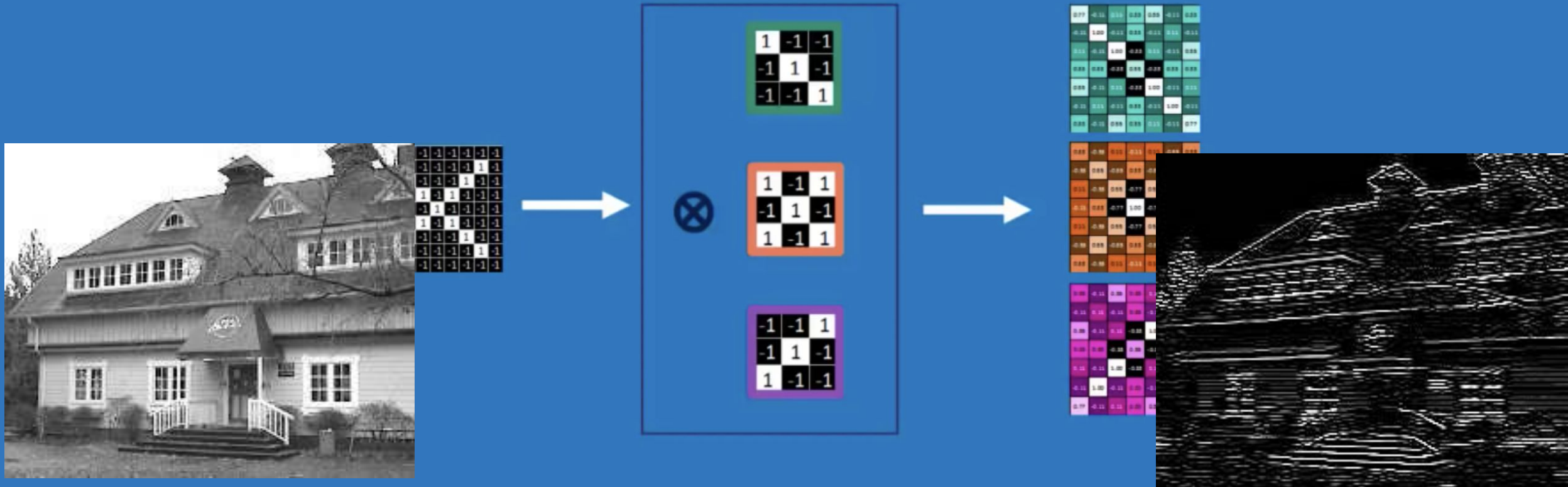
Section 3: Pooling and Subsampling

Multiple Filters and ReLU

Multiple filters

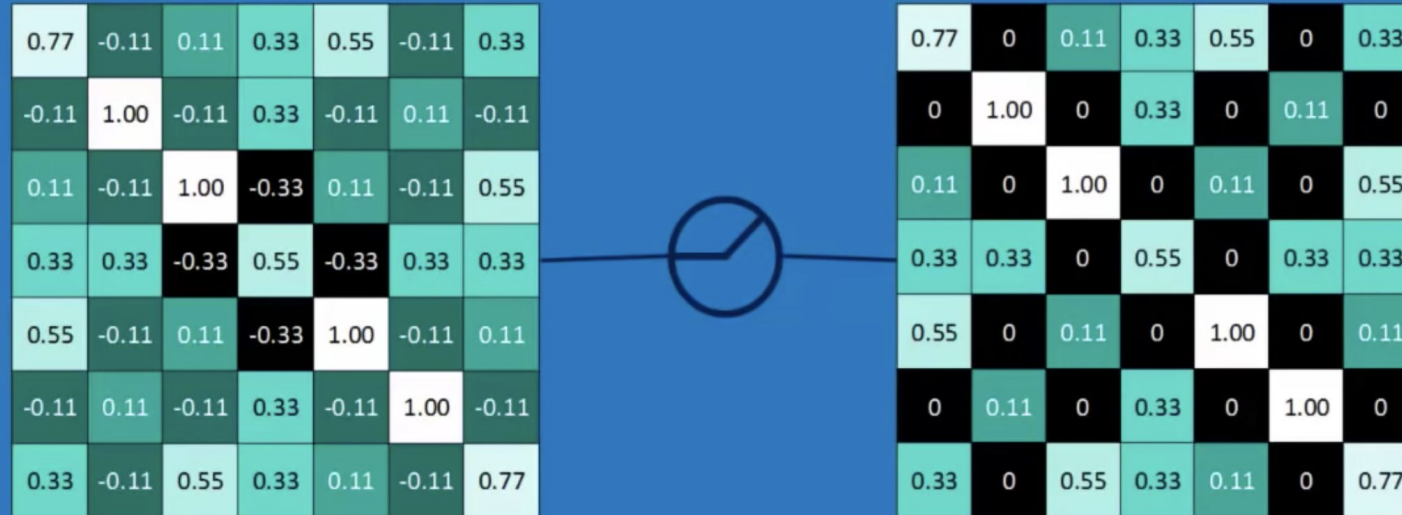


A convolution layer



Potential to add a ReLU

$$\text{ReLU}(x) = \max(0, x)$$



Combining filters

E 3.1-3.2 Experiment with multiple filters and RELU

Pooling



Pooling = Local invariance

- Recall: filters give us global invariance
- Pooling gives local invariance

The need for some invariance

Features may appear in (slightly) different places



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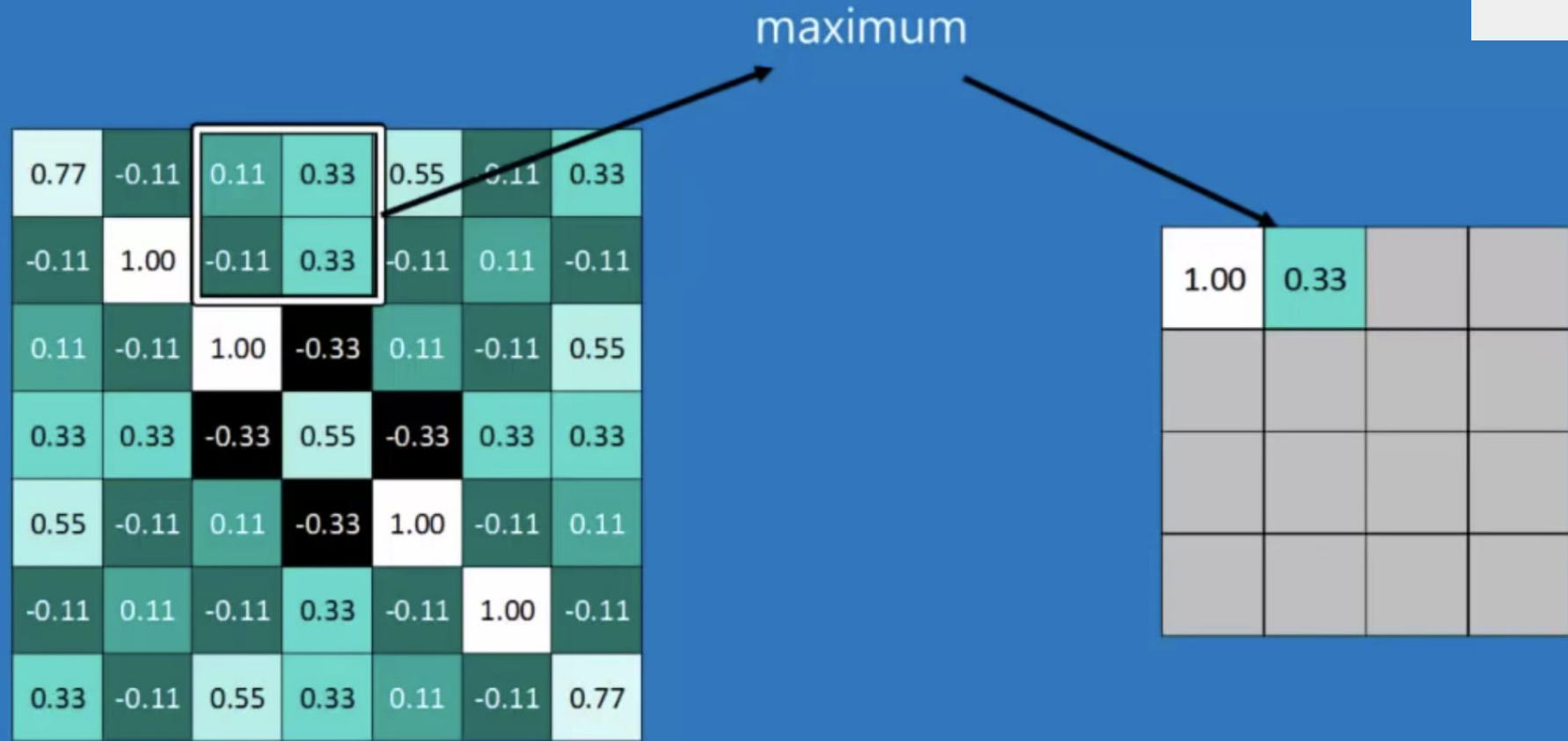
All following (blue) slides from Brandon Rohrer

