

# Relating unsupervised word segmentation to reported vocabulary acquisition

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## Abstract

A range of computational approaches have been used to model the discovery of word forms from continuous speech by infants. Typically, these algorithms are evaluated with respect to the ideal 'gold standard' word segmentation and lexicon. These metrics assess how well an algorithm matches the adult state, but may not reflect the intermediate states of the child's lexical development. We set up a new evaluation method based on the correlation between word frequency counts derived from the application of an algorithm onto a corpus of child-directed speech, and the proportion of infants knowing the words according to parental reports. We evaluate a representative set of 4 algorithms, applied to transcriptions of the Brent corpus, which have been phonologized using either phonemes or syllables as basic units. Results show remarkable variation in the extent to which these 8 algorithm-unit combinations predicted infant vocabulary, with some of these predictions surpassing those derived from the adult gold standard segmentation. We argue that infant vocabulary prediction provides a useful complement to traditional evaluation; for example, the best predictor model was also one of the worst in terms of segmentation score, and there was no clear relationship between token or boundary F-score and vocabulary prediction.

**Index Terms:** language acquisition, word segmentation, infant vocabulary, speech units, computational modeling.

## 1. Introduction

Segmenting – identifying words in fluent speech – is a key step in language acquisition and especially in lexical development. However, the absence of systematic silences between words in continuous speech makes this task a particularly difficult one, especially early in development where other key components of language (phonology, morphology, syntax, etc.) are not yet fully known to infants. Thus, a key research question becomes: how do infants get word segmentation off the ground? Two strands of research have addressed this issue: one using laboratory experiments in infants, [1, 2, 3, 4, 5], and another one using computational modeling [6]. Here, we focus on the latter approach with a view to comparing the *adequacy* of computational systems as models of infant word segmentation.

Most of the computational work on word segmentation have taken the view that a good model, when fed with enough data, will reach the optimal performance of a human adult. This is usually quantified by defining as 'gold standard' the segmentation corresponding to the blank spaces between words in the orthographic transcription of the input data. Provided this ideal segmentation, objective metrics can be defined, typically, type, token and boundary precision, recall and f-scores (see below). While this gold standard can be argued to represent the adult state, it most certainly does not capture intermediate states of knowledge in infants. Indeed, there is now clear evidence that

infants make segmentation errors, in that they extract from continuous speech a "proto-lexicon" containing many items that adults would view as non-words [4, 7].

A number of alternatives to gold standard metrics have been discussed. One is that the proposed model should be *cognitively plausible* given what is known about infant cognition (e.g., [8]). Another is that models should reproduce documented patterns of successes and errors found in development (e.g., [9, 10]). One limitation of such proposals is that it is difficult to rank the relative merit of algorithms on these dimensions because there is no agreed upon list of criteria or patterns of results that could be turned into an objective metric. For instance, [8] argues that infants focus on segmenting rather than on storing potential words, whereas [11] argues that it is more cognitively plausible that infants try to learn word-like units rather than learning segmentation strategies.

We propose to use one source of evidence that has not yet been exploited for this purpose, and which may provide a way to determine the relative merit of algorithmic proposals in a quantifiable way: parental reports of word comprehension. These reports are typically collected using the MacArthur Communicative Development Inventory (CDI for short [12]), a standardized questionnaire containing more than 400 items. The CDI has been translated in several language and has been collected in a large quantity of families in the WordBank repository [13]. Recently, CDI comprehension data have been used to look at the earliest words that infants acquire and age of acquisition for each of these words has been estimated across several languages. Input-related factors – frequency, mean length utterance – and conceptual factors – concreteness, babiness : measure of association with infancy – have been found to predict vocabulary age of acquisition [14]. Of course, parental report may not reflect the true state of the infant's comprehension lexicon. The ideal source of data would use experiments that bypass the parent and measure lexical knowledge in the child, like word-to-meaning paradigms [15, 16] or segmentation experiments [1, 17]. Yet, these studies are limited to a small number of preselected test items and are difficult to deploy across a large number of infants. This is why, despite its many drawbacks, parental reports remain a good proxy of word knowledge in infants.

In this paper, we introduce a new measure derived from the correlation between the frequency of occurrence of a word form in the output of an algorithm (applied onto a large corpus of transcribed child-directed speech), on the one hand and the proportion of infant's reported comprehending that word form on the other. We evaluate 8 algorithm-unit combinations, as follows. The corpus was represented using either the phoneme or the syllable as basic unit. The algorithms were drawn from two main classes of algorithms: one class tracks *local statistical cues* at a sub-lexical level in order to find where to segment speech, the other builds a *word form lexicon* to represent or cap-

ture the corpus. Both classes make the assumption that phrases boundaries are known, and contain distributional information useful for segmenting words [18]. We use two algorithms from each class, introduced in more detail in Section 2.

