



[microresearch]

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Quadratic convergence of a multivalued series (S_+)

Open Mathematics Collaboration^{*†}

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Abstract

We use the Infinity Theorem to find two possible values for S_+ .

keywords: multivalued series, infinity theorem

Introduction

1. In this paper, we use the **Infinity Theorem** [1].

The S_+ series

2. $S_+ = 1 + 1 + 1 + 1 + 1 + \dots$
3. $S_+ = -\frac{(2n-1)}{2} = -n + \frac{1}{2}$ for $n \in \mathbb{N} = \{1, 2, 3, \dots\} \cup \{0\}$.

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4. Summing over (2) and (3),

$$\sum_{n=1}^{+\infty} S_+ = \sum_{n=1}^{+\infty} \left(-n + \frac{1}{2}\right).$$

5.

$$S_+ \sum_{n=1}^{+\infty} 1 = - \sum_{n=1}^{+\infty} n + \frac{1}{2} \sum_{n=1}^{+\infty} 1$$

6. From the reference [2],

$$S = \sum_{n=1}^{+\infty} n = \{-1/12, \infty\}$$

7. Using (2), and the finite result of (6),

$$S_+^2 = \frac{1}{12} + \frac{1}{2} S_+.$$

8.

$$S_+^2 - \frac{1}{2} S_+ - \frac{1}{12} = 0$$

9.

$$S_+ = \frac{1}{4} \pm \frac{\sqrt{\frac{7}{3}}}{4}$$

Final Remarks

10.

$$S_+ = \left\{ -\frac{(2n-1)}{2}, \frac{1}{4} \pm \frac{\sqrt{\frac{7}{3}}}{4}, \pm\infty : n \in \mathbb{N} \cup \{0\} \right\}$$

Open Invitation

*Review, add content, and **co-author** this article [3, 4].*

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Ethical conduct of research

This original work was pre-registered under the OSF Preprints [5], please cite it accordingly [6]. This will ensure that researches are conducted with integrity and intellectual honesty at all times and by all means.

References

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