Max-pooling

2*2, Stride 2



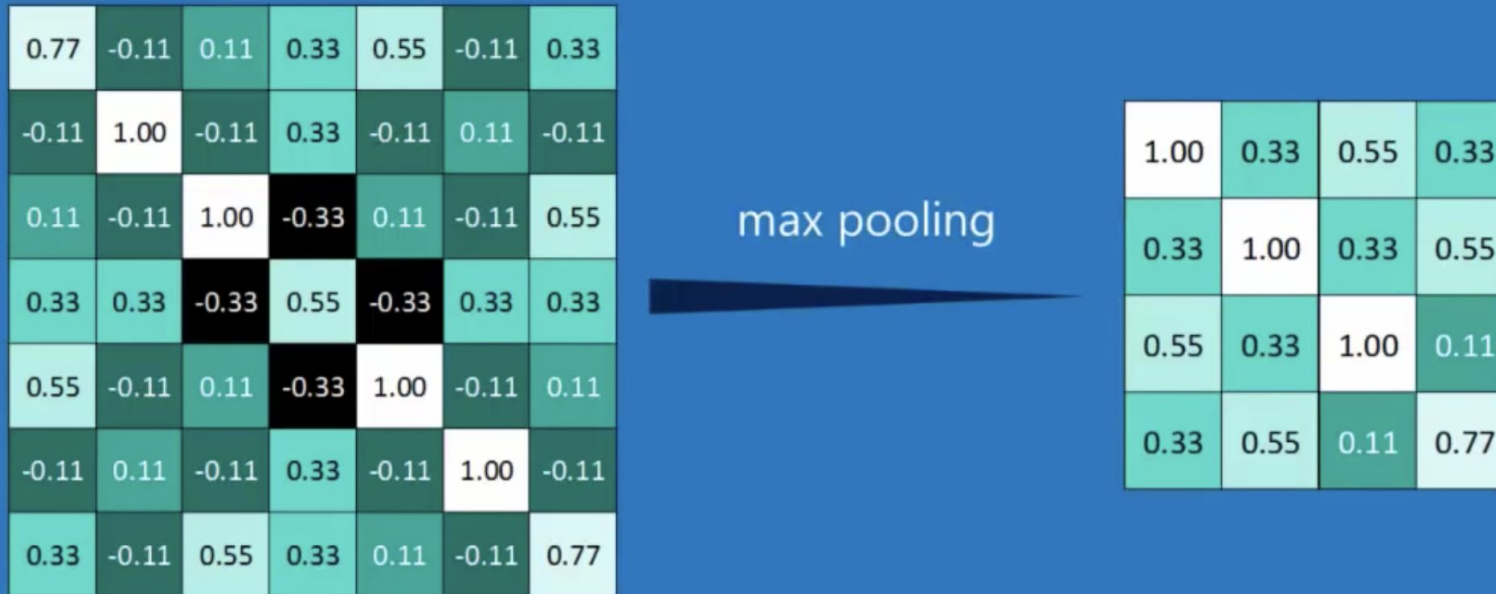
Across space



Again, Padding problem!



And a whole max pooling operation



How many parameters?

Hold up, how does this reduce the # of params?

0.77	-0.11	0.11	0.33	0.55	-0.11	0.33
-0.11	1.00	-0.11	0.33	-0.11	0.11	-0.11
0.11	-0.11	1.00	-0.33	0.11	-0.11	0.55
0.33	0.33	-0.33	0.55	-0.33	0.33	0.33
0.55	-0.11	0.11	-0.33	1.00	-0.11	0.11
-0.11	0.11	-0.11	0.33	-0.11	1.00	-0.11
0.33	-0.11	0.55	0.33	0.11	-0.11	0.77

max pooling

1.00	0.33	0.55	0.33
0.33	1.00	0.33	0.55
0.55	0.33	1.00	0.11
0.33	0.55	0.11	0.77

Next layer has fewer connections!