## 2. Methods

### 2.1. Data

We used as input to the word segmentation algorithms the Brent-Siskind corpus [19]. This corpus is the longest one in the CHILDES repository [20], containing orthographic transcriptions for more than 100 hours of recordings from 16 American English-speaking mother-infant pairs. Table 1 gives some details about the corpus. For evaluating word segmentation al-

Table 1: *Descriptive statistics of the Brent-Siskind corpus — NU: number of utterances, AUL: average utterance length, TTR: token-type ratio, AWL-ph: average word length in number of phonemes, AWL-syl: average word length in number of syllables, infants’ age range in months*

NU	AUL	TTR	AWL-ph	AWL-syl	age
113363	3.59	60,4	3.06	1.23	9-15

gorithms on infant reported lexicon, we used American English language data available on the WordBank repository [13], corresponding to the “Words and Gestures” form of the CDI. Most of these items are nouns (e.g., *ball*) but there are also other classes, such as verbs (*watch*), function words (*you*), adjectives (*big*) and even onomatopoeia (*baa*). There were different numbers of parental reports at different ages, ranging from 66 to 761. In order to maximize our chances of having sufficient sensitivity, we focus on the 761 parental reports for infants aged 13 months.

### 2.2. Word segmentation algorithms

The first model using local statistical cues is the **Diphone-Based Segmentation** (DiBS) algorithm [8], previously studied by [21, 22], based on phonotactics properties, which keeps in memory the frequency of two phones occurring together and decides to place a boundary between them by computing Bayes’ Theorem. To do that, the model has several assumptions: the learner knows the phonetics categories, is able to detect utterance boundaries, assumes phonological independence across word boundaries, tracks context-free distribution of diphones and knows the relative frequency of word forms already learned. All these assumptions are discussed in [8] from a psycholinguistic point of view indicating why it is plausible that infants might act as a DiBS learner when starting segmenting speech. The only free parameter of the model is the context-free probability of a word boundary and is determined by average word length and number of words per utterance. This setting is quite controversial since the model is partly supervised – word boundaries are given for a subset of the corpus to fix the context-free probability of a word boundary – whereas the infant segmentation is not. DiBS was trained on the first 200 utterances estimating the context-free probability of a word boundary.

Another local statistical model is based on tracking **transitional probabilities (TPs) over syllables** which posits a boundary between two syllables if its co-occurrence probability is locally lowest [1] (relative threshold) or is lower than an absolute threshold usually computed by taking the averaged value

of syllables pairs. As it is highly improbable that infants compute this absolute threshold, we chose the relative one, which also implies that monosyllabic words can only be found at the utterance edge [23]. We chose the forward dependency measure over the backward and the mutual information ones since it has been shown that it performs better on English. A possible explanation would be that forward TP gives more information in Subject-Verb-Object languages [24]. Compared to DiBS, TPs demands a larger memory as the number of all possible syllables encountered are much greater than the number of all possible phones. In that sense, TPs seem less cognitively plausible. However, a number of experimental studies using artificial languages suggested that infants can assemble high statistical sequences of syllables and bound them with lower statistical sequences [1] and therefore can rely on TPs over syllables [2].

The lexicon-based strategy needs learners to have larger memory and wider knowledge on its language than local statistical strategies. The **PUDDLE** (Phonotactics from Utterances Determine Distributional Lexical Elements) algorithm developed by [9] and based on the PARSER model [25], builds incrementally a lexicon by using information on utterance boundaries and by deducing phonotactics constraints. More precisely, each time a sequence of phonemes is encountered, if a match with a word in the proto-lexicon is found and if phonotactics constraints are respected, then the chunk of phonemes is added to the proto-lexicon, the beginning and ending phonemes pairs are added respectively to a list made of previously encountered beginning and ending phonemes pairs. Hence, the phonotactics constraints are the following: when a match is found, the previous pair of phonemes must belong to the list of ending phonemes pairs and the following pair of phonemes must belong to the list of beginning pair. These constraints avoid over-segmentation to the level of phonemes and make the proto-lexicon closer to the real lexicon of the corpus. Moreover, the model promotes frequent words by counting the occurrences of words added in the proto-lexicon and then by sorting the list of these words by frequency. For PUDDLE, since time (number of mathematics operations) and space (memory needed) requirements were heavy in the original awk script, we made a version in python using the collection modules, resulting in a 120-fold decrease in computation time and optimized space use.

The last algorithm used is the **unigram Adaptor Grammar (AGu)** [26], [27] which models an optimal learner, i.e a learner having an infinite memory and a batch process, looking at the whole corpus before segmenting. The framework consists of two modules: a lexicon generator and an adaptor. The first one generates a lexicon of items that are likely to be found in the corpus and the second assigns items frequencies. Importantly, the unigram AG assumes that lexicon items are generated independently from each others and that the stochastic process is chosen so that items’ frequencies follow a power-law distribution as it has been found in natural language.