Bunch of Filters

0.77	-0.11	0.11	0.33	0.55	-0.11	0.33
-0.11	1.00	-0.11	0.33	-0.11	0.11	-0.11
0.11	-0.11	1.00	-0.33	0.11	-0.11	0.55
0.33	0.33	-0.33	0.55	-0.33	0.33	0.33
0.55	-0.11	0.11	-0.33	1.00	-0.11	0.11
-0.11	0.11	-0.11	0.33	-0.11	1.00	-0.11
0.33	-0.11	0.55	0.33	0.11	-0.11	0.77

0.33	-0.55	0.11	-0.11	0.11	-0.55	0.33
-0.55	0.55	-0.55	0.33	-0.55	0.55	-0.11
0.11	-0.55	0.55	-0.77	0.55	-0.55	0.11
-0.11	0.33	-0.77	1.00	-0.77	0.33	-0.11
0.11	-0.55	0.55	-0.77	0.55	-0.55	0.11
-0.55	0.55	-0.55	0.33	-0.55	0.55	-0.11
0.33	-0.55	0.11	-0.11	0.11	-0.55	0.33

0.33	-0.11	0.55	0.33	0.11	-0.11	0.77
-0.11	0.11	-0.11	0.33	-0.11	1.00	-0.11
0.55	-0.11	0.11	-0.33	1.00	-0.11	0.11
0.33	0.33	-0.33	0.55	-0.33	0.33	0.33
0.11	-0.11	1.00	-0.33	0.11	-0.11	0.55
-0.11	1.00	-0.11	0.33	-0.11	0.11	-0.11
0.77	-0.11	0.11	0.33	0.55	-0.11	0.33

And a whole max pooling operation

0.77	-0.11	0.11	0.33	0.55	-0.11	0.33
-0.11	1.00	-0.11	0.33	-0.11	0.11	-0.11
0.11	-0.11	1.00	-0.33	0.11	-0.11	0.55
0.33	0.33	-0.33	0.55	-0.33	0.33	0.33
0.55	-0.11	0.11	-0.33	1.00	-0.11	0.11
-0.11	0.11	-0.11	0.33	-0.11	1.00	-0.11
0.33	-0.11	0.55	0.33	0.11	-0.11	0.77

max pooling

1.00	0.33	0.55	0.33
0.33	1.00	0.33	0.55
0.55	0.33	1.00	0.11
0.33	0.55	0.11	0.77

How many parameters?

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1.00	0.33	0.55	0.33
0.33	1.00	0.33	0.55
0.55	0.33	1.00	0.11
0.33	0.55	0.11	0.77

0.55	0.33	0.55	0.33
0.33	1.00	0.55	0.11
0.55	0.55	0.55	0.11
0.33	0.11	0.11	0.33

0.33	0.55	1.00	0.77
0.55	0.55	1.00	0.33
1.00	1.00	0.11	0.55
0.77	0.33	0.55	0.33

Pooling layers

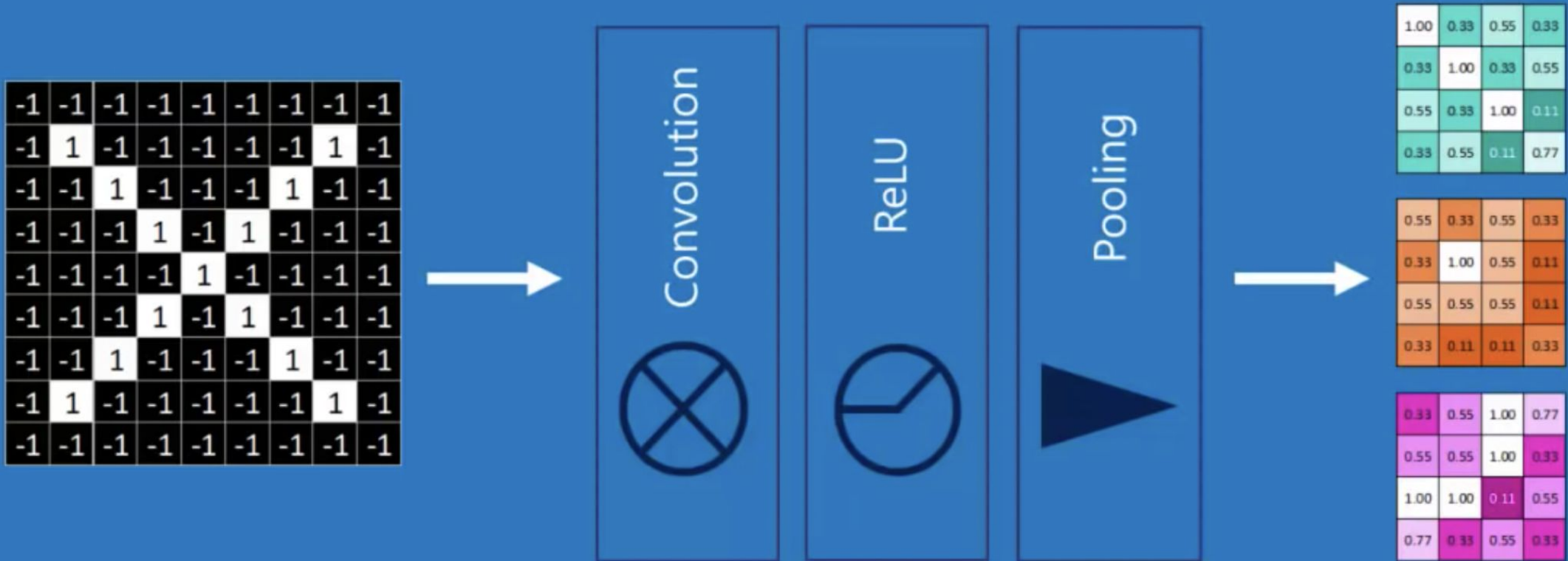
- Want to:
 - Reduce dimensions of data, without additional parameters
 - Introduce some **local** translation invariance
- Pooling operation can be $\max(0, x)$ or $\text{average}(x)$

Dive into pooling 🤿

**E 3.3-3.4 Experiment with and then
implement max pooling**

Section 4: Putting it all together

So far: not much of a hierarchy



Chain it



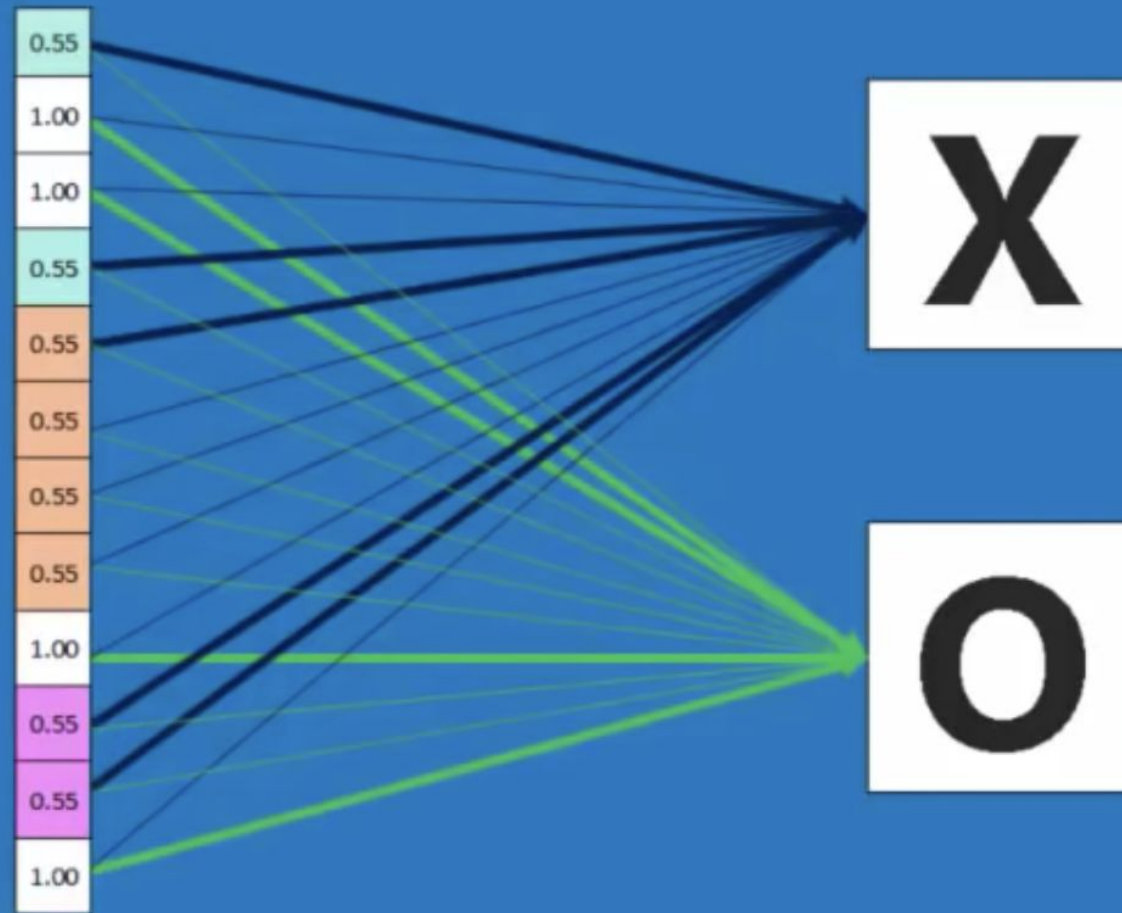
How to transition to fully connected



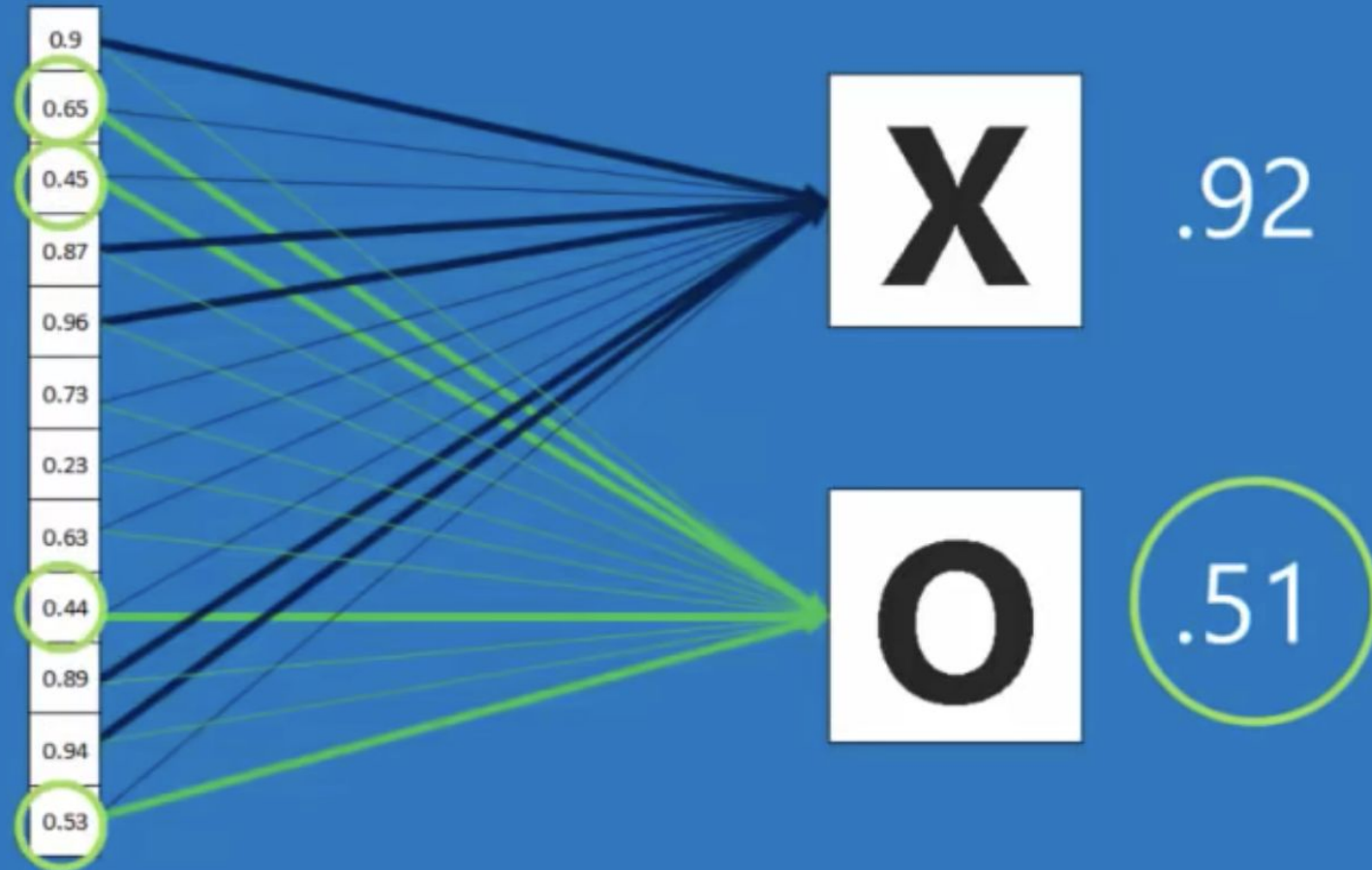
Fully connected read out



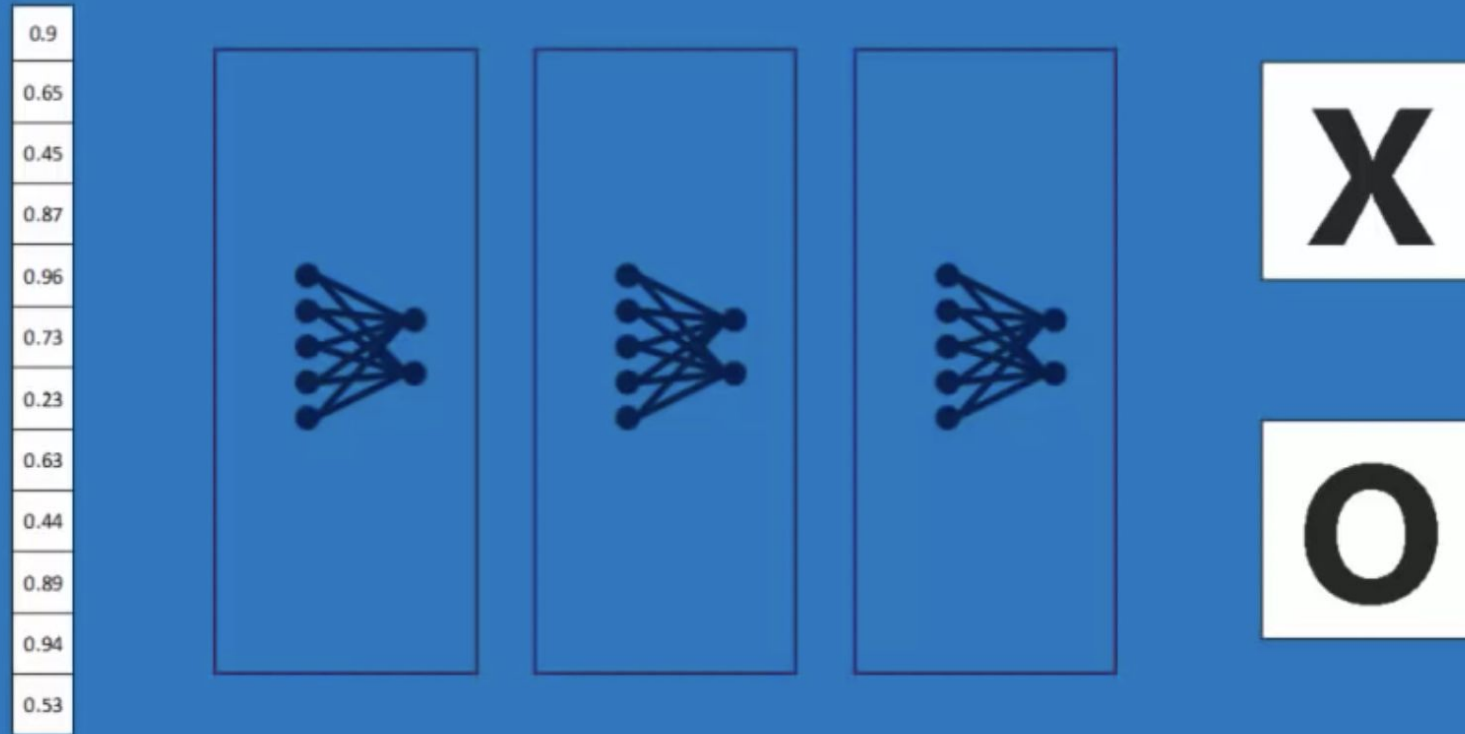
Predict both



Get activations



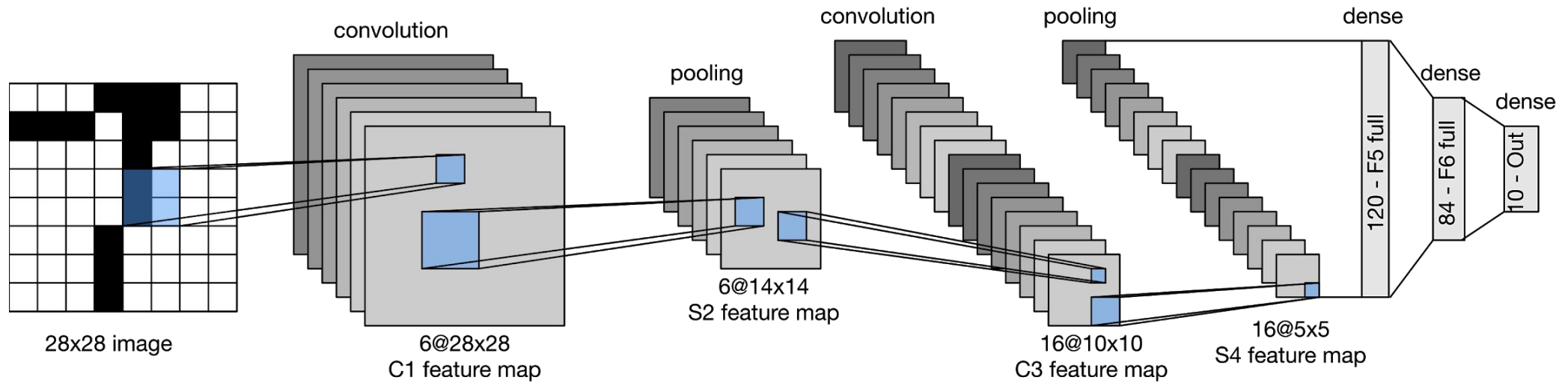
Multiple layers of fully connected



Now stack it all together



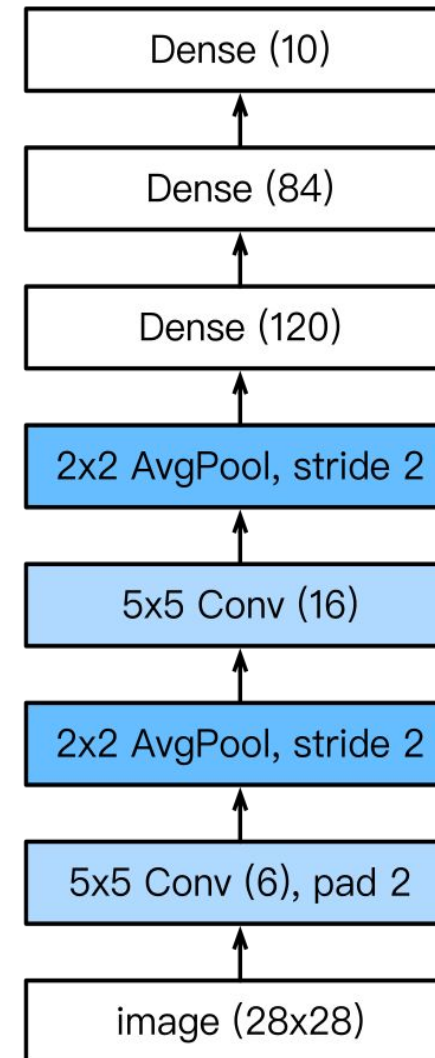
Putting things together



Input → (Conv → ReLU → Pooling) → ... → Fully connected

From 'Dive into deep learning'

Another way of visualizing the same network

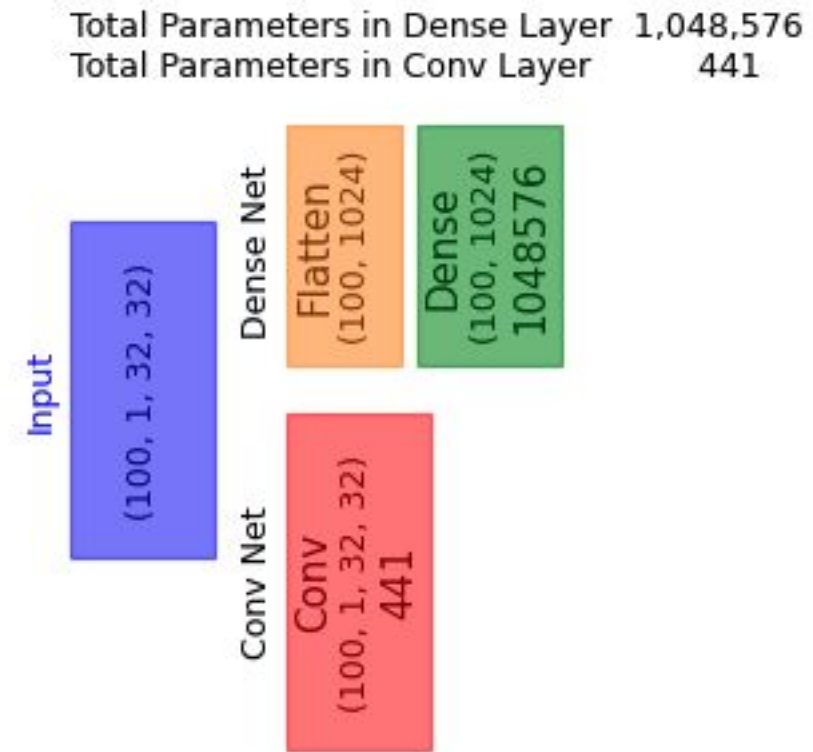


Let us calculate that: Convolution and pooling

- 1×1 image with 2 padding is 5×5
- 5×5 image, 5×5 filter \Rightarrow 1 output
- 300×400 image with 2 padding is 304×404
- 304×404 image, 5×5 filter $\Rightarrow 300 \times 400$
- Maxpool 2×2 pooling window 300×400 , stride 2 $= 150 \times 200$

Dense vs conv layers