### 2.3. Data processing and algorithm evaluation

The scripts used for all processing steps are available on the second author’s github: <https://github.com/alecristia/CDSwordSeg>. The corpus processing steps consisted of cleaning up annotations and converting orthography into surface phonological forms. The latter was achieved with the American English voice of the Festival Text-to-Speech system [28], which provides syllable boundaries.

A few changes were necessary when changing the unit of input representation from the original one. For AGu – syl-

Evaluation of the final output of each algorithm for each input representation was assessed by using the traditional token F-score, i.e., the harmonic mean of precision (ratio of true positives to the number of segmented items by the algorithm) and recall (ratio of true positives to the number of segmented items by the reference). Type and boundary F-scores were also used for comparison purposes. Since PUDDLE is incremental, we assessed its performance by a 5-fold cross-validation with the hope of measuring performance at asymptote. Finally, for AGu, 8 parses of 2000 iterations – of which the first 100 were removed before parse reduction, were used. Because this algorithm is not deterministic (unlike all other algorithms), the process was repeated five times and averaged.

In our linear regression, the predictor was the logarithm of the number of times a word was correctly segmented; the outcome was the proportion of infants reported to understand that word. We checked that the residuals were normally distributed and had homogeneous variance.

Table 2 also gives the detail segmentation F-scores – lexicon, token and boundary F-scores – for each algorithm. At first glance, the best performances are: AGu with phoneme when evaluated with Type F-score, PUDDLE with syllable when evaluated on Token F-score and Boundary F-score, and TPs with syllable when evaluated on its correlation with the infant reported vocabulary. This is quite surprising and this leads us to think that the traditional F-scores metrics are not correlated with the coefficient of determination  $R^2$  of the regression predicting

With regard to the effect of the unit of representation, TPs, DiBS and PUDDLE show surprisingly better segmentation performance with their non-initial input: phoneme for TPs, syllable for DiBS and for PUDDLE. AGu, on the contrary, is clearly better with phonemes, but it might be due to the low complexity of the grammar itself: taking into account one or two level of collocation – groups of words that tend to appear together – might favor the syllabic unit over the phoneme. In fact, conclusions must be drawn carefully as the unit presented introduces some bias in the segmentation. Indeed, since phonemes are thrice as common as syllables in the corpus (see Table 1), the number of possible boundaries are much bigger with phonemes than with syllables, hence the boundary precision must be lower for algorithms using phonemes than syllables, which is actually found in Table 2. Nonetheless, Figure 2 first confirms that  $R^2$  and the token F-score don't have a linear relationship and second, indicates that sub-lexical algorithms (DiBS and TPs) are more affected by the change of unit than lexical-based algorithms.

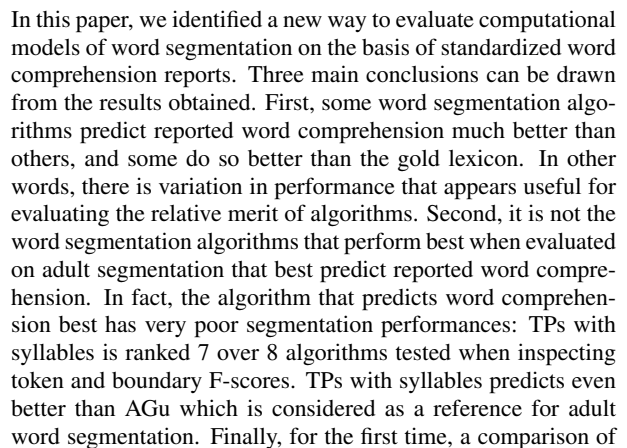


Table 2: *F-score, Precision and Recall for Type, Token and Boundary statistics of four word segmentation algorithms on the Brent-Siskind corpus as a function of input units,  $R^2$  prediction score of 13 month-old-infants' vocabulary and standard error SE. Boldface indicates the best statistics on each column.*