- Now you'll compare the number of parameters in networks that use dense (fully connected) vs convolutional layers



Understand how hyperparameters
affect the number of parameters

**E 4.1 Explore how NN layers fit together, and
how the architecture changes the # of params**

Let's implement a CNN!

Make a network

Now we're going to chain together the components of CNNs that we've been talking about.

- Convolution
- Convolution
- Pool Layer
 - Flatten the output here!
- Fully Connected Layer
- Fully Connected layer

Let's train!

- Now we are going to put everything together and train

E 4.2 Train a CNN!

Section 5: Writing our own training loop

Dive into the data



The Data

- Fashion mnist

0 T-shirt/top

1 Trouser

2 Pullover

3 Dress

4 Coat

5 Sandal

6 Shirt

7 Sneaker

8 Bag

9 Ankle boot



Before training, let us really understand the dataset

Visualize the dataset

Understand its properties

How hard do you think the task will be?

Which classes are likely the most confusable?

E 5.1 Get a feeling for the dataset

The training loop



Now, we want you to design the training loop

In the last section you chained together the steps of a network.

Now, let's construct our own training loop, to really understand what's happening

What goes into a training loop

- Choose the correct criterion
 - We will use cross entropy

$$H(p, q) = - \sum_{x \in X} p(x) \log(q(x))$$

What goes into a training loop

- Code up the training part
 - loss
 - calculating gradients
 - stepping forward
- Keep a track of the running loss i.e for each epoch we want to know the average loss of the batches.
- We have already done the same for accuracy for you.

What goes into a training loop

- This exercise requires you to know the names of some important functions
- This is one exercise where it would be **ok to look at the solution if you get stuck!** As you're starting out, you might not know the names of particular functions. Don't worry about that! Just make sure you understand what is going on in the solution!

E 5.2 Build your training loop. Don't rush, take your time!