Algorithm	Unit Input	Type			Token			Boundary			Regression	
		F-score (rank)	Prec.	Rec.	F-score (rank)	Prec.	Rec.	F-score (rank)	Prec.	Rec.	$R^2$ (rank)	SE
TPs	Syllable	0.188 (6)	0.111	0.607	0.361 (7)	0.476	0.291	0.602 (7)	0.947	0.441	<b>0.186</b> (1)	0.0076
	Phoneme	0.166 (7)	0.124	0.253	0.468 (5)	0.432	0.512	0.657 (5)	0.590	0.742	0.034 (7)	0.0066
DiBS	Syllable	0.417 (2)	0.523	0.347	0.602 (4)	0.570	0.638	0.801 (4)	0.745	0.866	0.093 (4)	0.0084
	Phoneme	0.057 (8)	0.035	0.159	0.236 (8)	0.234	0.240	0.467 (8)	0.459	0.475	0.029 (8)	0.0119
PUDDLE	Syllable	0.315 (5)	0.234	0.479	<b>0.811</b> (1)	<b>0.821</b>	<b>0.802</b>	<b>0.903</b> (1)	0.918	<b>0.889</b>	0.046 (6)	0.0066
	Phoneme	0.380 (3)	0.306	0.501	0.706 (3)	0.682	0.733	0.820 (3)	0.782	0.862	0.067 (5)	0.0065
AGu	Syllable	0.340 (4)	0.232	<b>0.634</b>	0.408 (6)	0.532	0.331	0.637 (6)	<b>0.985</b>	0.471	0.148 (2)	0.0084
	Phoneme	<b>0.517</b> (1)	<b>0.585</b>	0.464	0.782 (2)	0.787	0.777	0.889 (2)	0.897	0.881	0.135 (3)	0.0070
Adult gold standard		—	—	—	—	—	—	—	—	—	0.118	0.0065

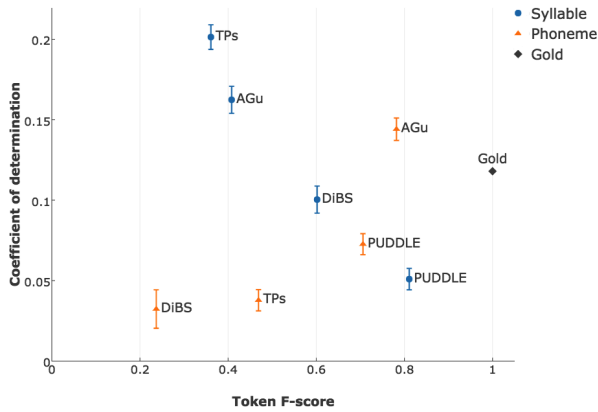


Figure 2: *Token F-score plotted against the coefficient of linear regression predicting infant lexicon from word segmentation algorithms' true positives. Error bars are twice the standard error, estimate of the standard deviation.*

the unit of input representation has been achieved and indicates that there is no predominance of a unit over another on every F-score and on correlation with the infant reported vocabulary. This comparison also exhibits the fact that some algorithms, DiBS and TPs, are more sensitive to a change of unit than others and it appears that those ones are based on local statistical regularities.

It is noteworthy that the algorithm with the highest predictive value regarding infants' vocabulary is also the algorithm which received the most support in an experimental setup using artificial languages made up of strings of syllables [1, 7]. It is also noteworthy that this algorithm completely fails when its input is specified in terms of phonemes, not syllables [30]. However, before jumping to conclusions and claiming that our analysis provides *proof* that TPs on syllables is *the* algorithm used by infants, two caveats are in order. First, it would be important to replicate this study with other corpora and other languages in order to assess the robustness and generality of our finding. Second and more importantly, our analysis only provides evidence for half of the predictions of the algorithm. Indeed, with the CDI, we can only test the predicted correct segmentations, not the errors. All of the 8 algorithms make systematic segmentation errors which can be considered as predictions regarding the content of the early infant lexicon. In order to prove that an algorithm is truly used by infants, one

would therefore also need to check that infants also make the erroneous segmentations predicted by the algorithm, using, for instance, the paradigm provided in [7].

Conducting large scale experimental work in infants is costly. Fortunately, our approach could still be used to as a first pass to quickly test a large set of algorithms on their correct predictions before it becomes worth setting up the experiments on their incorrect ones. Here, we only scratched the surface in that many other segmentation algorithms have been proposed, some sublexical [31], some lexical [32, 33] and others using a combination of both strategies [34, 35]. It would be interesting to add to the mix algorithms that work from raw speech instead of phonetic transcriptions [36, 37, 38].

Finally, our findings provide a new angle to understand the strategy that infants may be using to kick-start their lexical segmentation: The fact that a very rudimentary algorithm like TP outperforms the gold segmentation in predicting infant's vocabulary indicates that infants may not use, at least initially, an optimal segmentation strategy, but rather a simple heuristics that gives them a first proto-lexicon, to be cleaned up at a later stage. One could therefore get a hint at such a heuristics by studying the way in which the initial vocabulary as assessed by parental reports systematically deviates from what could be expected based on the gold segmentation.

To conclude, we presented evidence that word segmentation algorithms can be distinguished through their correlation with reported infant word comprehension, providing a novel way of integrating cognitive considerations in modeling approaches of early language acquisition.

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