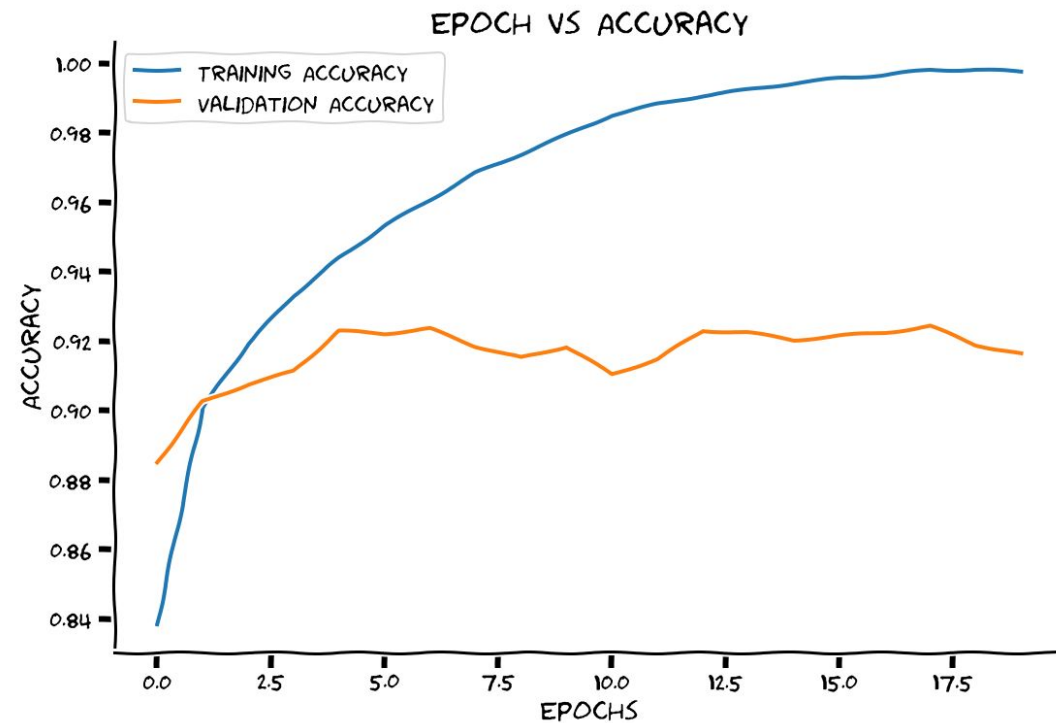
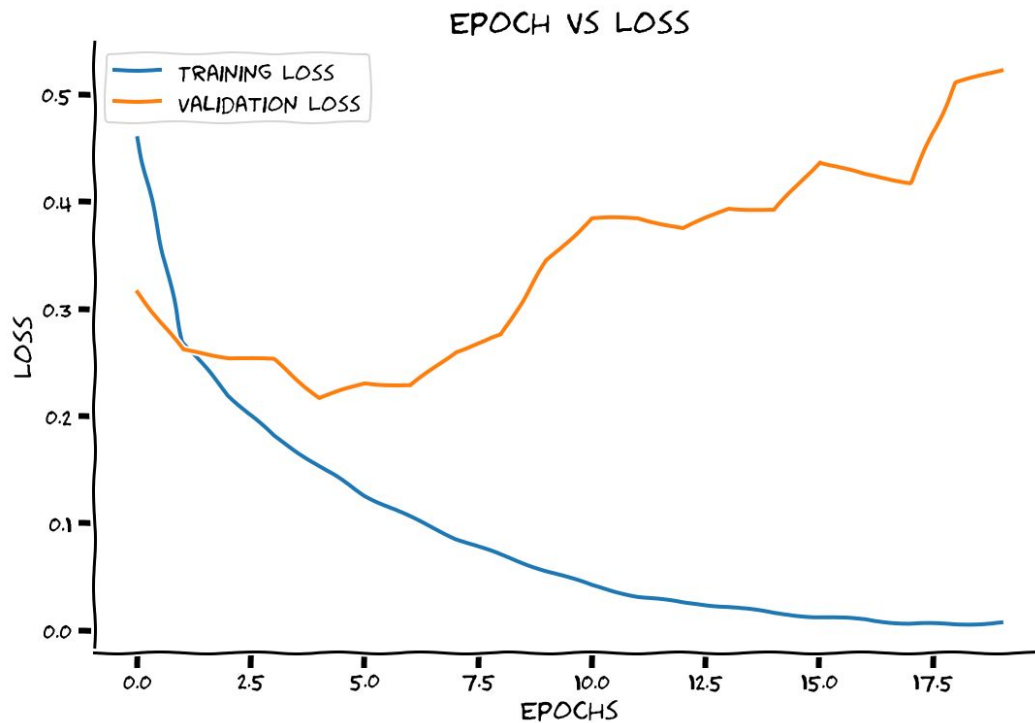
Section 6: Overfitting

Dropout



Overfitting

In the model you just build there were strong signs of overfitting.



What can we do? Dropout

Intuition: no one neuron should be *too* important

Just like the brain, there should be redundancy in connections

Dropout: randomly set some of the hidden activations to 0

Parameter: % of neurons to set to 0

What can we do? Dropout

Add drop-out

```
self.dropout1 = nn.Dropout(0.25)
```

```
x = self.dropout1(x)
```

Where do you have to do this?

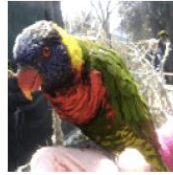
Check how much dropout helps

**E 6.1 Add dropout. Retrain.
What happens to train and test performance?**

Data augmentation

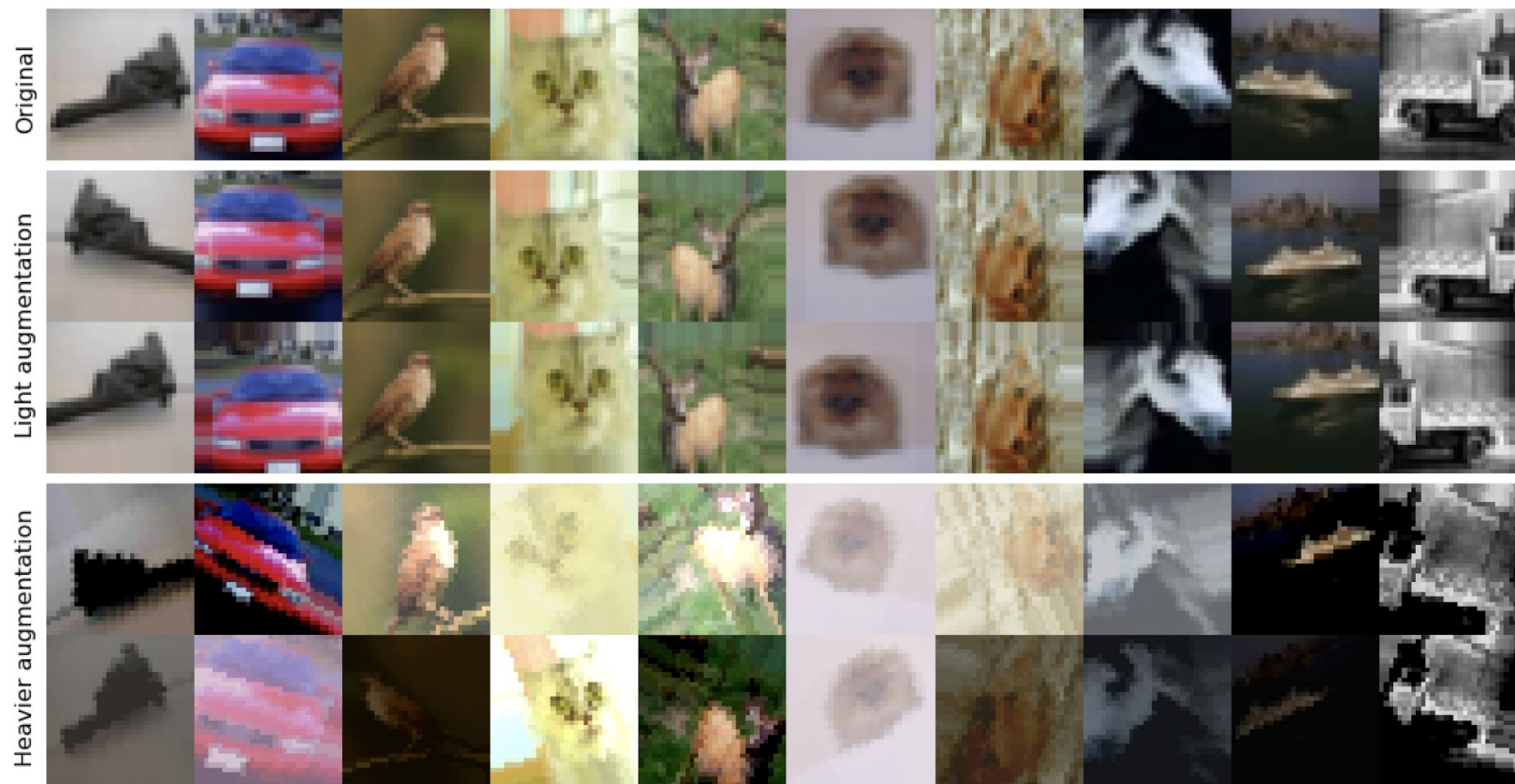


What can we do? Data augmentation



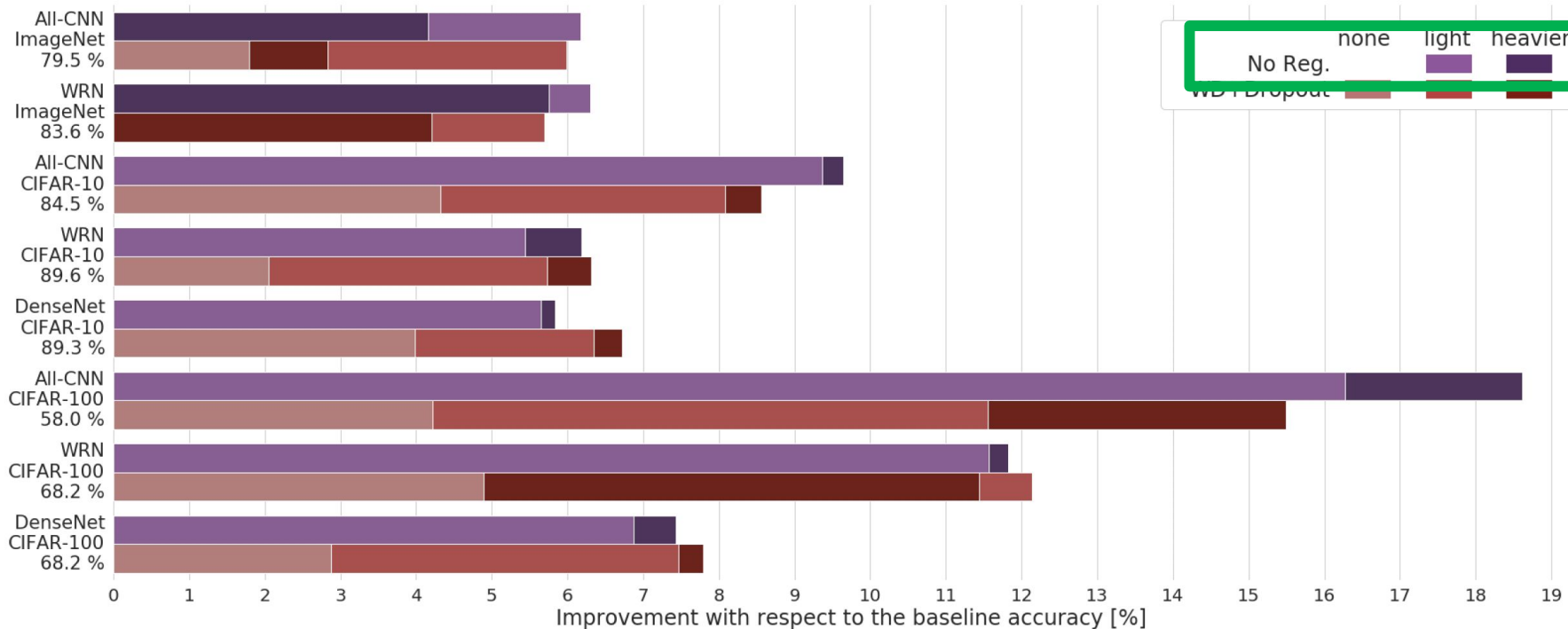
source: Hernandez Garcia Thesis

Different strengths of DA



source: Hernandez Garcia, arxiv

Data augmentation is often more important than direct regularization



source: Hernandez Garcia, arxiv

Data augmentation

Now edit the training loop.

We want:

- Resize

- Flip

- Rotations (< 20 degrees)

- Color jitter

E 6.2 How much does data augmentation help?